

1 **MEG analysis of neural dynamics in Attention-Deficit/**  
2 **Hyperactivity Disorder with Fuzzy Entropy**

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22 **Abstract-** The aim of this study was to analyze the neural dynamics in Attention-  
23 Deficit/Hyperactivity Disorder (ADHD). For this purpose, magnetoencephalographic  
24 (MEG) background activity was analyzed using fuzzy entropy (FuzzyEn), an entropy  
25 measure that quantifies signal irregularity, in 13 ADHD patients and 14 control  
26 children. Additionally, relative power (RP) was computed in conventional frequency  
27 bands (delta, theta, alpha, beta and gamma). FuzzyEn results showed that MEG activity  
28 was more regular in ADHD patients than in controls. Moreover, we found an increase  
29 of power in delta band and a decrease in the remaining frequency bands. Statistically  
30 significant differences ( $p$ -values  $< 0.05$ ; nonparametric permutation test for multiple  
31 comparisons) were detected for FuzzyEn in the posterior and left temporal regions, and  
32 for RP in the posterior, anterior and left temporal regions. Our results support the  
33 hypothesis that ADHD involves widespread functional brain abnormalities, affecting  
34 more areas than fronto-striatal circuits, such as the left temporal and posterior regions.

35

36 **Keywords-** Attention-Deficit/Hyperactivity Disorder, fuzzy entropy, relative power,  
37 magnetoencephalography.

38

## 39        **1. INTRODUCTION**

40            Attention-Deficit/Hyperactivity Disorder (ADHD) is the psychiatric disorder most  
41 commonly diagnosed and treated in children. Its prevalence ranges between 8% and  
42 12% children worldwide. Additionally, at least half of children with the disorder will  
43 continue suffering the symptoms in adulthood [1]. It is characterized by several  
44 behavioral disturbances, such as inattention, hyperactivity and impulsivity, which  
45 predispose the patients to academic and social dysfunctions, accidents or chaotic  
46 interpersonal relationships [2]. Pharmacotherapy helps children and adolescents with  
47 ADHD to concentrate and to be calmer, less hyperactive and more focused [3].  
48 Methylphenidate is the most commonly used medicine in the management of ADHD,  
49 whereas atomoxetine is recommended when the former fails. However, medication  
50 should always be offered as part of a comprehensive treatment plan [3], [4].

51            Initially, it was believed that the etiology of the disease consisted on one simple  
52 cause. However, nowadays ADHD is considered a complex, multifactorial disorder  
53 caused by the confluence of many different types of risk factors (e.g., genes, biological  
54 predisposition and psychosocial adversity) [5]. This multifactorial view of ADHD is  
55 consistent with the heterogeneity in its pathophysiology and clinical expression [1]. The  
56 ADHD pathophysiology profile comprises dysfunction in the fronto-subcortical  
57 pathways and imbalances in the dopaminergic and noradrenergic systems [2]. Brain  
58 imaging studies fit well with this concept and also involve the cerebellum and corpus  
59 callosum in the pathophysiology of ADHD [6].

60            The complexity of the diagnosis cannot be ignored. Because there is no objective  
61 test or marker for ADHD, diagnosis relies entirely on clinical criteria [1]. Although  
62 there are well-defined criteria (Diagnostic and Statistical Manual of Mental Disorders,

63 DSM, and International Statistical Classification of Diseases, ICD), clinicians must deal  
64 with data from multiple informants (parents, teachers and friends) and must attend to  
65 developmental variations in symptom expression (comorbidity is a key clinical feature  
66 observed in ADHD patients). This complexity may explain the discrepancies among  
67 clinicians and among different studies of the disorder [5]. Hence, new approaches are  
68 needed to understand ADHD [7], [8]. With this aim, the analysis of brain activity can be  
69 a noteworthy alternative.

