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Highlights

- A novel curl-based rotation measurement built from tensorial magnitudes is proposed.
 - Proposed rotation descriptor makes no assumption about the cardiac topology.
 - Locally increased vorticity values are present in hypertrophied myocardial segments.
 - Extracted vortical features have proven useful in cardiomyopathy discrimination.
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Graphical Abstract

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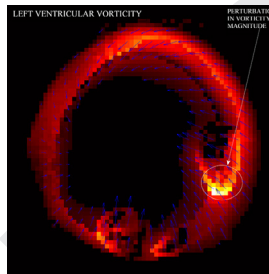
Vortical features for myocardial rotation assessment in hypertrophic cardiomyopathy using cardiac tagged magnetic resonance

Santiago Sanz-Estébanez^{a,*}, Lucilio Cordero-Grande^b, Teresa Sevilla^c,
Ana Revilla-Orodea^c, Rodrigo de Luis-García^a, Marcos Martín-Fernández^a,
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ABSTRACT

Left ventricular rotational motion is a feature of normal and diseased cardiac function. However, classical torsion and twist measures rely on the definition of a rotational axis which may not exist. This paper reviews global and local rotation descriptors of myocardial motion and introduces new curl-based (vortical) features built from tensorial magnitudes, intended to provide better comprehension about fibrotic tissue characteristics mechanical properties. Fifty-six cardiomyopathy patients and twenty-two healthy volunteers have been studied using tagged magnetic resonance by means of harmonic phase analysis. Rotation descriptors are built, with no assumption about a regular geometrical model, from different approaches. The extracted vortical features have been tested by means of a sequential cardiomyopathy classification procedure; they have proven useful for the regional characterization of the left ventricular function by showing great separability not only between pathologic and healthy patients but also, and specifically, between heterogeneous phenotypes within cardiomyopathies.

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1. Introduction

Hypertrophic cardiomyopathy (HCM) (Maron et al., 2014) is a relatively common heart muscle disease with a heterogeneous phenotypic expression that occasionally overlaps with other pathologies that also present left ventricular hypertrophy. Differentiating the underlying etiology of the ventricular hypertrophy is a frequent clinical problem with relevant implications since each etiology needs a specific management and presents a different prognosis. HCM is characterized by a hypertrophied and nondilated left ventricle (LV) (Baron, 2008), often with an asymmetrical wall thickness distribution. HCM occurs in the presence of myocyte hypertrophy and interstitial and replacement fibrosis, which cause the walls of the ventricles to thicken (Maron et al., 1992) and a reduction on the cavity volume is usually observed. This thickening

may block blood flow out of the ventricle. Therefore, the main features of a HCM heart summarize in increased LV mass and thickened walls, especially in the interventricular septum (Urbano-Moral et al., 2014). These abnormalities lead to altered forces revealing a significant reduction in the diagonal components of the strain (Saltijeral et al., 2010). Previous studies have shown that regional LV dysfunctions predate over the morphologic changes related with the phenotypic expression of hypertrophy and obstruction (Dhillon et al., 2014).

As previously stated, etiological factors are of great importance in the cardiovascular disease detection (Maron et al., 2006). Global indices, such as the global longitudinal strain (Shimon et al., 2000), have been employed for cardiovascular disease identification, reporting noticeable prognostic value; however, local measurements could provide more insight to the behavior of fibrotic tissue (Piella et al., 2010). In this direction, it has been hypothesized that the presence of greater myocardial twist may be associated with a greater degree of myocardial fibrosis in HCM patients. Consequently, assessment of LV rotation mechanics as a characteristic of cardiac function may help differentiate the presence of fibrosis (Young and Cowan, 2012). Consistently with these studies, we adhere to the appropriateness of local analyses and their clinical

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cal value on the basis that most heart diseases typically affect localized regions of the myocardium. In addition, local studies can be used to improve cardiac analytics, which may help predict the effects of specific cardiovascular diseases on the tissue.

Rotation parameters have recently gained increasing attention due to their simplicity and ease of quantification; they constitute interesting measures of cardiac performance which provide additional information on myocardial mechanics as a complement of standard pump function indices (Rüssel et al., 2009a). However, most of the rotation parameters described in the literature implicitly require an accurate description of an axis of rotation. The center of mass given by myocardial boundaries is widely used as such; however, the heart can translate during the cardiac cycle, which commonly results in misalignments of the center along subsequent frames, incurring in estimation errors. Hence, non-biased calculation methods, which compensate centroid motion, are mandatory for the use of LV torsion as a measure of myocardial dysfunction quantification (Sengupta et al., 2008). Still, additional drawbacks have been reported; Young et al. (1994) state that, for HCM, the axis of rotation is shifted from the LV center of mass towards the inferoseptal region. In addition, for HCM patients, due to their characteristic asymmetrical wall thickness distribution, accurate centroid estimation could become an extremely challenging task.

