Modelling of adsorption and intercalation of hydrogen on/into tungsten disulphide multilayers and multiwall nanotubes

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Modelling of adsorption and intercalation of hydrogen on/into tungsten disulphide multilayers and multiwall nanotubes

José I. Martínez, a,* Alex Laikhtman, b Hoi Ri Moon, c Alla Zak, b and Julio A. Alonso d,†

Understanding the interaction of hydrogen with layered materials is crucial in the fields of sensors, catalysis, fuel cells and hydrogen storage, among others. Density functional theory, improved by the introduction of van der Waals dispersion forces, provides an efficient and practical workbench to investigate the interaction of molecular and atomic hydrogen with WS\textsubscript{2} multilayers and nanotubes. We find that H\textsubscript{2} physisorbs on the surface of those materials on top of W atoms, while atomic H chemisorbs on top of S atoms. In the case of nanotubes, the chemisorption strength is sensitive to the nanotube diameter. Diffusion of H\textsubscript{2} on the surface of WS\textsubscript{2} encounters quite small activation barriers whose magnitude helps to explain new experimental results for the observed dependence of the hydrogen concentration with temperature. Intercalation of H\textsubscript{2} between adjacent planar WS\textsubscript{2} layers reveals an endothermic character. Intercalating H atoms is energetically favorable, but the intercalation energy does not compensate for the cost of dissociating the molecules. When H\textsubscript{2} molecules are intercalated between the walls of a double wall nanotube, the rigid confinement induces the dissociation of the confined molecules. A remarkable result is that the presence of a full H\textsubscript{2} monolayer adsorbed on top of the first WS\textsubscript{2} layer of a WS\textsubscript{2} multilayer system strongly facilitates the intercalation of H\textsubscript{2} between WS\textsubscript{2} layers underneath. This opens up an additional gate to intercalation processes.

1. Introduction

After graphene, a new generation of layered two-dimensional (2D) materials has emerged due to their excellent electronic, optical and mechanical properties. Within this family, hexagonal boron nitride (h-BN), some transition metal oxides, transition metal dichalcogenides (TMDCs), and new materials such as black phosphorus, germanene and antimonene, cover a wide range of properties expected to be profitable in diverse applications. In particular, TMDCs are formed by chalcogen elements (X = S, Se, Te, among others) and transition metals (M = Mo, W, Ti, Zr, Hf, among others) piled up in a layered structure. Here the molecular MX\textsubscript{2} layers are bonded to each other by weak van der Waals forces, while each molecular layer consists of an atomic metal layer sandwiched by two atomic chalcogen layers (X-M-X) bonded by strong covalent bonds. The layers can be easily exfoliated, as it occurs with graphene layers in graphite.

Single MX\textsubscript{2} layers often show different properties compared to their corresponding bulk materials. For instance, these materials present electronic band-gaps whose magnitude depends on the number of stacked layers. Moreover, Mak et al.\textsuperscript{2} and Splendiani \textit{et al.}\textsuperscript{3} demonstrated that monolayers of trigonal prismatic MoS\textsubscript{2} undergo an indirect-to-direct electronic band gap transition which originates from quantum confinement. As a result, strong photoluminescence emerges, so offering novel applications of such monolayers for a variety of electronic and optical devices. Atomic defects in the layers can act locally as catalytic regions. All these properties make dichalcogenide nanostructures composed of one or few-layers very appealing for applications in different fields: sensors and biosensors,\textsuperscript{4} nanoelectronics,\textsuperscript{4-6} optoelectronics,\textsuperscript{5,7} spintronics,\textsuperscript{4} catalysis,\textsuperscript{1,7} energy storage,\textsuperscript{8,9} and hydrogen storage.\textsuperscript{10} Studies of transition metal chalcogenides (CoS, CuS)\textsuperscript{11,12} and dichalcogenides (WS\textsubscript{2}, VS\textsubscript{2})\textsuperscript{13-15} have delivered promising results towards the development of optical and electrochemical sensors and biosensors.

The interaction of hydrogen with a variety of materials is highly relevant to the development of hydrogen cells and hydrogen storage. Novel storage methods based on the hydrogen-surface interaction have been proposed. These methods are intended to replace the present technology of storing hydrogen in steel tanks at high pressures. One of these alternative techniques involves storing hydrogen in porous and layered materials. The storage mechanism
in this case is based on the adsorption of molecular hydrogen on the inner surface of the pores, or in between adjacent layers. Thus, a large effective area available for adsorption is likely to result in a large amount of stored hydrogen. Storage in porous carbons and carbon nanotubes has been studied in depth, both experimentally and by computer simulations. The atomic structure of the pore walls in porous carbons is similar to that of graphene ribbons, although often curved and with abundant defects. The interaction between $H_2$ and the graphitized walls is weak and dominated by dispersion interactions.

Another interesting effect is that functionalization of the surface of layered materials with atomic hydrogen can be used to change the properties of these materials. For instance, a variety of chemisorbed hydrogen dimer structures was formed upon room-temperature adsorption of atomic hydrogen on single layer graphene grown on SiC(0001). In such a way a local doping of the graphene lattice was induced. Besides, it has been recently reported that the chemisorption of atomic $H$ generates a magnetic moment in graphene. The magnetic moment is characterized by an ~20 meV spin-split state at the Fermi energy, essentially localized on the carbon sublattice opposite to the one where the hydrogen atom is chemisorbed. Additionally, full functionalization of graphene with hydrogen produces a material, graphene, with different electronic properties. In the case of TMDs, the modification of the electronic properties of MoS$_2$ due to hydrogen adsorption is the basis for the construction of hydrogen chemical sensors with this material.

The interaction between hydrogen and inorganic layered materials has been explored to a much lesser extent than for carbon-based structures. The hydrogen storage properties of multilayer nanotubes of MoS$_2$, TiS$_2$, and BN were investigated in several studies. Tenne and co-workers were the first who reported that the TMDs with layered structures, like WS$_2$ and MoS$_2$, can form closed-cage nanoparticles with polyhedral or nanotubular shapes. An experimental investigation of the interaction of hydrogen with WS$_2$ nanotubes and fullerene-like nanoparticles, and their capacity to store hydrogen, has been reported in two previous publications and some preliminary ideas on the interaction have been proposed. Various hydrogenation methods were applied in those experiments: hydrogenation by high-pressure molecular hydrogen, as well as microwave and radiofrequency (RF) plasma-enhanced hydrogenation performed at low gas pressures. Our main goal in this work is to further elucidate the details of the interaction between hydrogen and WS$_2$. For that purpose we present an exhaustive theoretical first-principles investigation of different aspects of the interaction between hydrogen and different varieties of layered WS$_2$ materials: single layers, multilayers and nanotubes. We have investigated adsorption of atomic and molecular hydrogen on the surfaces, dissociation of $H_2$ diffusion, and intercalation between the WS$_2$ layers, which can help to interpret the results of the hydrogenation experiments. In addition, we present some new experimental results on hydrogen adsorption that can be interpreted in the light of the diffusion calculations.