70 The neurobiological basis of ADHD has been widely studied using neuroimaging  
71 techniques (for a review, see [9] and/or [10]). Initially, single photon emission  
72 computed tomography (SPECT) and positron emission tomography (PET) were used to  
73 study the involvement of basal ganglia [11], blood flow measurement [12] and cerebral  
74 glucose metabolism [13], among other parts and characteristics of the brain. However,  
75 these early studies showed some methodological concerns (poor subject matching,  
76 absence of control group, etc.). Hence, it is difficult to assess their results and make  
77 cross-comparisons. Later, other neuroimaging techniques, like functional magnetic  
78 resonance imaging (fMRI) and diffusion tensor imaging (DTI), enabled functional and  
79 structural connectivity studies, respectively [14]. Their main results suggest that the  
80 core symptoms of ADHD might derive from dysregulated modulation of cortical  
81 plasticity in the developing brain, which leads to altered patterns of corticocortical  
82 connectivity [14]. Structural connectivity studies involve alterations in the white matter  
83 frontostriatal and in the superior longitudinal fasciculus. Alternatively, functional  
84 connectivity studies put forward that functional disconnections within frontostriatal and  
85 mesocortico-limbic circuits play a fundamental role in the generation of ADHD  
86 symptoms. On the other hand, neurophysiological measures can provide complementary  
87 information to neuroimaging techniques about this issue [14].

88 Electroencephalography (EEG) and magnetoencephalography (MEG) measure the  
89 electric and magnetic fields generated by the neurons, respectively [15]. Both EEG and  
90 MEG have higher temporal resolution than PET and fMRI. Likewise, they record the  
91 neural activity directly, without the need to interpret it in terms of proxy measures, such  
92 as glucose consumption [15], [16]. MEG offers some advantages over EEG, since  
93 magnetic fields are reference-free and less affected by distortions produced by the  
94 resistive properties of the skull and the scalp [15]. On the other hand, MEG equipment  
95 is distinguished by limited availability and high costs in comparison to EEG devices  
96 [17], [18]. Previous researches have proven that the analysis of EEG/MEG activity can  
97 be useful to characterize the brain activity in ADHD [19].

98 The neurophysiology of ADHD has been mainly examined by means of  
99 quantitative EEG/MEG analyses and event-related potentials (ERPs). For resting EEG,  
100 a slowing of brain oscillatory activity in comparison to normal children was found. In  
101 this sense, an increase in relative theta power and a reduction in relative alpha and beta  
102 power, along with increased theta/alpha and theta/beta ratios, are the most reliably  
103 findings associated with ADHD [20], [21]. In the case of ERPs, a complex range of  
104 deficits has been associated with the disorder, for example, in the preparatory responses  
105 or auditory modality [22]. Studies using nonlinear measures have found a decrease of  
106 complexity in the MEG frontal activity of ADHD patients [23]. Kovatchev *et al.* [24]  
107 employed a consistency index, derived from a specific mathematical representation of  
108 EEG data, to validate the idea that ADHD interferes with transitions from one task to  
109 another. The differences were especially significant in male children, which reported  
110 good values of ADHD/control classification. Recent studies suggested that irregularity  
111 analyses based on entropy measures can provide valuable information to understand  
112 brain dynamics in ADHD. These studies found that MEG activity in ADHD patients

113 was less irregular than in controls [25] – [27]. In summary, nonlinear metrics and  
114 spectral analyses have been useful to explore the neurophysiological substrate of neural  
115 dysfunction in ADHD so far. Nevertheless, further research is indeed required to  
116 describe the neural dynamics associated with this disorder.

117 In this study, we analyzed the neural dynamics of ADHD by means of fuzzy  
118 entropy (FuzzyEn) and spectral analysis. FuzzyEn quantifies the signal irregularity and  
119 exhibits a more flexible behavior than other previous entropy metrics, due to the  
120 exponential function it uses as a classifier [28]. In addition, relative power (RP) in five  
121 frequency bands (delta, theta, alpha, beta and gamma) was calculated in order to explore  
122 the spectral content of MEG recordings. In the current research, we attempt to address  
123 the following questions: (i) Can FuzzyEn provide further insights into the underlying  
124 brain dynamics associated with ADHD?; (ii) Can spectral analysis provide  
125 complementary results to FuzzyEn?; (iii) Can FuzzyEn and RP results reflect the  
126 regional abnormalities of ADHD?