Imaging techniques provide essential information for the study of these pathologies; several modalities have been proposed in an effort to measure advanced cardiac mechanics in the LV: speckle tracking echocardiography (Helle-Valle et al., 2005; Bansala and Kasliwalb, 2013), Cine Displacement Encoded (DENSE) Magnetic Resonance Imaging (MRI) (Zhong et al., 2010) or traditional cine Steady State Free Precession (SSFP) MRI, combined with feature tracking techniques (Heermann et al., 2014), to mention a few. Nevertheless, myocardial tissue tagging with cardiovascular magnetic resonance is currently the gold standard for assessing regional myocardial function (Shehata et al., 2009). If it is not widely used in the daily practice is because it is time consuming, but to date is an accurate method to measure regional contractility (Jeung et al., 2012). MR-Tagging (Ibrahim, 2011) is usually performed by spatial magnetization modulation (SPAMM) (Axel and Dougherty, 1989) or a variant of this technique. SPAMM is grounded on the ability of altering the magnetization of the tissue (within the limitations of relaxation times in MR) even in the presence of motion. The tagging procedure is based on the superposition of a spatial modulation over the applied gradients which may be subsequently tracked throughout the cardiac cycle, from which the cardiac function can be assessed.

Harmonic Phase (HARP) based methods (Osman et al., 2000) are widely used as a motion estimation technique in MR-Tagging (MR-T). These methods are capable of reconstructing displacement fields accurately, grounded on the assumption of constant local phase, which turns out to be more reliable than the constant pixel brightness assumption. This approach is based on the use of SPAMM tag patterns, which modulate the underlying image, producing a set of spectral peaks in the Fourier domain. Each of these spectral peaks carry information about a particular component of tissue motion, and this information can be extracted using phase demodulation methods, obtaining tensorial descriptors of deformation and, for our case, rotation estimations.

Curl is a differential operator that describes the infinitesimal rotation of a vector field. Its direction determines the axis of rotation while its magnitude shows the amount of rotation. The term vortex is commonly associated to a localized increased value on the magnitude of the given curl vector (this property will be hereafter referred to as vorticity). The local rotation measured by the curl operator should not be confused with the bulk angular veloc-

Table 1Demographic data of the pathologic and healthy patients in the study (mean \pm std).

Patients	HCM	SLVH	Healthy Vol.
Number of cases	39	17	22
Age	58 \pm 16.3	69.8 \pm 10.5	49.2 \pm 21.8
Sex (M/F)	27/12	12/5	14/8
Ejection Fraction (%)	70.4 \pm 5.4	69.7 \pm 6.1	63.6 \pm 6.5
Diastolic LV volume (ml)	140.6 \pm 22.8	131 \pm 50.3	150.3 \pm 31.5
Systolic LV volume (ml)	42 \pm 9	41.8 \pm 22.4	53.8 \pm 13.9
Wall thickening (%)	78.4 \pm 20.1	79.8 \pm 18.6	89.6 \pm 16.9

ity vector observed within the myocardial tissue with respect to a fixed cardiac axis.

Numerous 4D phase-contrast MRI (Köhler et al., 2013) studies have made use of the curl operator. Flow vortical patterns in the heart chambers, the aorta, the carotid sinus and pulmonary circulation are physiological, but can also be related to certain pathologies including aortic aneurysms, pulmonary hypertension and congenital heart defects. Vortical patterns often occur because of morphological alterations, vessel widenings or after stenosis (von Spiczak et al., 2015). These structures may alter the pressure and shear forces on the walls and trigger processes leading to cell death.

It is our understanding that curl can also quantify the local rotation within the muscle. Consequently, in this paper we introduce a novel local rotation descriptor based on robust tensorial measurements that relates the presence of increased vorticity values with the hypertrophic tissue in the heart. Rotation is estimated without influence of global myocardial parameters, such as axis of rotation or cavity radius, allowing a regional comparative study in patients with LV hypertrophy of different etiologies; HCM and Secondary forms of LV Hypertrophy (SLVH), as well as healthy subjects. To the best of our knowledge, this is the first study that relates local vortices in myocardial tissue with the presence of fibrosis.

2. Materials and methods

2.1. Materials

For the validation of the proposed approach, our study is a retrospective analysis based on a database of patients who underwent the ordinary clinical protocol according to their symptoms; the database consisted in 78 individuals who were affected by either primary HCM or SLVH (hypertensive heart disease, aortic stenosis or athlete heart disease) or were healthy volunteers. The number of pathologic patients was 56; 39 of them, with ages from 30 to 86, were diagnosed as primary HCM. These patients showed hypertrophy, predominantly in the septal region of the LV. Following the same protocol, 17 patients were diagnosed of SLVH according to chronic pressure overload. The differential diagnosis between primary HCM and SLVH was based on previous echocardiographic studies and clinical and familial records. About the healthy volunteers, 22 were included in the study with ages between 16 and 84; these subjects underwent the MRI protocol because of a previous suspicion of cardiac pathology but all of them turned out to be healthy.