The theoretical methods used in the calculations are presented in Section 2, and the pure WS$_2$ materials, planar multilayers and nanotubes are described in Section 3. Sections 4 and 5 present the results of the adsorption of molecular and atomic hydrogen, respectively. The study of the diffusion of molecular and atomic hydrogen in Section 6 is used to interpret new hydrogenation experiments also reported in that Section. The intercalation of hydrogen between layers in multilayers and double-walled nanotubes is investigated in Section 7, and the Raman spectrum of physisorbed $H_2$ molecules is modelled in Section 8. The conclusions of this work are summarized in Section 9.

2. Computational Methods

Atomistic simulations for planar and curved layered WS$_2$ materials, clean and with hydrogen adsorbed, have been performed with the density functional formalism (DFT), as implemented in the plane-wave package QUANTUM ESPRESSO. Only valence electrons have been explicitly taken into account, and the ionic cores have been described by Projector Augmented Wave (PAW) pseudopotentials. The Perdew-Burke-Ernzerhof (PBE) generalized gradient approximation (GGA) functional has been used for electronic exchange and correlation (XC) effects. Because long-range dispersion interactions are expected to be relevant in the interaction between hydrogen and the WS$_2$ surface, a perturbative van der Waals correction was applied. For this purpose, we have used an empirical $r^{-6}$ correction to add dispersive forces to conventional density functionals within the DFT+D formalism. To optimize the geometrical configurations, structural relaxations were performed within a conjugate-gradient minimization scheme until the maximum force on any atom was below 0.01 eVÅ$^{-1}$. The self-consistent calculations were performed with a plane-wave cutoff of 500 eV. The Fermi level was smeared out using the Methfessel-Paxton approach with a Gaussian width of 0.01 eV, and all energies were extrapolated to T=0 K. The Brillouin zone was sampled by employing optimal Monkhorst-Pack grids. With these setups, total energies are converged to a precision better than 10$^{-6}$ eV, and adsorption energies are obtained with accuracies of 0.01 eV.

Apart from the enthalpies of $H_2$ adsorption and dissociation, an important feature to ascertain the competition between molecular adsorption and dissociative chemisorption is the height of the dissociation barrier. Transition states have been investigated herein with the climbing-image nudged elastic band (CI-NEB) approach implemented in the QUANTUM ESPRESSO package, where the initial, final, and a sufficient number of intermediate image-states (30 in the present case) were free to fully relax. This CI-NEB method has several desirable advantages: i) it converges to a minimum energy path (MEP), providing sufficient resolution in the discrete representation of the path when enough images are included in the seeking process; ii) it only requires evaluation of the interaction energy and the first derivative of the energy with respect to coordinates; iii) the convergence to the MEP is decoupled from the discrete representation of the path, making the former robust and the latter flexible; iv) the method guarantees to provide a
continuous path even when multiple MEPs exist. Within this approach we have computed the minimum energy paths, as well as the height of the corresponding energy barriers at the transition states for surface diffusion of atomic and molecular hydrogen, and dissociation of H₂ on the WS₂ surface.

We have used a supercell approach and periodic boundary conditions to model the layered WS₂ materials: a single planar layer, a trilayer, a surface, and the bulk crystal. In the calculations for the layer, trilayer and surface we have considered a distance of about 25 Å of empty space between neighbouring supercells along the axis perpendicular to the layers (say, the z-axis). To obtain the optimal structures, the positions of the atoms were allowed to fully relax during the optimizations, and the lattice parameters along the two directions parallel to the layers were optimized. To model the WS₂ surface, five layers were considered, and the distance between the two bottom layers was kept fixed at the calculated bulk separation. The Brillouin zone for all the systems was sampled by using a [4×4×1] Monkhorst-Pack grid, guaranteeing good convergence in energy and electronic density. In the (4×4) unit cell of all the layered systems considered, the unit cell in each WS₂ layer, with optimized size of (12.6×12.6) Å², contains 48 atoms (16 W and 32 S atoms) showing perfectly balanced WS₂ stoichiometry.

We have also investigated a large variety of WS₂ nanotubes (NTs). Periodic boundary conditions have been applied along the longitudinal tube axis, to model nanotubes of infinite length. In addition, we have taken a distance of at least 15 Å of vacuum between neighbouring supercells along the two lateral directions perpendicular to the nanotube axis. All the atom positions were allowed to fully relax in the structural optimization process, and the lattice parameter parallel to the nanowire axis was fully optimized. The Brillouin zone for all the nanotube systems was sampled by using a [8×1×1] Monkhorst-Pack grid, once again guaranteeing good convergence in energy and electronic density.

3. Clean Planar and Curved Layered WS₂ Materials

Tungsten disulphide is a compound formed by WS₂ layers. Each layer is itself a sandwich formed by two planes of sulphur atoms with a plane of tungsten atoms in between. The chemical bonding between W and S atoms is strong inside each sandwich, where each W atom is coordinated to six S atoms forming a trigonal prism. On the other hand, the bonding between adjacent WS₂ layers is weak. The calculated inter-layer distance in the bulk (distance between the W planes) is 6.15 Å, which deviates by only 1.2 % from the experimental value of 6.23 Å. The trilayer (three WS₂ layers) and the surface are shown in Figure 1. The optimized inter-layer distance in the trilayer is 6.13 Å. In the case of the surface, the optimized distance between layers is 6.14 Å, intermediate between those for the trilayer and the bulk (notice that the separation between the two bottom layers in the surface model used here is fixed at 6.15 Å).

We have investigated single-wall WS₂ nanotubes of different chiralities and diameters: arm-chair (8,8), (10,10), (12,12), (14,14), (16,16) nanotubes, and zig-zag (16,0), (20,0), (24,0), (28,0), (32,0) nanotubes. We also studied the representative double-walled (8,8)@(16,16), (10,10)@(16,16), (16,0)@(28,0) and (20,0)@(32,0) nanotubes. Cross section views of these nanotubes are plotted in Figures 1 and 2. The distances between the inner and the outer walls in the double-walled nanotubes are close to 6.21 Å, slightly higher than the interlayer distances for planar systems (6.13-6.15 Å). This trend is consistent with the experimental data on multiwall nanotubes, which also reveals larger interlayer separations than the WS₂ solid. The cross sections of all the nanotubes are perfectly circular (see Figures 1 and 2). Taking the arm-chair (10,10) and the zig-zag (20,0) nanotubes as specific examples, the maximum (outermost S atoms) and minimum (innermost S atoms) diameters of these nanotubes are 22.4 Å / 16.1 Å in the first tube, and 25.2 Å / 18.8 Å in the second. We then estimated the diameters of the single-wall nanotubes, DNT, by taking the average between the maximum and minimum diameters for each nanotube. This estimation results in diameters of 15.7 Å, 19.2 Å, 22.4 Å, 26.1 Å and 29.4 Å for the arm-chair (8,8), (10,10), (12,12), (14,14) and (16,16) nanotubes, respectively, and 18.4 Å, 22.0 Å, 25.9 Å, 30.2 Å and 34.0 Å for the zig-zag (16,0), (20,0), (24,0), (28,0) and (32,0) nanotubes, respectively.
Figure 1. Top panel: optimized structures of the WS$_2$ trilayer and surface. Bottom panel: optimized structures of (left) the arm-chair (m,m) single-wall WS$_2$ nanotubes with m=8, 10, 12, 14, and 16, and (right) the zig-zag (m,0) single-wall WS$_2$ nanotubes with m=16, 20, 24, 28 and 32. W and S atoms are represented by blue and golden spheres, respectively.