## 127 **2. MATERIAL AND METHODS**

### 128 *A. Subjects*

129 In this study, MEG recordings were acquired from 27 subjects. Thirteen children  
130 were included in the ADHD group (age =  $9.5 \pm 1.3$  years, mean  $\pm$  standard deviation,  
131 SD; range 8-12 years). They fulfilled the criteria of DSM-IV diagnosis of ADHD  
132 combined type with associated impairment in at least two settings and a Conners' Parent  
133 Rating Scale (CPRS) hyperactivity rating greater than two SD above age- and sex-  
134 specific means [29]. The DSM-IV used the parent version of the Diagnostic Interview  
135 for Children and Adolescents [30]. The patients had never taken any psychoactive drug  
136 or received any psychoactive therapy. The control group was formed by 14 children

137 (10.4 ± 1.5 years, mean ± SD; range 8-13 years) without past or present neurological  
138 disorders.

139 Both groups, patients and control subjects, had similar age and years of education  
140 (6.8 ± 1.2 years in ADHD patients and 7.3 ± 1.4 years in controls; mean ± SD). All of  
141 them were strictly right-handed. Children and parents gave their written informed  
142 consent and assent to participate in the study. The Institutional Review Board approved  
143 the research protocol.

#### 144 *B. MEG recording*

145 MEG signals were recorded from each participant using a 148-channel whole-  
146 head magnetometer (MAGNES 2500 WH, 4D Neuroimaging) placed in a magnetically  
147 shielded room at MEG Center “Dr. Pérez-Modrego” (Spain). Before the recording  
148 process, subjects were asked to remain in a relaxed state, lying in a bed, with their eyes  
149 closed and awake, in order to reduce the presence of artifacts in the recordings.

150 Five minutes of MEG data were acquired from each subject at a sampling  
151 frequency of 678.17 Hz. A process of down-sampling by a factor of four was carried  
152 out, resulting a sampling rate of 169.55 Hz. Data were digitally filtered using a 1-65 Hz  
153 band-pass filter and a 50 Hz notch filter. Both visual inspection and independent  
154 component analysis (ICA) were performed to minimize the presence of oculographic,  
155 cardiographic and myographic artifacts. A mean of 23.2 ± 14.1 artifact-free epochs of 5  
156 s (848 data points) per channel and subject were selected for further analyses. Figure 1  
157 shows examples of MEG epochs (channel A1, placed at central region) from an ADHD  
158 patient and a control.

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159 PLEASE, DISPLAY FIGURE 1 AROUND HERE

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### 160 C. Fuzzy entropy (*FuzzyEn*)

161 FuzzyEn is a measure of time series irregularity. Similar to other embedding  
162 entropies, as approximate entropy (ApEn) or sample entropy (SampEn), it provides  
163 information about how a signal fluctuates with time by comparing the time series with a  
164 delayed version of itself [31]. It is defined as the negative natural logarithm of the  
165 conditional probability that two similar vectors remain similar when the dimension  
166 changes from  $m$  to  $m + 1$  [28]. To compute FuzzyEn, three parameters must be fixed.  
167 The first parameter,  $m$ , is the length of the vectors to be compared, like in ApEn and  
168 SampEn. The other two ones,  $r$  and  $n$ , are the width and the gradient of the boundary of  
169 the exponential function, respectively. Similar to ApEn and SampEn, FuzzyEn can be  
170 applied to noisy physiological signals with relatively short datasets [28]. However,  
171 FuzzyEn provides some advantages over ApEn and SampEn. Firstly, using the concept  
172 of fuzzy set, FuzzyEn measures the similarity of two vectors by means of an  
173 exponential function rather than the Heaviside function, used by ApEn and SampEn.  
174 The latter function is a two-state classifier with a rigid boundary, unsuitable in the real  
175 physical world because of the ambiguity in the boundaries between different classes  
176 [28]. Due to the soft and continuous boundaries of fuzzy functions, FuzzyEn offers  
177 more flexibility in the selection of the parameters than ApEn and SampEn [32].  
178 Likewise, it ensures to be well-defined even at small values of such parameters.  
179 Secondly, FuzzyEn excludes self-matching (i.e., vectors are not compared to  
180 themselves) and considers only the first  $N - m$  vectors of length  $m$ , being  $N$  the length of  
181 the original time series. Therefore, all the compared vectors exist, even when their  
182 lengths change from  $m$  to  $m + 1$ . Finally, FuzzyEn removes the baseline in the  
183 construction of  $m$ -dimensional vectors. Thereby, vectors similarity depends on their  
184 shapes rather than their absolute coordinates. These features provide to FuzzyEn

185 stronger relative consistency and less dependence of data length than ApEn and  
 186 SampEn algorithms [28], [32].