All subjects signed the ordinary informed consent for the MR session and agreed in writing to share the resulting images for research purposes. Personal data were treated according to current legislation. Demographic data of both controls and cases, the latter indexed by pathology type, are given in Table 1.

We have acquired short axis (SA) and long axis (LA) MR-T datasets for each patient, from apex to base, using a MR Complementary SPAMM (C-SPAMM) SENSitivity Encoding (SENSE) Turbo

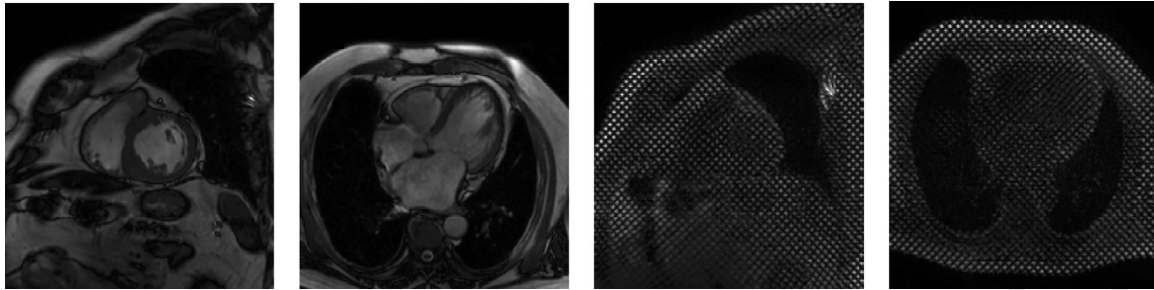


Fig. 1. Example images of the sequences acquired for the study. MR-Cine SA, MR-Cine LA, MR-Tagging SA and MR-Tagging LA, from left to right.

Table 2

Details on the sequences of MR images used in the paper. Δ_p : Reconstructed Pixel Resolution (mm). Δ_s : Slice Thickness (mm). N_p : Number of pixels for dimension. N_t : Number of Temporal Phases. N_s : Number of slices. T_R : Repetition Time (ms). T_E : Echo Time (ms). α : Flip Angle (degrees).

Parameters	Δ_p	Δ_s	N_p	N_t	N_s	T_R	T_E	α
MR-T SA	1.21-1.32	10	256-432	16-25	10-15	2.798-6.154	1.046-3.575	7-25
MR-C SA	0.96-1.18	8-10	240-320	30	10-15	2.902-3.918	1.454-2.222	45
MR-T LA	1.21-1.34	10	240-340	15-27	1-3	2.903-4.507	1.097-2.897	10-45
MR-C LA	0.98-1.25	8-10	256-448	30	1-3	2.858-3.529	1.251-2.132	45

Field Echo sequence on a Philips Achieva 3T scanner. Regarding the tagging parameters, we validate the method for a fixed tag spacing of $k_i = 1/\lambda$, with $\lambda = 7$ mm using two different orientations $\mathbf{U}_i = (\cos(\theta_i); \sin(\theta_i))$ with $\theta = [\pi/4; 3\pi/4]$ for the stripe directions.

Additionally, we have also acquired a balanced SSFP SA MR-Cine (MR-C) sequence at the same spatial location for each patient; snapshots of the acquired sequences are shown in Fig. 1. The myocardium has been segmented in the end-diastolic (ED) phase of the MR-C sequence by two cardiologists. Cine segmentations are used to align the tagging orientations to a common reference system to correct for patient motion. The ED segmentation is used to define a region of interest (ROI) in which to compute meaningful measurements. Resolution details about these sequences are included in Table 2.

2.2. Methods

2.2.1. Preprocessing

We have implemented a preprocessing pipeline in order to (a) propagate the ROI in MR-C from ED to the end-systolic (ES) phase—in which subsequent calculations will be carried out—and (b) align the MR-C and MR-T sequences at ES. These two steps are:

- **Registration** The MR-C sequence is processed by means of a groupwise elastic registration procedure (Cordero-Grande et al., 2013a) in order to propagate the ED segmentations towards ES phase. The transformation is achieved by B-spline based Free Form Deformations (FFD) (Rueckert et al., 2006). A gradient-descent optimization scheme is performed where the sum of the squared differences of image intensities is used as registration metric. A smoothness penalty term has also been introduced to constrain the spline-based FFD transformation to be smooth.
- **Alignment** An affine registration method is performed to align MR-T and MR-C images at ES phase. The MR-T sequence has been detagged by means of a homomorphic filtering procedure (Makram et al., 2015) prior to the alignment process.