As a test of the robustness and thermal stability of the optimized structures obtained in the calculations, constant temperature molecular-dynamics simulations were performed by heating some nanotubes up to a temperature T = 850 °C, and all the structures were verified to be stable. This result is consistent with the experimental observation that fullerenic-like multilayer WS$_2$ nanoparticles are thermally stable at this temperature.

4. Adsorption of Molecular Hydrogen

Calculations have been performed to model the adsorption of molecular hydrogen on different layered WS$_2$ structures. As a first step we have investigated the adsorption of H$_2$ on the most relevant adsorption sites of the planar WS$_2$ structures, single layer, trilayer and surface, for the following orientations of the molecular axis: (a) H$_2$ molecules laying parallel to the layer on top of a W atom; (b) molecules perpendicular to the layer on top of a W atom; (c) molecules parallel to the layer on top of a S atom; (d) molecules perpendicular to the layer on top of a S atom. Those configurations are plotted in Figure 3. The calculations reveal that the H$_2$ molecules prefer sitting on top of a W atom, so the coverage will be defined as the fraction of W atoms with an adsorbed H$_2$ molecule. Different coverages, x (monolayer fraction), have been investigated, ranging between low coverage, $x = 0.0625$ ML (one H$_2$ molecule per unit cell of the surface layer), up to full coverage, $x = 1$ ML. Full coverage is achieved with 16 adsorbed molecules per unit cell because the number of W atoms in the unit cell chosen is 16. The adsorption energies per H$_2$ molecule for coverage $x$ are defined by the following expression:

$$E_{ads}(xML) = \frac{E(clean) + nE(H_2) - E(xML)}{n}, \quad (1)$$

where $E(xML)$ is the energy per unit cell of the system with $x$ molecules and the closest plane of S atoms, corresponding to a fraction $x$ of a monolayer, $E(clean)$ is the energy of the corresponding unit cell of the clean system (no hydrogen adsorbed), and $nE(H_2)$ is the energy of $n$ isolated gas molecules, where n is the number of hydrogen molecules in the unit cell for coverage $x$. The results for adsorption on a single WS$_2$ layer at the coverage of one H$_2$ molecule per unit cell ($x = 0.0625$ ML) are presented in Table 1.

Table 1. Adsorption energies $E_{ads}$ (in eV) per H$_2$ molecule on a WS$_2$ layer, and distances $d_{ads}$ (in Å) between the H$_2$ molecules and the closest plane of S atoms, for the four relevant adsorption configurations: (a) parallel on top of a W atom, (b) perpendicular on top of W, (c) parallel on top of S, (d) perpendicular on top of S. The coverage is $x = 0.0625$ ML.

<table>
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<th>Configuration</th>
<th>(a)</th>
<th>(b)</th>
<th>(c)</th>
<th>(d)</th>
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<tr>
<td>$E_{ads}$ (eV)</td>
<td>0.065</td>
<td>0.073</td>
<td>0.048</td>
<td>0.051</td>
</tr>
<tr>
<td>$d_{ads}$ (Å)</td>
<td>2.83</td>
<td>2.95</td>
<td>3.41</td>
<td>3.37</td>
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The adsorption energies are positive in all cases; that is, molecular adsorption is favourable. Their values are small, typical of the physisorption regime. The calculations reveal two preferential adsorption configurations: these are the configurations (a) and (b), corresponding to adsorption of H$_2$ on top of W atoms, where a triangular hollow formed by three S atoms permits the easy accommodation of physisorbed H$_2$ molecules. The adsorption energies for these two configurations, 0.065 eV and 0.073 eV, respectively, are not too different. The corresponding adsorption distances (distance between the centre of mass of the H$_2$ molecule and the closest plane of S atoms) are 2.83 Å and 2.95 Å for the parallel and perpendicular orientations of the molecule, respectively. This difference is mainly an effect of the orientation: in the perpendicular orientation, the H atom closest to the plane of S atoms is at a distance of 2.57 Å, and this short distance is the reason for the higher physisorption energy of the molecule. The results for adsorption on top of S atoms are also reported in Table 1. The number of S atoms in the upper plane of a WS$_2$ layer is also 16, so the coverage $x = 0.0625$ ML corresponds to the same number of molecules per unit cell as in the case of adsorption on W atoms. Adsorption on S atoms leads to longer adsorption distances.
compared to adsorption on W atoms, and consequently produces lower adsorption energies. The molecule-layer distances, i.e., the distance between the centre of mass of the H$_2$ molecule and the closest plane of S atoms, are 3.41 Å and 3.37 Å for the (c) and (d) configurations, respectively. These large values also result in a weaker dependence of adsorption energy and adsorption distance on the orientation of the molecule.

Then, the H$_2$ physisorption energies and distances have been monitored as a function of H$_2$ coverage. Four different coverages have been investigated: 0.0625 ML (one H$_2$ molecule per unit cell), 0.25 ML (4 molecules per unit cell), 0.5 ML (8 molecules per unit cell), and 1 ML (16 molecules per unit cell). The results for adsorption on a W atom (configurations called (a) and (b) above) of the single WS$_2$ layer are presented in Table 2. For given coverage values, the perpendicular configuration yields higher adsorption energies as compared to the parallel configuration. The adsorption energies per H$_2$ molecule decrease slightly with increasing adsorption coverage: from 0.065 eV to 0.059 eV for configuration (a), and from 0.073 eV to 0.064 eV for configuration (b). This decrease arises from repulsive interactions between neighbour H$_2$ molecules: the H$_2$–H$_2$ interaction potential is repulsive for distances smaller than 3.4 Å between the two molecules. As a result, adsorption distances increase slightly with coverage for both configurations. The adsorption energies per H$_2$ molecule and the adsorption distances for the (c) and (d) configurations with the H$_2$ molecules adsorbed on S atoms (not shown in Table 2) practically do not vary with coverage within the range 0.0625—1 ML, yielding values of 0.048—0.047 eV and 3.36—3.37 Å for configuration (c), and 0.051—0.050 eV and 3.41—3.42 Å, for configuration (d). These values are nearly independent of coverage. As such they confirm the idea of a weaker dependence of adsorption energy and adsorption distance on the orientation of the molecule for these two configurations.

**Figure 3.** Top (left) and side (right) views of: a) H$_2$ molecule adsorbed on top of a W atom of a single WS$_2$ layer with the molecular axis parallel to the layer; b) H$_2$ molecule adsorbed on top of a W atom with the axis perpendicular to the layer; c) H$_2$ molecule adsorbed on top of a S atom with the axis parallel to the layer; d) H$_2$ molecule adsorbed on top of a S atom with the axis perpendicular to the layer. Blue, golden and white spheres represent W, S and H atoms, respectively.

**Table 2.** Adsorption energies $E_{\text{ads}}$ (in eV) per H$_2$ molecule, and adsorption distances $d_{\text{ads}}$ (in Å) between the H$_2$ molecules and the closest plane of S atoms, for the two most stable adsorption configurations: (a) H$_2$ on top of a W atom with the axis parallel to the layer; (b) H$_2$ on top of a W atom with the axis perpendicular to the layer; (c) H$_2$ molecule adsorbed on top of a S atom with the axis parallel to the layer; (d) H$_2$ molecule adsorbed on top of a S atom with the axis perpendicular to the layer. The results are the same for the WS$_2$ layer, the trilayer, and the bulk surface.