187 Given a time series  $X = x(1), x(2), \dots, x(N)$  the FuzzyEn algorithm reads as  
 188 follows [28]:

189 1) Compose  $N-m+1$  vectors of length  $m$  such that:

$$190 \quad X_i^m = \{x(i), x(i+1), \dots, x(i+m-1)\} - x_0(i) \quad (1)$$

191 where  $x_0(i)$  is given by:

$$192 \quad x_0(i) = \frac{1}{m} \sum_{j=0}^{m-1} x(i+j) \quad (2)$$

193 2) Compute the distance,  $d_{ij}^m$ , between each two vectors,  $X_i^m$  and  $X_j^m$ , as the  
 194 maximum absolute difference of their corresponding scalar components:

$$195 \quad d_{ij}^m = d(X_i^m, X_j^m) = \max_{k \in (0, m-1)} [(x(i+k) - x_0(i)) - (x(j+k) - x_0(j))] \quad (3)$$

196 3) Given  $n$  and  $r$ , calculate the similarity degree,  $D_{ij}^m$ , between  $X_i^m$  and  $X_j^m$   
 197 through a fuzzy function  $\mu(d_{ij}^m, n, r)$ :

$$198 \quad D_{ij}^m(n, r) = \mu(d_{ij}^m, n, r) = \exp[-(d_{ij}^m)^n / r] \quad (4)$$

199 4) Define the function  $\phi^m$  as:

$$200 \quad \phi^m(n, r) = \frac{1}{N-m} \sum_{i=1}^{N-m} \left( \frac{1}{N-m+1} \sum_{j=1, j \neq i}^{N-m} D_{ij}^m \right) \quad (5)$$

201 5) Increase the dimension to  $m+1$ , form the vectors  $\{X_i^{m+1}\}$  and get the function  
 202  $\phi^{m+1}$ :

203 
$$\phi^{m+1}(n, r) = \frac{1}{N-m} \sum_{i=1}^{N-m} \left( \frac{1}{N-m+1} \sum_{j=1, j \neq i}^{N-m} D_{ij}^{m+1} \right) \quad (6)$$

204 6) Finally,  $FuzzyEn(m, n, r)$  is defined as the negative natural logarithm of the  
 205 deviation of  $\phi^m$  from  $\phi^{m+1}$ :

206 
$$FuzzyEn(m, n, r) = \lim_{N \rightarrow \infty} \{ \ln[\phi^m(n, r)] - \ln[\phi^{m+1}(n, r)] \} \quad (7)$$

207 which, for finite datasets, is estimated by the statistic:

208 
$$FuzzyEn(m, n, r, N) = \ln \phi^m(n, r) - \ln \phi^{m+1}(n, r) \quad (8)$$

209 *D. Spectral Analysis*

210 Spectral analysis is a classic approach to characterize electromagnetic brain  
 211 recordings. It offers a complementary view of the neural dynamics in comparison to  
 212 non-linear analysis. In this study, the power spectral density (PSD) for each MEG signal  
 213 was estimated as the Fourier transform of the autocorrelation function, according to the  
 214 Wiener-Khinchin-Einstein theorem [33]:

215 
$$PSD_x(k) = \frac{1}{N} \cdot \sum_{i=0}^{2N-1} R_{xx}(i) \cdot e^{-j \frac{2\pi k i}{2N-1}}, k = 0, 1, \dots, 2N-1, \quad (9)$$

216 where  $R_{xx}(i)$  denotes the discrete-time autocorrelation function of time series  
 217  $X = x(1), x(2), \dots, x(N)$ .