2.2.2. Motion estimation

3D HARP motion reconstruction using the C-SPAMM technique requires a minimum of 3 linearly independent wave vectors (Osman et al., 2000). We have extended the aforementioned

HARP methodology for the computation of the deformation gradient tensor using SA and LA images on the intersection of the slices as shown in Fig. 2. For points on which LA axis images were not available, 2D motion has been reconstructed. The motion estimation technique is based on the extraction of the local phase of the grid pattern according to the method presented in Cordero-Grande et al. (2011, 2016). A windowed Fourier Transform (WFT) is applied to the image at ES phase. The WFT provides a representation of the image spectrum in the surroundings of each pixel of the original image, so HARP band pass filtering techniques can be directly applied on the spatially localized spectrum of the image. To adequately retrieve the shape of the spectral peaks, we have resorted to an anisotropic filtering approach combining Gaussian band-pass and all-pass filters as proposed in Sanz-Estébanez et al. (2016a). Finally, each of the image phase $\varphi_i(\mathbf{x})$ (two for each plane) can be extracted in the spatial domain from the inverse WFT of the aforementioned filtered spectrum.

As mentioned before, we have extended the HARP methodology by allowing the estimation of motion under the application of a set of four wave vectors. Therefore, 3D deformation gradient tensor can be robustly recovered at the intersection points of both axes, by applying the methodology presented in Cordero-Grande et al. (2016). The material deformation gradient tensor $\mathbf{F}(\mathbf{x})$ can be estimated from the gradient of the phase image as stated in Osman et al. (2000) as:

$$\mathbf{K} = \frac{\partial \varphi}{\partial \mathbf{x}}(\mathbf{x})\mathbf{F}(\mathbf{x}) = \mathbf{Y}(\mathbf{x})\mathbf{F}(\mathbf{x}), \quad (1)$$

where \mathbf{K} represents the two stripe orientations of four given wave vectors corresponding to each tagged image. Robust estimation of $\mathbf{F}(\mathbf{x})$ is achieved through Least Absolute Deviation (LAD) procedure. The reconstruction is performed via Iteratively Reweighted Least Squares (IRLS):

$$\mathbf{F}_{l+1}(\mathbf{x}) = (\mathbf{Y}^T(\mathbf{x})\mathbf{W}_l(\mathbf{x})\mathbf{Y}(\mathbf{x}))^{-1}\mathbf{Y}^T(\mathbf{x})\mathbf{W}_l(\mathbf{x})\mathbf{K}, \quad (2)$$

with $\mathbf{W}_l(\mathbf{x})$ a diagonal weighting matrix, which is updated at each iteration by considering fitting residuals (Cordero-Grande et al., 2016).

From this estimated tensor, the main cardiac function characteristics can be obtained through the Lagrangian strain tensor, defined as:

$$\mathbf{E}(\mathbf{x}) = \frac{1}{2}(\mathbf{F}(\mathbf{x})^T\mathbf{F}(\mathbf{x}) - \mathbf{I}). \quad (3)$$

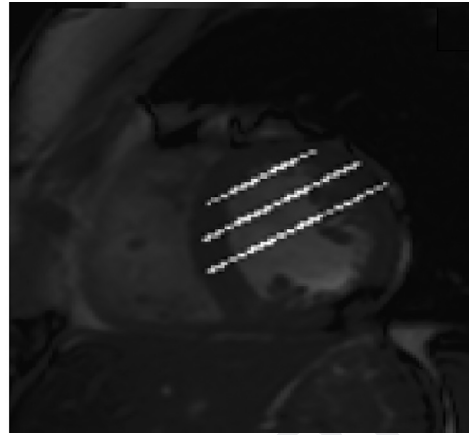
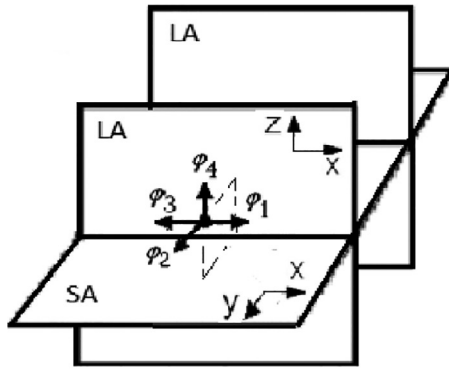


Fig. 2. The figure on the left sketches the proposed 3D HARP motion reconstruction scheme for the intersected points between SA and LA planes, which are shown in the figure on the right over the SA.

228 The spatial resolution of the reconstructed tensors depends on
 229 the width of the HARP band pass filter (Parthasarathy and Prince,
 230 2003; 2004); the HARP method is upper limited by half of the tag
 231 spacing (small deformation assumption). However, WHARP meth-
 232 ods (Sanz-Estébanez et al., 2016a; Cordero-Grande et al., 2016) try
 233 to accommodate the band pass filter to the local frequency of the
 234 signal in order to approach to the maximum achievable resolution.
 235 Therefore, effective HARP resolution will vary dynamically, allow-
 236 ing large deformations, as those observed at ES, being captured at
 237 a maximal scale of 1.5 times half the tag spacing.