<table>
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<tr>
<th>H$_2$ Coverage</th>
<th>Config. (a) $E_{\text{ads}}$ (eV)</th>
<th>$d_{\text{ads}}$ (Å)</th>
<th>Config. (b) $E_{\text{ads}}$ (eV)</th>
<th>$d_{\text{ads}}$ (Å)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.0625 ML</td>
<td>0.065</td>
<td>2.83</td>
<td>0.073</td>
<td>2.95</td>
</tr>
<tr>
<td>0.25 ML</td>
<td>0.064</td>
<td>2.84</td>
<td>0.071</td>
<td>2.96</td>
</tr>
<tr>
<td>0.5 ML</td>
<td>0.062</td>
<td>2.84</td>
<td>0.067</td>
<td>2.96</td>
</tr>
<tr>
<td>1 ML</td>
<td>0.059</td>
<td>2.86</td>
<td>0.064</td>
<td>2.98</td>
</tr>
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</table>

It is important to notice that the numerical results of Table 2 do not change for adsorption on the surface of a trilayer or on the surface of bulk WS$_2$. This means that the van der Waals interactions between the WS$_2$ layers do not affect the interaction between H$_2$ and the outermost layer. However, the H$_2$ adsorption on the topmost layer of the WS$_2$ multilayers (trilayer and surface) induces a widening of the distance between the topmost and the second WS$_2$ layers. This decoupling is enhanced by increasing H$_2$ coverage: the interlayer distances of 6.13 Å for the clean trilayer and 6.14 Å for the clean surface, increase up to 6.21 Å and 6.23 Å, respectively, for full coverage of $x = 1$ ML. Another relevant observation is that the strength of the adsorption energies is similar to those for H$_2$ on graphene.

Similar phenomena occur in nanotubes. Table 3 lists the results for low coverage of the outermost wall of three double-walled nanotubes, (10,10)@(16,16), (16,0)@(28,0) and (20,0)@(32,0). Namely, the coverage is one adsorbed H$_2$ molecule per nanotube unit cell, comparable to the coverage $x = 0.0625$ ML in planar layers. The most stable adsorption configurations are again the configurations (a) and (b) described above. The adsorption energies and adsorption distances are very close to those for low coverage, $x = 0.0625$ ML, on the planar WS$_2$ structures. No noticeable correlation is found between the adsorption energies and the nanotube diameters (neither for single-wall nor for double-walled nanotubes), with $E_{\text{ads}}/H_2$ ranging between 0.063—0.060 eV and 0.072—0.068 eV for the (a) and (b) configurations, respectively. We show below that this behaviour is different for chemisorption of atomic hydrogen. When H$_2$ molecules are adsorbed on the innermost wall of the nanotubes, that is, on the hollow internal surface of the nanotubes, the preferred adsorption configurations are again configurations (a) and (b), and the adsorption energies are practically the same as for adsorption on the external wall. A slight increase in the adsorption distances occurs by increasing the H$_2$
content. For instance, an increase of 0.03 Å is observed for external adsorption in configuration (a) when the H₂ content increases up to 0.5 ML, and an increase of 0.06 Å for internal adsorption.

Table 3. Adsorption energies $E_{ads}$ per H₂ molecule (in eV), and adsorption distances $d_{ads}$ (in Å) for the most stable adsorption configurations, (a) and (b), on either the outer- or the innermost wall of double wall nanotubes. The values are given for the low coverage: one molecule adsorbed per nanotube unit cell.

<table>
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<tr>
<th>Nanotube</th>
<th>Config. (a)</th>
<th>Config. (b)</th>
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<tr>
<td></td>
<td>$E_{ads}$ (eV)</td>
<td>$d_{ads}$ (Å)</td>
</tr>
<tr>
<td>(10,10)@(16,16)</td>
<td>0.063</td>
<td>2.83</td>
</tr>
<tr>
<td>(16,0)@(28,0)</td>
<td>0.061</td>
<td>2.84</td>
</tr>
<tr>
<td>(20,0)@(32,0)</td>
<td>0.061</td>
<td>2.84</td>
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An interesting possibility to be explored is the adsorption of more than one hydrogen monolayer on the surface of planar platelets. For this purpose we performed computer simulations in which the starting configuration was formed by H₂ molecules on top of all W and S atoms, which corresponds to 2 ML coverage in the notation used above. All the molecules were initially placed as a single layer parallel to the surface. Their centres of mass are separated by a distance of 2.9—3.0 Å from the topmost plane of S atoms, and the molecules are orientated perpendicular to the WS₂ layer. Structural relaxation of the system allowed the hydrogen molecules to optimize their positions, forming two layers as shown in Figure 4. In all cases the molecular axes conserved a nearly perpendicular orientation. The H₂ molecules of the layer closest to WS₂ sit on top of W atoms, like in the case of a single H₂ layer discussed above. These molecules are at a distance of 2.84 Å from the plane of S atoms, very close to the distance of 2.86 Å for 1 ML coverage in Table 2. The H₂ molecules of the upper layer rest on sites above S atoms to optimize their interaction with WS₂ and with the lower H₂ layer. The distance between the two planes formed by the centres of mass of the H₂ molecules in the two layers is 2.52 Å. The average adsorption energy for the two adsorbed layers is 0.058 eV per molecule. It is only a bit smaller than the physisorption energy per molecule of 0.064 eV for one adsorbed H₂ monolayer with the molecules in the perpendicular orientation (see Table 2). In spite of the upper hydrogen layer being more distant from WS₂, the similarity of the adsorption energies can be understood as a result of the attractive van der Waals interactions between the two adsorbed layers. The calculated energy for desorbing the top H₂ layer is 0.052 eV per molecule, which is not too different from the desorption energy value of 0.064 eV per molecule when only a single layer is adsorbed.

5. Adsorption of Atomic Hydrogen

The adsorption of a single H atom on the surface of layered WS₂ materials produces a chemisorption state. Figure 5 shows the most stable configuration of H on a single WS₂ layer, chemisorbed on top of an S atom with the S—H bond perpendicular to the layer. The distance between the H and S atoms is 1.43 Å, and the chemisorption energy

$$E_{chem}(H) = E(clean) + E(H) - E(H@WS₂)$$  \hspace{1cm} (2)

is 1.37 eV. In this equation, $E(H)$ represents the energy of an isolated H atom, and $E(H@WS₂)$ is the energy of the system with adsorbed H. This chemisorption energy really corresponds to coverage $x = 0.0625$ ML, that is, one H atom per unit cell. By comparison with molecular adsorption discussed above, the bond distance is much shorter, and the bond strength is much higher.