218 The PSD was then averaged for each channel and participant. Likewise, only  
 219 positive frequencies were selected to obtain the one-sided PSD. Finally, the one-sided  
 220 PSD was normalized to a scale from 0 to 1, leading to the normalized PSD ( $PSD_n$ ):

221 
$$PSD_n(m) = \frac{PSD_x(m)}{\sum_{m=m_1}^{m_2} PSD_x(m)}, m = 0, 1, \dots, N-1, \quad (10)$$

222 where  $m_1$  and  $m_2$  denote the discrete cut-off frequencies. They can be replaced by the  
 223 continuous frequencies  $f_1 = f_s \cdot m_1 / N$  and  $f_2 = f_s \cdot m_2 / N$ , where  $f_s$  represents the sampling  
 224 frequency, whereas  $f_1 = 1$  Hz and  $f_2 = 65$  Hz are the cut-off frequencies of the digital  
 225 band-pass filter.

226 The definition of RP was obtained summing the contribution of the spectral  
 227 components in the conventional frequency bands: delta (1-4 Hz), theta (4-8 Hz), alpha  
 228 (8-13 Hz), beta (13-30 Hz) and gamma (30-65 Hz):

$$229 \quad RP^{m_b} = \sum_{m \in m_b} PSD_n(m), m_b = \{\text{delta, theta, alpha, beta, gamma}\}, \quad (11)$$

230 where  $m_b$  denotes the discrete frequency range corresponding to each conventional  
 231 frequency band.

### 232 *E. Statistical Analysis*

233 Initially, an exploratory analysis was carried out to study the data distribution. In  
 234 order to evaluate the normality and the homoscedasticity of FuzzyEn and RP values, the  
 235 Lilliefors' test and the Bartlett's test were used, respectively. FuzzyEn and RP values  
 236 did not meet the parametric test assumptions. Hence, grand-averaged FuzzyEn and RP  
 237 values were compared between ADHD patients and control subjects by means of Mann-  
 238 Whitney  $U$ -tests ( $\alpha < 0.05$ ).

239 Statistical analyses at the sensor level for FuzzyEn and RP were carried out using  
 240 a multiple comparisons nonparametric permutation test [34]. This test is useful to  
 241 achieve a strong control over type I error in situations in which the multiplicity of  
 242 testing must be taken into account (e.g., 148 sensors). In permutation test, the  
 243 distributional assumption is weak. Typically, it is assumed that each distribution has the  
 244 same shape, though possibly different means. The null hypothesis asserts that the  
 245 distributions have equal means, and hence they are the same. Consequently, the

246 permutation of the distributions within the available observations leads to an equally  
247 likely statistic. Therefore, the goal is to compute the permutation distribution for the  
248 maximal statistic  $F^{max}$  (i.e., the maximum of the sensor statistics for each permutation).  
249 Multiple comparisons were then corrected by selecting a critical threshold at the  $c+1$   
250 largest member of the permutation distribution for  $F^{max}$ , where  $c = \lfloor \alpha N \rfloor$ ,  $\alpha N$  rounded  
251 down ( $\alpha$  represents the significance level, typically 0.05, and  $N$  is the number of  
252 permutations, 5000). Sensors with  $F$  statistics exceeding this threshold exhibit evidence  
253 against the corresponding sensor hypothesis at level  $\alpha$ . The corrected  $p$ -value for each  
254 sensor is estimated according to the proportion of the permutation distribution for  $F^{max}$   
255 that exceeds the observed sensor statistic [34].

### 256 3. RESULTS

#### 257 A. Optimization of FuzzyEn parameters

258 FuzzyEn is more flexible than other entropy algorithms to select the value of its  
259 parameters. Chen *et al.* [28] recommended choosing  $m$  such as  $N \in (10^m - 30^m)$ .  
260 Regarding the fuzzy similarity boundary determined by the other two parameters,  $r$  and  
261  $n$ , choosing narrow ones will enlarge the influence of the noise, whereas a broad  
262 boundary may cause an information loss. Thus, FuzzyEn was calculated for the 148  
263 MEG channels for all the combinations among the following parameter values:  $m = 1$ ,  
264 2;  $r = 0.1, 0.15, 0.20, 0.25$  times the SD of the original time series; and  $n = 1, 2, 3$ . The  
265 lowest  $p$ -value according to the Mann-Whitney  $U$ -test was achieved for the parameter  
266 combination: FuzzyEn (2,0.2·SD,3). As shown in Figure 2, the shape of the exponential  
267 function makes possible the maximal exploitation of its properties: continuity (there is  
268 no abrupt change like in Heaviside function) and convexity (its maximum correspond to  
269 the self-similarity case).