238 These tensors have been calculated at ES, where the greatest
 239 deformation along the cardiac cycle takes place.

240 2.2.3. Rotation parameters

241 In addition to thickening and shortening, the myocardium also
 242 undergoes a wringing motion during systolic phases due to the
 243 obliquely oriented subendocardial and subepicardial myofibers.
 244 Many descriptors have been proposed to measure this motion that
 245 rely on either global information derived from simplified anatomical
 246 models or on tensorial strain and deformation magnitudes built
 247 from local motion estimates.

248 *Measures based on global information.* It is well known that the
 249 LV apex globally rotates anticlockwise at a relatively constant rate
 250 throughout systole. On the contrary, the base, initially rotating an-
 251 ticlockwise, reverses direction providing a net clockwise rotation
 252 at ES phase. The resulting difference of these two motions is de-
 253 fined as twist, defined to be positive by convention (Young and
 254 Cowan, 2012).

255 There is currently a lack of standardization for methods used to
 256 characterize the global LV twisting motion. These descriptors rely
 257 on geometrical models of the heart for torsion and twist calcula-
 258 tion. Consequently, both a well-defined fixed axis of rotation and
 259 regular myocardial radii over the whole heart are mandatory. For
 260 example, torsion has been traditionally calculated as relative ro-
 261 tation in degrees (Lorenz et al., 2000), rotation per length in de-
 262 grees/mm, torsional shear angle, also in degrees (Buchalter et al.,
 263 1990), and longitudinal-circumferential shear strain (dimension-
 264 less) (Fung, 1965). Traditional rotation indices are obtained by vec-
 265 torial product between position vectors at ES $\mathbf{u}_{ES}^{\vec{}}$ and ED $\mathbf{u}_{ED}^{\vec{}}$
 266 phases as:

$$267 \sin(\beta) = \frac{|\mathbf{u}_{ED}^{\vec{}} \times \mathbf{u}_{ES}^{\vec{}}|}{|\mathbf{u}_{ED}^{\vec{}}||\mathbf{u}_{ES}^{\vec{}}|}. \quad (4)$$

268 As stated above, twist computation depends on the exact loca-
 tions of the apical and basal slices and requires accurate motion

compensation, specially for centroid motion correction. Twist per
 unit length is also widespread, since torsion is relatively constant
 in the longitudinal direction (Young and Cowan, 2012). Nonethe-
 less, this measure does not scale appropriately between hearts of
 different sizes and we have not observed a significant complemen-
 tary value with respect to the twist.

275 The torsional shear angle is a measure of the change in angle
 276 between line segments which are initially aligned with the
 277 anatomical axes of the LV. Many studies have used the formula
 278 given by Aelen et al. (1997). However, it has been demonstrated
 279 that it usually overestimates deformation (Rüssel et al., 2009b), so
 280 we have resorted to an unbiased alternative formula based on circum-
 281 ferential displacements:

$$282 T = \frac{(\beta_{apex} r_{apex} - \beta_{base} r_{base})}{D}, \quad (5)$$

283 where D is the distance between selected segments.¹ However,
 284 HCM characteristic endocardial irregularities may hinder the accu-
 285 rate estimation of both the myocardial radius and the axis, which
 are crucial in this formulation.

286 *Tensorial descriptors.* Another important group of rotation descrip-
 287 tors focus on the properties of the tissue that provide localized
 288 characterization of the motion by tensorial analysis. As stated in
 289 solid mechanics (Fung, 1965), the 3D strain state at any point in a
 290 body can be fully represented by three diagonal strains and three
 291 shear strains. From them, the longitudinal-circumferential shear
 292 (E_{lc}) is a useful measure closely related to torsion. According to this
 293 analysis, local torsion measures can be defined, i.e., the 3D local
 294 torsion shear can be given by:

$$295 \sin(\theta_{lc}) = \frac{2E_{lc}}{\sqrt{1 + 2E_{cc}\sqrt{1 + 2E_{ll}}}}, \quad (6)$$

296 where E_{cc} and E_{ll} represent the circumferential and longitudi-
 297 nal strains, respectively; these components can be obtained by
 298 straightforward operations on the Cartesian components in (3).
 299 Nevertheless, shear strains are several magnitudes lower than di-
 300 agonal strains, so factors other than inotropic state may greatly af-
 301 fect its estimation (Petitjean et al., 2005).

302 Angular variation between two states of stress in the plane
 in Cartesian coordinates can be expressed by a single angle ϕ as

¹ Rotation parameter β has been pixelwise estimated; therefore, rotation mea-
 sures expressed on (5) are referred to the median of the rotation distribution on
 basal and apical segments.