In contrast to the H₂ physisorption on WS₂ nanotubes, where no correlation was observed between the adsorption energies and the nanotube diameters, the H chemisorption energies exhibit such a correlation. On the nanotubes, the H chemisorption configuration is the same as for planar layers. We have calculated the chemisorption energies of H on the outer surface of all the studied single-wall nanotubes for the lowest coverage of 0.0625 ML. The chemisorption energy plotted in Figure 6 has a value of 1.39 eV for the nanotube with the largest diameter, the zig-zag (32,0) nanotube, and then increases linearly as the nanotube diameter decreases, reaching a value of 1.57 eV for the nanotube with the shortest diameter, the arm-chair (8,8). No difference is found between the arm-chair and zig-zag nanotubes. This behaviour reflects the enhanced reactivity of the S atoms as the surface curvature increases in the nanotubes. The H chemisorption energy on the (32,0) nanotube is already quite close to the chemisorption energy on the planar layer, 1.37 eV.

Recent experiments of plasma-hydrogenation of WS₂ materials did not reveal the existence of chemisorbed atomic hydrogen.26 This observation is now supported by the following calculations. The sum of the chemisorption energies of two separated H atoms is...
approximately 2.7 eV, a value substantially lower than the binding energy between the two H atoms in a free H₂ molecule, 4.52 eV. So, the process of dissociating the H₂ molecule and chemisorbing the two H atoms is energetically very unfavourable. Dissociating the H₂ molecule on the WS₂ surface costs slightly less, but the activation barrier is still high, as discussed next.

![Figure 5. Top and side pictorial views of the optimized structure of an H atom chemisorbed on top of an S atom of a single WS₂ layer. Blue, golden and white spheres represent W, S and H atoms, respectively.](image)

We have performed CI-NEB calculations to find the minimum energy paths for H₂ dissociation on the WS₂ single-layer, the bulk surface, and the (20,0)@(32,0) nanotube. This methodology provided results in good agreement with the experiments in other layered materials. The calculated barrier heights for H₂ dissociation range between 3.8 eV and 4.0 eV for the different starting (a)—(d) H₂ adsorption configurations. This range seems to have its origin in the initial orientation of the molecules and their on-surface location. Although these barriers are somewhat smaller than the dissociation energy of the free H₂ molecule, 4.52 eV, the large activation barriers indicate that H₂ dissociation leading to atomic H chemisorption is very unlikely to take place on the surface of WS₂ materials. Of course those barriers are no more relevant if chemisorbed H is produced in experiments already starting with atomic hydrogen. In fact, neutral H atoms and H⁺ cations are generated in a hydrogen plasma, in addition to molecular hydrogen, although in a concentration usually too small compared to that of H₂.

![Figure 6. Chemisorption energy per H atom (in eV) as a function of the nanotube diameter (in Å), in the low coverage regime 0.0625 ML, for single-wall nanotubes: arm-chair (8,8), (10,10), (12,12), (14,14), (16,16), and zig-zag (16,0), (20,0), (24,0), (28,0), (32,0) nanotubes. The result of the linear regression is also shown in the figure.](image)

### 6. Diffusion of H₂ and H on the Surface of WS₂ Layers

The diffusion of H₂ and H on the surface of a WS₂ layer has been investigated using the CI-NEB methodology. In the case of H₂, the diffusion event analysed is the jump from an initial state in which the molecule sits on its preferred position on top of a W atom to a similar final position on top of a neighbour W atom (see Figure 7). The CI-NEB method generates the path requiring the minimum energy. The calculations were performed for the two relevant initial orientations of the molecular axis, parallel and perpendicular to the WS₂ layer, but the orientation can change along the diffusion path. Figure 7 shows the initial and final configurations, as well as the configuration at the stage corresponding to the top of the barrier. The corresponding energies along the diffusion path are plotted on the left panels of this figure. The diffusion follows a path along the W—W bond, and the activation barriers are quite low: 0.025 eV in the case of a parallel molecule, and only 0.010 eV for the perpendicular molecule. Consequently, the H₂ molecules are expected to be quite mobile on the WS₂ surface at room temperature. These low activation barriers are not surprising because the H₂ molecule is physisorbed. For comparison, the calculated activation barrier for diffusion of H₂ on the surface of graphene is 0.010 eV. 46
Figure 7. (Right panel) Top and side views of the initial state, IS, transition state, TS (corresponding to the maximum of the activation barrier), and final state, FS, for the diffusion of H (top panels) and H$_2$ (middle and bottom panels) on the WS$_2$ surface. (Left panel) Computed CI-NEB energy barriers along the diffusion minimum energy diffusion paths (MEPs). Blue, golden, and white spheres represent W, S and H atoms, respectively.

On the other hand, as shown in Figure 7, the diffusion of an H atom between positions on top of neighbouring S atoms of the surface is quite different. The path is roughly the shortest path between the two S atoms, and the height of the activation barrier is 0.18 eV. Consequently, the mobility of H is much reduced compared to the mobility of H$_2$. In a previous work by some of us, hydrogenation of hollow WS$_2$ multiwall nanotubes was performed by exposing the material to a high-pressure (80 kbar) atmosphere of molecular hydrogen at temperatures of 35 °C, 200 °C and 350 °C; that is, near room temperature and above. The pressure-composition-temperature absorption isotherms indicated that the weight percent of absorbed hydrogen is 0.11-0.13%. Since physisorption is generally more efficient at low temperatures, we have performed a set of high pressure hydrogenations experiments in which WS$_2$ nanoparticles and multiwall nanotubes were kept at temperatures between -196 °C and -50 °C, and several isotherms were measured. The transmission electron microscopy (TEM) analysis revealed concentric semi-spherical WS$_2$ shells forming giant fullerene-like structures. The nanotubes were 50-150 nm wide and about 20 µm long, and the diameters of the spherical or semi-spherical nanoparticles were in the range of 50-250 nm. As can be observed in Figure 8, the isotherms measured at -196 °C show the increase of hydrogen concentration up to 0.16 wt. % for nanotubes, and up to 0.28 wt. % for nanoparticles. The highest hydrogen concentrations were obtained, however, at -78 °C: 0.29 wt. % for nanotubes and 0.36 wt. % for nanoparticles.

The increase in the hydrogen concentration at low temperatures is substantial, up to three times compared to room temperature. And the fact that hydrogen concentration is higher at -78 °C than at -196 °C is remarkable. Our interpretation is that diffusion, which is generally favoured by higher temperatures, plays a significant role. Diffusion allows the H$_2$ molecules moving through the material to efficiently reach all the available adsorption sites. The thermal energies, $k_BT$, at -196 °C and -78 °C are 0.007 eV/molecule and 0.017 eV/molecule, respectively, and the activation barrier for diffusion of H$_2$ molecules in the perpendicular configuration is 0.010 eV, smaller than $k_BT$ at -78 °C. This rough estimation indicates that diffusion becomes more efficient at $T = -78 °C$ than at -196 °C, explaining the result of larger hydrogen concentration at -78 °C.