270

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271

*B. Global analysis*

272

FuzzyEn results were grand-averaged based on all the artifact-free 5 s epochs.

273

Mean values ( $\pm$  SD) for control and ADHD groups were  $0.4811 \pm 0.0376$  and  $0.4415 \pm$

274

0.0960, respectively. Consequently, we can infer that the brain abnormalities and

275

dysfunctions, which underlay ADHD, can be associated with a decrease in irregularity

276

of MEG activity. Figure 3 summarizes the boxplots of averaged results for each group.

277

Even though non-significant differences were observed, the results showed a trend

278

toward significance ( $p$ -value = 0.0680; Mann-Whitney  $U$ -test).

279

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280

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281

Additionally, RP in delta, theta, alpha, beta and gamma frequency bands was

282

calculated to complement FuzzyEn results. Figure 4 shows the normalized PSD for

283

control and ADHD groups. The spectral analysis showed a significant increase of RP in

284

delta band for ADHD patients ( $p$ -value = 0.0061; Mann-Whitney  $U$ -test). The results in

285

theta band showed that ADHD patients obtained lower RP values than controls. Even

286

though non-significant differences were found, a trend toward significance was

287

observed ( $p$ -value = 0.0688; Mann-Whitney  $U$ -test). In the remaining bands (alpha,

288

beta, gamma), control subjects exhibited higher values of RP than ADHD patients,

289

although differences were not statistically significant. RP mean values and the

290

corresponding  $p$ -values are shown in Table 1.

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291

PLEASE, INSERT TABLE 1 AND FIGURE 4 AROUND HERE

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292 *C. Sensor-level analysis*

293 In addition to global analysis, we explored the spatial patterns of FuzzyEn and RP  
294 values. The averaging process performed for global analysis may oversimplify ADHD  
295 related effects on MEG activity. For this reason, further analyses are needed to  
296 accurately characterize the neural activity in ADHD. Figure 5 depicts the brain maps  
297 showing the spatial distribution of the averaged FuzzyEn for each group and the  
298 corresponding statistical analyses (multiple comparisons nonparametric permutation  
299 test). The major differences can be appreciated in the posterior region, though some  
300 differences can also be observed in the left temporal and anterior regions. Significant  
301 differences did not appear in the global analyses due to the aforementioned averaging  
302 process.

---

303 PLEASE, DISPLAY FIGURE 6 AROUND HERE

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304 Finally, Figure 5 summarizes the spatial distribution of mean RP values for each  
305 frequency band and the corresponding statistical analyses. Delta band exhibits  
306 significant differences in the posterior, left temporal and anterior regions, whereas theta  
307 band shows only significant differences in the posterior and left temporal areas.  
308 Regarding alpha band, significant differences can be found in the posterior region. Beta  
309 band displays significant differences in anterior and posterior regions. Lastly,  
310 significant differences were found in the posterior area for gamma band.

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311 PLEASE, DISPLAY FIGURE 6 AROUND HERE

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## 4. DISCUSSION

In this paper, we have analyzed MEG background activity from 14 control subjects and 13 ADHD patients by means of FuzzyEn, a measure of time series irregularity. In addition, RP has been computed to complement the FuzzyEn results.

### A. *FuzzyEn and the neural activity of ADHD*

Regarding the first research question, we put forth the idea of whether FuzzyEn could be useful to provide further insights into the underlying brain dynamics of ADHD. Our findings support the notion that FuzzyEn provides an original description of ADHD neural dynamics. We found that ADHD patients show significantly lower FuzzyEn values than control subjects, especially in the posterior region. Hence, neural dynamics in ADHD are characterized by a less irregular neurophysiological behavior in this region. Moreover, these results agree with the hypothesis of a loss of physiological complexity due to diseases [35]. However, the dysfunctional implications of this decrease in MEG irregularity are not clear [9]. Initially, it was hypothesized that the neurobiological basis of ADHD involves structural and functional brain abnormalities in fronto-striatal circuits. This hypothesis has been widely supported by neuroimaging studies [10], [14]. However, a second hypothesis stresses that the abnormalities are more widespread and affect other cortical regions as posterior parietal cortex and the cerebellum [9]. Despite the fact that MEG signals are thought to reflect the cerebral cortex activity, previous work suggests that they can be also useful to study the activity of the cerebellum [36]. Several MRI studies detected a decreased size of the posterior inferior lobe of the cerebellum (lobules VIII-X) in ADHD patients in comparison with controls [37] – [41]. This reduction of the volume may explain the decrease in irregularity that was found in the posterior region. Consequently, the present results