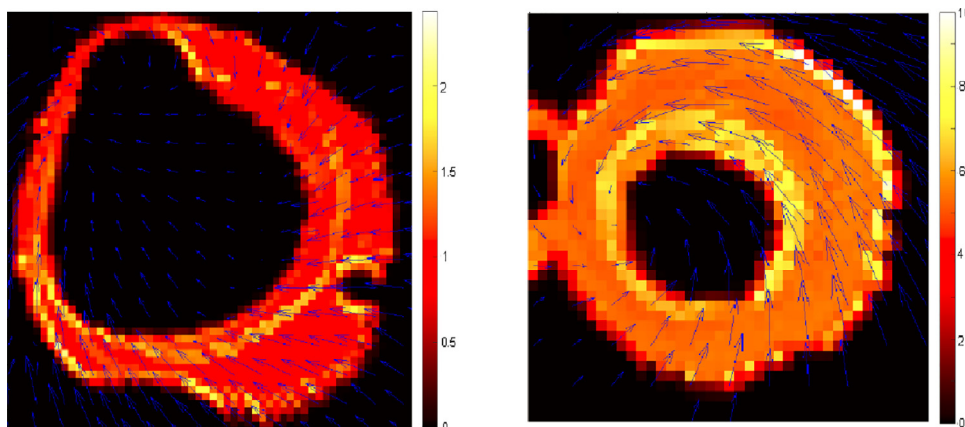


Fig. 3. Examples of vorticity vector modulus at ES from (9) in basal and apical slices, left and right respectively. The arrows show the extracted cardiac displacement field while the colour represents the intensity of vorticity (unitless). Some outliers are observed near the boundaries due to the difficulty of HARP methods in tracking material points in the presence of great intensity changes. Scales are set to best accommodate the range of values on the given cardiac plane, since myocardial rotation varies in modulus and direction along the cardiac axis.

303 stated in Fung (1965):

$$304 \quad \tan(2\phi) = \frac{2\varepsilon_{xy}}{\varepsilon_{xx} - \varepsilon_{yy}}, \quad (7)$$

305 where ε represents the Cauchy's strain tensor ($\boldsymbol{\varepsilon}$) directly related
306 with the stress tensor by the Lamé parameters (Fung, 1965). Partic-
307 ular values of ϕ show angular variation of stress principal direc-
308 tions between both states (ES and ED phases).

309 Additionally, in Cordero-Grande et al. (2013b) a novel rotation
310 parameter has been proposed built from the (longitudinal) trans-
311 formation that suffers a local coordinate at ED through time in the
312 LR plane as given by the material deformation gradient tensor \mathbf{F} .

$$313 \quad \alpha^{LR} = \arctan(-F_{lr}/F_{ll}). \quad (8)$$

314 Our work elaborates on vortical patterns widely employed for
315 the identification of abnormal flow patterns. Nonetheless, the term
316 vortex bears different interpretations as defined in the literature.
317 For most flow studies performed in clinical practice, the term vor-
318 tex denotes rotating motion, where stream or pathlines tend to
319 curl back on themselves (Markl et al., 2011). In fluid dynamics, a
320 vortex is a region in a fluid in which the flow is rotating around an
321 axis line, which may be straight or curved. More explanatory notes
322 on the theoretical definition of the term vortex can be found in
323 Stalder et al. (2010). In this paper, the term vortex will be used in
324 the solid mechanics context as a local abnormally increased rota-
325 tion component. In order to find evidence of perturbations within
326 the myocardial tissue, material vortical patterns can then be asso-
327 ciated to increased values of a dynamic rotation parameter ex-
328 tracted from the deformation gradient tensor.

The curl of a given deformation field \mathbf{u} describes local spinning
vectors (see Fig. 3) and can be calculated as:

$$329 \quad \bar{\boldsymbol{\omega}}(t) = \begin{pmatrix} \omega_x(t) \\ \omega_y(t) \\ \omega_z(t) \end{pmatrix} = \frac{1}{2} \nabla \times \mathbf{u}(t) = \frac{1}{2} \begin{pmatrix} \frac{\partial u_z}{\partial y} - \frac{\partial u_y}{\partial z} \\ \frac{\partial u_x}{\partial z} - \frac{\partial u_z}{\partial x} \\ \frac{\partial u_y}{\partial x} - \frac{\partial u_x}{\partial y} \end{pmatrix} \quad (9)$$

$$= \frac{1}{2} \begin{pmatrix} F_{zy} - F_{yz} \\ F_{xz} - F_{zx} \\ F_{yx} - F_{xy} \end{pmatrix}$$

330 where F_{ab} represents a component of the material deformation
331 gradient tensor in Cartesian coordinates. Hereinafter, vortical pa-
332 rameters will be expressed in Cartesian coordinates as opposed to
the cylindrical coordinates from the strain tensor used in (6).

333 In this paper we hypothesize that local increasing of vortic-
334 ity values (in modulus) arises within myocardial segments with
335 fibrosis-related perturbations. Nonetheless, high vorticity values, ir-
336 respective of the fibrosis degree, are prone to appear in myocardial
337 boundaries, giving rise to multiple outliers in rotation estimation.