Interestingly, the following trend was observed in the high-pressure hydrogenation of multiwall nanotubes measured in the previous work: the amount of hydrogen adsorbed at 200 °C and 350 °C is smaller than at 35 °C. The explanation is that H$_2$ desorption competes with adsorption, and is responsible for the lowering of the amount of adsorbed hydrogen observed at 200 °C and 350 °C. Desorption of H$_2$ from the surface of WS$_2$ has an energy cost of 0.06—0.07 eV (see Table 2), and the values of $k_BT$ at 35 °C, 200 °C and 350 °C are 0.027 eV, 0.041 eV and 0.054 eV, respectively; thus, desorption will deplete the amount of adsorbed hydrogen at the two highest temperatures considered.
7. Intercalation of Hydrogen in Multilayers and Multiwall Nanotubes

The calculations presented above reveal that H₂ can be adsorbed on the surface of WS₂ multilayers and nanoparticles, or in the outermost or innermost walls of WS₂ nanotubes. To investigate the possibility of intercalation of H₂ between WS₂ layers we have performed calculations by intercalating the trilayer with increasing amounts of H₂. For this purpose, H₂ molecules were placed between the first and the second layers of the trilayer, and the system was allowed to fully relax to reach its lowest energy structure. Four hydrogen concentrations were explored, namely \( x = 0.0625 \) ML, 0.25 ML, 0.5 ML and 1 ML. As a specific example, we consider the case of the lowest hydrogen concentration, \( x = 0.0625 \) ML. The simulations started by placing the intercalated molecules (one per cell) in an initial position which is below a W atom of the upper WS₂ layer and above a S atom of the middle layer, with the molecular axis perpendicular to the layers. This is precisely the configuration called (b) above when viewed with reference to the upper layer of the trilayer. During the structural relaxation, the molecule evolved by moving to a position above a neighbour W atom of the intermediate layer, and changing the orientation of the molecular axis, which ends up oriented parallel to the layers (see Figure 9). At the same time, the separation between the WS₂ layers increased until reaching 6.21 Å, which is the optimal separation to adjust the intercalated molecules. The orientation now obtained for the molecule is different from its orientation when the molecule is adsorbed on a free WS₂ surface, that is, when the molecule is not confined. The reason is that intercalation with the parallel orientation forces a smaller widening of the spatial gap between the two confining layers as compared to the perpendicular orientation.

Based on this observation, the simulations of the intercalation with higher amounts of hydrogen started with the H₂ molecules initially placed on top of W atoms of the middle layer, with the molecular axis parallel to the layers. The main change occurring during structural optimization was the readjustment of the distances between the WS₂ layers. Figure 9 shows the final configurations for intercalation with 0.25 ML, 0.5 ML and 1 ML of H₂. Table 4 reveals that the distance between the first and the second layer increases substantially as the amount of intercalated hydrogen increases. Another observation is that the final orientation of the intercalated molecules at 1 ML of H₂ is intermediate between parallel and perpendicular. The expanded separation between the two WS₂ layers is responsible for this orientation.

The intercalation energy per hydrogen molecule can be defined by the following expression:

\[
E_{\text{int}}^{\text{mol}}(x\text{ML}) = \frac{E(\text{trilayer}) + nE(H_2) - E(x\text{ML})}{n},
\]

where \( E(x\text{ML}) \) is the energy of the unit cell of a trilayer intercalated with a fraction \( x \) of a monolayer of H₂, \( E(\text{trilayer}) \) is the energy of the corresponding unit cell of the clean trilayer, and \( nE(H_2) \) is the energy of \( n \) isolated gas molecules, where \( n \) corresponds to the number of hydrogen molecules in the unit cell for the intercalate fraction \( x \). The intercalation energy, given in Table 4, is negative in all cases; that is, intercalation is unfavourable. However, a noticeable lowering of the magnitude of the intercalation energy per molecule is observed as \( x \) increases, which is due to two factors.

Figure 8. Hydrogen absorption isotherms measured at -196 °C in: (left) giant fullerenic-like WS₂ nanoparticles, and (right) multi-walled WS₂ nanotubes.

Figure 9. Optimal structures for intercalation of molecular hydrogen between the first and the second layers of the WS₂ trilayer for different H₂ content (0.0625 ML, 0.25 ML, 0.5 ML and 1 ML).

\( E_{\text{int}}^{\text{mol}}(x\text{ML}) = \)
The first factor can be understood from the column labelled $E_{\text{exp}}$ in Table 4. The intercalation of $H_2$ produces a widening of the interlayer distance. Then we define the expansion energy as the energy per unit cell that would be required to increase the distance between the first and the second layers of a clean (non-intercalated) trilayer. To be consistent with the sign convention chosen for the adsorption and intercalation energies, we assign the negative sign to the expansion energy cost. The magnitude of the expansion energy becomes larger as the distance between WS$_2$ layers increases. However $E_{\text{exp}}$ varies in a special way. The expansion energy for the widening of the interlayer distance from 6.13 Å to 6.21 Å (distances corresponding to intercalation with 0 ML and 0.0625 ML, respectively) is large. It amounts to -1.50 eV per unit cell, with an expansion energy rate of -1.50/0.07 = -21.4 eV/Å. Next, for the interlayer widening from 6.21 Å to 7.51 Å as a result of increasing the amount of intercalated $H_2$ from 0.0625 ML to 0.25 ML, the expansion energy rate drops to the value -2.26/1.3 = -1.74 eV/Å. The lowering tendency of the expansion energy rate continues for the interlayer widening from 7.51 Å to 8.17 Å, yielding a value -1.0 eV/Å. In the last step, an expansion energy rate of -0.72 eV/Å is found for the interlayer widening from 8.17 Å to 8.61 Å.

The second factor responsible for the lowering of the magnitude of the intercalation energy per molecule is simply the increasing value of $n$ in the denominator on the right-hand side of eq. (3). The difference between the intercalation and expansion energies is the binding energy, $E_b$, listed in the last column of Table 4. This is negative for low coverage, because the layer expansion is still small (the distance between the $W$ planes of the two adjacent layers is 6.21 Å) and the intercalated molecules sample the repulsive part of the molecule-W$_2$ potential. Then, as the amount of intercalated $H_2$ increases, the binding energy turns positive since the large interlayer expansion allows the $H_2$ molecules sampling the attractive part of the molecule-W$_2$ potential. At this limit, higher binding energies are obtained compared to adsorption on a free WS$_2$ surface due to the molecule interaction with the two confining layers.

It can be noticed from previous sections that the distance between chemisorbed $H$ atoms and the surface of a WS$_2$ layer (1.43 Å) is about one half of the distance between physisorbed $H_2$ molecules on WS$_2$ (2.83-2.98 Å). Consequently, one might suggest that dissociation of the intercalated $H_2$ molecules could be favourable because the interlayer expansion will be less for intercalated atomic hydrogen. For our purposes the most convenient definition of the intercalation energy of $H$ atoms is the following:

$$E_{\text{int}}(x\text{ML}) = \frac{\{E(\text{trilayer})+nE(H)-E(x\text{ML})\}}{n} \quad (4)$$

In this equation, $E(\text{trilayer})$ is the energy of the unit cell of a clean WS$_2$ trilayer, $E(x\text{ML})$ is the energy of the unit cell of the trilayer intercalated with a fraction $x$ of a monolayer of $H$ atoms, $E(H)$ is the energy of a free $H$ atom, and $n$ is the number of hydrogen atoms in the unit cell for the intercalate fraction $x$. In contrast to intercalation of molecular hydrogen, intercalation of atomic hydrogen leads to positive intercalation energies (see Table 5); that is, the intercalated systems are energetically stable with respect to the clean trilayer and free $H$ atoms.