336 would support the second hypothesis from a different perspective of neuroimaging  
337 techniques.

### 338 *B. Spectral analysis to complement non-linear measures*

339 The second research question addresses the issue of whether RP results could  
340 complement FuzzyEn results. Our findings indicate that they complement each other.  
341 All frequency bands show to some extent significant differences in the posterior region.  
342 Moreover, left temporal and anterior regions also exhibit significant differences in  
343 several frequency bands. Thereby, the spectral analysis involves at least the two cerebral  
344 regions in which the neurobiological substratum of the ADHD lies according to the  
345 second previous hypothesis (anterior region: prefrontal cortex; posterior region:  
346 cerebellum). In that way, we can suggest that, while the first hypothesis is necessary for  
347 explaining ADHD pathophysiology, it is not sufficient.

348 Although significant differences were found in the left temporal region for both  
349 FuzzyEn and RP (delta and theta bands), the pathophysiological explanation is  
350 uncertain. Only few neuroimaging cerebral studies reported significant differences in  
351 this area. For instance, Castellanos *et al.* [6] detected significantly reduced temporal  
352 lobe volumes. Sowell *et al.* [42] described abnormal morphology with reduced regional  
353 brain size in inferior portions of dorsal prefrontal cortices and in anterior temporal  
354 cortices, bilaterally. Again, these changes in size are believed to produce an irregularity  
355 reduction and a slowing in MEG background activity [9].

### 356 *C. Widespread abnormalities as core of ADHD pathophysiology*

357 We raised the third research question about whether there is a relationship  
358 between our results and the ADHD regional abnormalities. Taking into account that  
359 ADHD is considered as a multifactorial, heterogeneous and complex disorder [5], it  
360 seems more logic to think that its pathophysiology is caused by impaired interactions

361 among different parts of the brain, and not only by abnormalities or dysfunctions in a  
362 particular element. In sum, the second approach is more consistent with the etiological  
363 theory of the disorder and our results support it. In this sense, it should be investigated  
364 further to discover how genetic disorder, biological predisposition and social adversities  
365 modify brain development, leading to a heterogeneous neurobiological profile.  
366 Additionally, it should be noted that the prefrontal cortex is one of the brain areas more  
367 developed in the human beings and is among the latest cerebral regions that complete  
368 their development. Hence, the functions that prefrontal cortex controls or carries out  
369 may be more sensitive and, therefore, more easily detectable [43]. This may partially  
370 explain why originally several neuroimaging studies have postulated the prefrontal  
371 cortex and its connections with other cortical regions (fronto-striatal circuits) as the  
372 main pathophysiological basis of ADHD.

373         According to our results and other neuroimaging studies, an element that may be  
374 involved is the cerebellum. The cerebellum is associated with the coordination and the  
375 motor motion. It also plays a role in executive functions, such as timing of events,  
376 cognitive planning or affective processes, and has connections with the frontal brain  
377 [44]. The left temporal region also showed significant differences. This region contains  
378 areas relevant to the auditory-linguistic function. Consequently, both may be of interest  
379 in ADHD. Additionally, the dopamine transporter may play a crucial role. It is thought  
380 that a deficit or an excess of noradrenaline or dopamine receptor stimulation impairs  
381 neural and subsequent cognitive functions (working memory, executive functions, etc.),  
382 known to be deficient in ADHD [45]. Besides, projections from the ventral tegmental  
383 area, where is the origin of the dopaminergic cell bodies of the mesocorticolimbic  
384 dopamine system, to the striatum and the prefrontal cortex are fundamental in motor  
385 control and attention [46]. Finally, high levels of catecholamine released during severe

386 stress may disrupt cognitive functions of the prefrontal cortex [45]. Similarly,  
387 alterations in the superior longitudinal fasciculus [14], a pair of long bi-directional  
388 bundles of neurons connecting the front and the back of the cerebrum, emphasize the  
389 idea of that ADHD cerebral alterations and dysfunction are widespread.