338 These vorticity measures are insensitive to the definition of the
339 rotation axis, although 3D deformations are needed for its proper
340 reconstruction. When LA information is not available, only the lon-
341 gitudinal component (ω_z) of the vorticity vector can be estimated.
342 In addition, if the cardiac axis is not planned properly, vorticity
343 parameters will be estimated with a systematic error related to
344 the angular error of the axis. However, as it is common in clinical
345 practice, we will assume that the main axis of rotation will lie on
346 the LA planes (i.e., will be normal to the SA image planes). Hence,
347 the ω_z component of the vorticity vector provides clinical compli-
348 ance as it is aligned with the wringing motion of myocardial fibers.
349 Thus, a phase increment due to the aforementioned local rotation
350 can be extracted by integration:

$$351 \quad \int_{t_{ED}}^{t_{ES}} \omega_z(t) dt = \vartheta(t_{ES}) - \vartheta(t_{ED}) = \vartheta(t_{ES}) \approx \frac{\omega_z(t_{ES})}{2} (t_{ES} - t_{ED}). \quad (10)$$

352 This parameter will be referred to as local rotation ϑ . Therefore,
353 twist motion will be approximated as

$$354 \quad \text{Twist } \vartheta = |\vartheta_{\text{base}} - \vartheta_{\text{apex}}| \quad (11)$$

355 For comparative purposes, we will also estimate ϑ and β rota-
356 tion distributions with two other different methodologies. First, we
357 will analyse the capabilities of the elastic registration algorithm de-
358 scribed in Section 2.2.1 applied to MR-C to detect rotation from the
359 estimated deformation fields. Second, we have employed an atlas-
360 based approach that consists of a spheroidal model (Young and
361 Axel, 1992) fitted at ED and that deforms due to the forces ex-
362 erted from a stripe tracking procedure (Young et al., 1995) on the
363 MR-T sequence throughout the cardiac cycle. Deformations are for-
364 mulated from continuous parameter functions which, in addition,
365 include parameterized twisting and rotation axis deformation as
given in Park et al. (1996) and, therefore, can be applied to any
shape.

2.2.4. Classification

366 We have resorted to a classification method (Sanz-
367 Estébanez et al., 2016b) to assess the discriminating ability
368 of the rotation features previously described. The procedure,
369 sketched in Fig. 4, consists in an automated processing pipeline
370