The intercalated $H$ atoms become attached to $S$ atoms, reproducing the behaviour already seen in Figure 5. All the $H$ atoms in Figure 10 are attached to $S$ atoms of the upper basal plane of the middle WS$_2$ layer, but binding energies and distances do not change when part of the $H$ atoms are attached to $S$ atoms of the upper WS$_2$ layer. Intercalation increases slightly the distance between adjacent WS$_2$ layers, and this effect is enhanced by increasing the amount of intercalated $H$. However, by comparing Tables 4 and 5, it is worth noticing that the forced separation between WS$_2$ layers induced by intercalation of atomic hydrogen is quite small in comparison to intercalation of $H_2$. The reason for this is that the $H$ atom is small and its binding to $S$ is strong, so it can be easily accommodated between the adjacent WS$_2$ layers. This also justifies that the intercalation energies per atom in Table 5 are close to the chemisorption energies (1.37 eV) of $H$ atoms on the surface of a single WS$_2$ layer. However, the experimental Raman measurements did not detect $H-S$ bonds (see below). We conclude that the amount of atomic hydrogen on the surface of WS$_2$ materials, or intercalated between layers is non-significant, or perhaps there was not enough atomic $H$ in the RF plasma.
Figure 10. Optimal structures for the intercalation of atomic hydrogen between the first and the second layers of the WS$_2$ trilayer for different H content (0.25 ML, 0.5 ML, 0.75 ML and 1ML). The H atoms are attached to S atoms belonging to the upper basal plane of the second WS$_2$ layer. Blue, golden and white spheres represent W, S and H atoms, respectively.

The intercalation energies in Table 5 are positive. This is because the reference in eq. (4) is formed by the free H atoms. To compare these intercalation energies with the intercalation energies of H$_2$ molecules given in Table 4, both should be measured with respect to the same reference and this is the system of free molecules. First, the number of H atoms intercalated in the cell should be the same in the two cases, so if the coverage of molecular hydrogen is $x$, the comparable coverage of atomic hydrogen should be $2x$. In this way we can compare the configurations of 4 molecules per cell ($x$(H$_2$) = 0.25 ML) and 8 atoms per cell ($x$(H) = 0.5 ML), and also the configurations of 8 molecules per cell ($x$(H$_2$) = 0.50 ML) and 16 atoms per cell ($x$(H) = 1 ML). On the other hand, the dissociation energy of the H$_2$ molecule into two H atoms has to be added (with negative sign) to the atomic intercalation energies. In this way, the energy to intercalate 4 molecules in the cell is $-1.01 \text{ eV} \times 4 = -4.04 \text{ eV}$, or $-1.01 \text{ eV}$ per molecule, and the energy to dissociate 4 free molecules and intercalate those 8 atoms in the cell is $-4.52 \text{ eV} \times 4 + (1.32 \text{ eV}) \times 8 = -7.75 \text{ eV}$, or $-1.88 \text{ eV}$ per molecule. A similar calculation gives $-0.48 \text{ eV/molecule}$ for the energy necessary to intercalate 8 molecules in the cell, and $-0.88 \text{ eV/molecule}$ for the energy to dissociate 8 molecules and intercalate the 16 atoms in the cell (notice that a negative sign indicates an endothermic process). In conclusion, atomic intercalation is unfavourable with respect to molecular intercalation if one accounts for the energy required to dissociate the H$_2$ molecules.

An interesting new effect occurs when H$_2$ is intercalated in multiwall WS$_2$ nanotubes. The conclusions arise from simulations of the intercalation of H$_2$ into the double wall nanotubes (10,10)@(16,16) and (20,0)@(32,0). Widening the separation between the two walls of the nanotube induced by intercalation of H$_2$ would result in a change of the radii of the concentric tubes, at least an increase of the radius of the external tube, and perhaps also a decrease of the radius in the inner tube. Those radii changes modify the interatomic distances in each tube, and produce substantial elastic stresses. The energy cost of such processes is much larger than the energy cost to separate two planar WS$_2$ layers. Another possibility would be a drastic local change of the structure of the tubes around the intercalated molecules, but this is also energetically costly and quite unfavourable. The alternative and more efficient route chosen by the system, and observed in the simulations, is that the intercalated H$_2$ molecules spontaneously dissociate and the H atoms form bonds with S atoms, preferentially with S atoms of the inner tube, as shown in Figure 11. Eight rows of molecules have been intercalated, each row parallel to the axis of the nanotube, and the positions of the rows have been chosen in such a way as to maintain substantial distances between adjacent rows. Different views of the starting configuration are shown in panels a), b) and c) of Figure 11. Panel e) shows the final configuration, with the hydrogen molecules dissociated and the H...
atoms bonded to S atoms, and panel d) represents an intermediate state in the scission path. The radii of the two concentric nanotubes did not change in the dissociation process. The behaviour of H$_2$ intercalated in multiwall nanotubes is qualitatively different from that observed for intercalation on planar multilayers. The difference arises from the geometry of the multiwall nanotubes, in which an expansion of the tube-tube distance produces an internal distortion of the rigid structure on each nanotube. In comparison, the expansion of the interlayer distance in planar multilayers is easier because the interlayer expansion does not affect the rigid internal structure of the layers. This argument, which explains the results of the simulations, is based on the assumption that the concentration of H$_2$ molecules intercalated between planar WS$_2$ layers is enough to produce the expansion of the interlayer distance. It is clear that this is the case for the concentrations investigated in this work, in particular for the lowest one, x = 0.0625 ML. However, this behaviour can change for diluted H$_2$ concentrations. As an extrapolation we predict that dissociation of H$_2$ intercalated between planar WS$_2$ multilayers will occur for very low concentration of H$_2$, much lower than those investigated here. Verifying this prediction is computationally hard because it needs enlarging the unit cell to sizes much larger than the sizes considered here.

To complete the previous analysis we have studied the diffusion mechanism of an H atom intercalated in a (10,10)@(16,16) nanotube. In the starting configuration, the H atom is chemisorbed on an S atom of the inner (10,10) nanotube (low coverage regime 0.0625 ML). Using the CI-NEB method we have investigated two different minimum energy paths (MEP). Path (a) corresponds to the unconstrained MEP from the initial configuration towards a final one with the H atom chemisorbed on the closest S atom of the inner nanotube. Path (b) is a constrained MEP with the same initial and final states as in (a) but this time imposing an intermediate step with the H atom chemisorbed on the closest S atom of the outer (16,16) nanotube. The activation energy barrier for path (a) is 0.23 eV. For path (b), we have found a first barrier of 0.32 eV separating the initial chemisorbed state from the intermediate (constrained) state, and a second barrier of nearly identical height separating the intermediate state from the final chemisorbed state. Consequently, route a) is more favourable. The diffusion barriers of H atoms intercalated into the MEPs are a bit higher than in the case of diffusion on the surface of a planar layer (0.18 eV). We interpret this feature as an effect of confinement, which hinders the activation of the normal modes associated with the S—H stretching allowing detaching the chemisorbed H atom, and makes diffusion more difficult. This is why diffusion of atomic hydrogen, either on the surface or intercalated into layers of WS$_2$, will be difficult at room temperature.