#### 390 *D. Limitations and future research lines*

391 There are some concerns that merit consideration. First of all, the size of the  
392 sample is small. This shortcoming causes that our findings must be taken as preliminary  
393 results. Hence, this approach should be extended on a much larger patient population,  
394 especially to assess the usefulness of FuzzyEn and/or RP as diagnostic tools, as well as  
395 to analyze the changes induced in the brain activity by pharmacological and non-  
396 pharmacological therapies. Secondly, one cannot forget the comorbidity of mental  
397 disorders. The detected decrease of MEG irregularity is not specific of ADHD. It  
398 appears in other physiological and pathological states in children, such as sleep [47] or  
399 epilepsy [48]. Regarding the spectral analysis, the same observation can be made. For  
400 instance, Onoe and Nishigaki [49] also perceived an increase of the delta power in  
401 febrile delirium children patients. Finally, we would like to indicate that brain imaging  
402 techniques are not absent from debate either [50]. The multitude of analytic techniques  
403 and measurements employed in different studies make difficult replication and cross-  
404 study comparisons [14].

## 405 **5. CONCLUSION**

406 In summary, FuzzyEn and spectral analyses of MEG activity exhibited significant  
407 differences mainly in the posterior and left temporal regions. The results support the  
408 hypothesis that the pathophysiology of ADHD is not only focused on a particular area,  
409 such as fronto-striatal circuits, but it is more widespread and it affects other parts of the  
410 brain, like the cerebellum. Along with the possible cerebral abnormalities, other factors

411 involved in the ADHD pathophysiology may also explain the differences (e.g., the  
412 dopamine transporter, projections from the ventral tegmental area to the striatum and  
413 the prefrontal cortex, high levels of catecholamine released during severe stress or  
414 alterations in the superior longitudinal fasciculus). The previous ideas are consistent  
415 with its multiple etiology pathways and agree with the results provided by  
416 neuroimaging studies.

417

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424

425 **CONFLICT OF INTEREST**

426 There are no conflicts of interest that could inappropriately influence this  
427 research work.

428

429 **ETHICAL APPROVAL**

430 Psychiatry service of Hospital Clinico San Carlos with number: 12/106-E.

431

432 **AUTHORSHIP RESPONSIBILITY**

433 • The material in this manuscript is original and contains no matter libelous or  
434 otherwise unlawful.

435 • The manuscript represents valid work and that neither this manuscript nor any other  
436 with substantially similar content under my authorship has been published or is  
437 being considered for publication elsewhere.

438 • I have participated sufficiently in the work to take public responsibility for all its  
439 content.

440

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- 572

573 **TABLE CAPTIONS**

574 Table 1. RP values (mean  $\pm$  SD) in the delta, theta, alpha, beta and gamma frequency  
575 bands for ADHD patients and control subjects, together with the corresponding  
576 statistical analyses (Mann-Whitney *U*-test).

577

578 **FIGURE LEGENDS**

579 Figure 1. Example of MEG time series from (a) an ADHD patient and (b) a control  
580 subject.

581 Figure 2. Exponential function used in vector similarity measurement of FuzzyEn for  
582 the combination:  $m = 2$ ,  $r = 0.2 \cdot SD$  and  $n = 3$ .

583 Figure 3. Boxplots of the grand-averaged FuzzyEn results.

584 Figure 4. Grand-averaged normalized PSD for control subjects and ADHD patients.

585 Figure 5. Topographic brain maps of averaged FuzzyEn values for each group and the  
586 corresponding statistical analyses (nonparametric permutation test corrected for multiple  
587 comparisons).

588 Figure 6. Topographic brain maps of the averaged RP for each group and the  
589 corresponding statistical analyses (nonparametric permutation test corrected for multiple  
590 comparisons) at (a) delta, (b) theta, (c) alpha, (d) beta and (e) gamma frequency bands.