Earlier in this Section (see Table 4) it was noticed that intercalation of 0.0625 ML of H$_2$ in a WS$_2$ trilayer expands the interlayer distance from 6.13 Å to a value of 6.21 Å, with an associated energy cost required for this expansion. A remarkable observation from Section 4 is that adsorption of a full H$_2$ monolayer on top of a WS$_2$ trilayer induces an increase in the distance between the topmost and the second WS$_2$ layers, from 6.13 Å to 6.21 Å (or from 6.14 Å to 6.23 Å in the case of the WS$_2$ bulk surface). The consequence is that intercalating 0.0625 ML of H$_2$ in a trilayer with its surface fully covered by H$_2$ will not pay the penalty of the expansion energy. This opens a new door to the intercalation process worth to be explored in the future. That is, the presence of adsorbates on the top layer may facilitate the intercalation of species between the layers.

8. Theoretical Raman Spectroscopy

In a previous work we reported a series of micro-Raman spectra of WS$_2$ nanoparticles (NPs): a) non-hydrogenated NPs, b) RF plasma hydrogenated NPs, and c) RF plasma hydrogenated NPs vacuum annealed up to 450 °C. The three spectra correspond to the black-solid lines in Figure 12. The aim of these experiments was to confirm that H$_2$ molecules had been adsorbed on the NPs. A prominent peak centred at ~4150 cm$^{-1}$ was observed for the hydrogenated samples only and attributed to the H—H stretching mode in H$_2$ molecules. This was confirmed by heating the hydrogenated samples in vacuum up to 450 °C. The intensity of the H$_2$ peak gradually decreased until vanishing after annealing (see Figure 12).

![Figure 12. Black-solid lines are micro-Raman spectra of WS$_2$ nanoparticles: (a) non-hydrogenated, (b) plasma hydrogenated, (c) plasma hydrogenated and vacuum annealed up to 450 °C. A vertical line indicates the location of the H$_2$ peak at 4150 cm$^{-1}$. The Blue-solid line is the theoretical non-resonant Raman peak for 1 ML of H$_2$ molecules physisorbed on a planar WS$_2$ layer. A mismatch smaller than 70 cm$^{-1}$ is found between experiment and theory.](image-url)

Motivated by those experiments, and in order to reinforce the validity of our structural hydrogenation model, we have calculated the non-resonant Raman spectrum for the optimized configuration of 1 ML H$_2$ molecules physisorbed on a single planar WS$_2$ layer. For this purpose we have used an approach based on second order
response. Specifically, the second order derivative of the electronic density matrix with respect to a uniform electric field has to be computed. This is done within the context of DFT\textsuperscript{50} implemented in the QUANTUM ESPRESSO code.\textsuperscript{28} In non-resonant Stokes Raman spectra of harmonic solids and surfaces, the peak intensities can be obtained within the Placzek approximation.\textsuperscript{51} This procedure yields the effective charges and dielectric tensor, the Raman tensor and the dynamical matrix, which finally permits the calculation of the Raman cross sections by applying Acoustic Sum Rules. In the calculations we force both translational and rotational modes to zero frequency. This approach proved to yield results in excellent agreement with experiment.\textsuperscript{52}

In Figure 12 the computed non-resonant Raman spectrum (blue-solid line) exhibits a unique and very pronounced peak centred at 4216 cm\textsuperscript{-1} (compared to the experimental peak at 4150 cm\textsuperscript{-1}). The excellent agreement confirms that the experimental peak is associated to the stretching mode of the physisorbed hydrogen molecules. The small mismatch, smaller than 70 cm\textsuperscript{-1}, can be due to two factors. The first one concerns the approximations introduced by the theoretical method. The second one is the deviation in the real samples from the 1 ML monolayer H\textsubscript{2} coverage assumed in the calculations. In fact, the assumption of a full H\textsubscript{2} monolayer adsorbed could induce a slight shift in the spectrum, because the interaction between neighbour molecules may affect the stretching of the individual molecules. On the other hand, the fact that the substrate in the Raman calculations is a planar WS\textsubscript{2} layer is not expected to introduce errors because the nanoparticles in the experiment are quite large.

9. Summary and Conclusions

The interaction of hydrogen with planar WS\textsubscript{2} multilayers and single and double-wall nanotubes has been investigated using the density functional formalism with van der Waals corrections. H\textsubscript{2} molecules deposited on the surfaces of WS\textsubscript{2} multilayers and nanotubes are physisorbed preferentially on top of the W atoms, and the adsorption energies (0.06—0.07 eV/molecule) and distances depend weakly on the coverage. For coverages in excess of one monolayer, a second layer is formed with the H\textsubscript{2} molecules on top of S atoms. In contrast, atomic hydrogen forms chemisorption bonds (of strength 1.4—1.6 eV/atom) with the external S atoms. In the case of nanotubes there is an inverse correlation between the bond strength and the nanotube diameter because a decrease in the diameter enhances the curvature and then the chemical reactivity of the nanotubes. While the chemisorption state is favourable starting with free H\textsubscript{2} atoms, the chemisorption energy of two H\textsubscript{2} atoms does not compensate for the energy required to dissociate the H\textsubscript{2} molecule. This theoretical observation of energetically favourable intercalation of atomic H will allow to improve the outcome of hydrogen adsorption experiments. The concentration of atomic hydrogen in the RF plasma used in our previous studies was about 1.5 % and, therefore, resulted in low atomic H intercalation.\textsuperscript{10,26} We believe that using higher atomic H concentration in the plasma will improve H intercalation towards highly desired applications for renewable energy storage systems.

Diffusion of the H\textsubscript{2} molecule on the surface of WS\textsubscript{2} from one W atom to a neighbour W atom is easy, with small activation barriers between 0.010 eV and 0.025 eV, depending on the initial orientation of the molecular axis. The magnitude of these barriers serves to rationalize new experimental results for the observed dependence of hydrogen concentration with temperature. The activation barriers for the diffusion of individual H atoms are one order of magnitude larger. Intercalating H\textsubscript{2} molecules between adjacent planar WS\textsubscript{2} layers is an endothermic process, although the main energy cost occurs for low H\textsubscript{2} concentration, and the intercalation energy per H\textsubscript{2} molecule decreases as the concentration of intercalated molecules increases. Intercalation of free H atoms is energetically favourable, but again the intercalation energy does not compensate for the cost of dissociating the molecules. An interesting effect occurs when H\textsubscript{2} molecules are intercalated between the two walls of a double wall nanotube. In this case, the rigidity of the structure induces the dissociation of the confined molecules. Diffusion of individual intercalated atoms encounters barriers with a height similar to that for diffusion on an open surface. A remarkable result is that the presence of a full H\textsubscript{2} monolayer adsorbed on top of the first WS\textsubscript{2} layer of a multilayer strongly facilitates the intercalation of H\textsubscript{2} between WS\textsubscript{2} layers underneath. This opens up a new door to intercalation processes. Finally, the calculated Raman peak corresponding to the H-H stretching mode of H\textsubscript{2} molecules adsorbed on a planar WS\textsubscript{2} surface is in very good agreement with experiment.

Overall, the calculations presented here have clarified the different processes and mechanisms related to the interaction of hydrogen with WS\textsubscript{2} nanomaterials. In this way we provide a solid basis for the interpretation and further improvement of the experiments on adsorption and storage of hydrogen on these layered materials.

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Notes and References

**TOC.** First-principles calculations, supported by new experimental evidences, have been used to clarify the different processes and mechanisms related to the interaction of hydrogen with WS₂ nanomaterials.