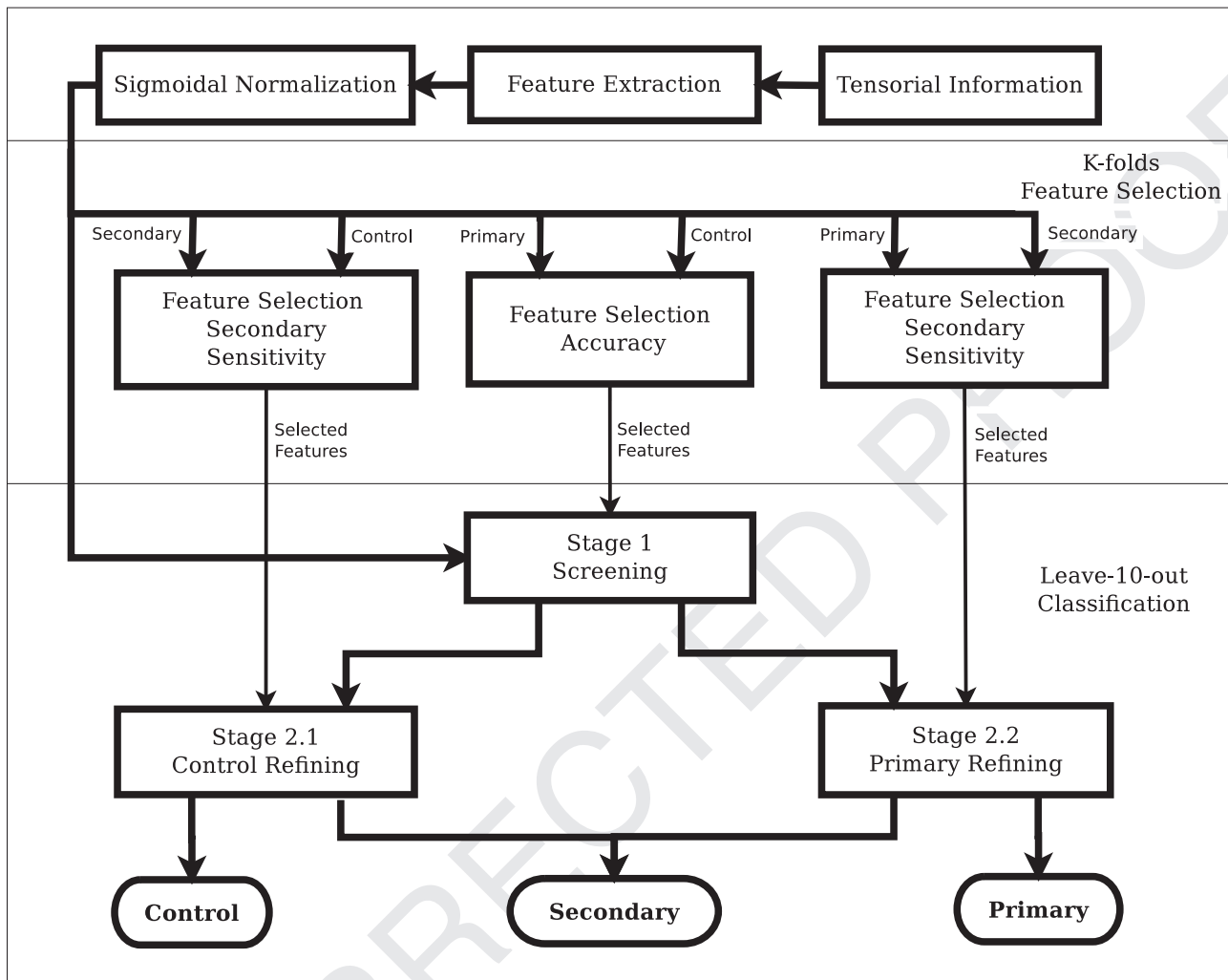


Fig. 4. Pipeline for the feature selection and classification stages.

371 to classify heterogeneous groups of ventricular hypertrophy (and
 372 controls) from myocardial functional descriptors. The proposed
 373 classification method is grounded on the idea that populations
 374 overlap strongly irrespective of the specific features selected for
 375 classification if the problem is addressed through a single stage.
 376 Our purpose is to classify a sample into one of three classes,
 377 namely, control, primary HCM and secondary hypertrophy (SLVH).
 378 Since secondary hypertrophy patients have subtle differences with
 379 respect to the other two classes, we have resorted to a two-stage
 380 classification procedure. Thus, we have divided the classification
 381 process in three stages and performed a feature selection step
 382 for each stage independently, following a sequential methodol-
 383 ogy that adapts to the characteristics of the population at every
 384 stage. Different machine learning methods (both supervised and
 385 unsupervised) have been implemented for each stage and all their
 386 possible combinations have been tested.

387 Mechanical descriptors extracted from the aforementioned ten-
 388 sors are an essential part of the classification procedure. We have
 389 considered different groups of features. First, the components of
 390 the strain tensor in the cylindrical coordinate system $\{R, C, L\}$
 391 are accounted for. We also use twist and torsion features (see
 392 Table 3) built from the aforementioned rotation parameters as
 393 extracted from the MR-T and MR-C sequences, as well as using
 394 the spheroidal model we have previously referred to. Additionally,
 395 since some rotation-related components have opposite directions

396 in apex and base, we consider the location of the zero crossing for
 397 these components as well.

398 For the feature extraction step, we have previously selected
 399 for each feature the most representative cardiac segments
 400 (Cerqueira, 2002) within clinical practice. For twist and torsion de-
 401 scriptors, we have considered septal segments, whereas for tensor-
 402 ial parameters, mid-ventricular or basal segments have been cho-
 403 sen. In Table 3 we show the segments involved in the calculation
 404 of each of the features; then the overall feature is, for robustness
 405 purposes, the median of the distribution within those segments,
 406 which will be the input to the classifier. For the twist param-
 407 eters the feature extracted is the difference between medians on
 408 apical and basal septal segments. On the other hand, for the zero
 409 crossing parameter, the feature represents the height of the cardiac
 410 axis at which the given rotation parameter, estimated slice by slice,
 411 changes its sign. Notice that the feature extraction step is grounded
 412 on clinical knowledge, i.e., it is not data-driven.

413 As reflected in Fig. 4, after feature extraction we carry out a
 414 normalization stage in order to diminish the influence of possible
 415 outliers. A sigmoidal function, with its scale factor set according
 416 to Theodoridis and Koutroumbas (1999), is used to this end. Data
 417 are mapped on the interval $(0,1)$ by imposing a generalized logistic
 418 function; outliers will tend to appear at either of the two extremes,
 419 while maintaining a linear relation for the rest of the data. Then,
 420 normalized features are arranged in vectors with different number

Table 3

Cardiac segments involved during the feature extraction stage for each one of the motion descriptors employed in the classification procedure. For each row, only one feature will be extracted, summarizing all the segments indicated below. The extracted features will be the input to the feature selection step, from which the final (survivor) feature vector (from 2 to 5 components) will arise. The number within braces indicates the equation that defines the parameter.

Segment	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
E_{rr} (3)							✓	✓	✓	✓	✓	✓					
E_{cc} (3)							✓	✓	✓	✓	✓	✓					
E_{ll} (3)	✓	✓	✓	✓	✓	✓											
E_{lc} (3)							✓	✓	✓	✓	✓	✓					
$\ \omega\ $ (9)	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓					
Twist ϑ (11)		✓	✓											✓			
Twist β (4)		✓	✓											✓			
Twist ϕ (7)		✓	✓											✓			
T (5)	✓	✓	✓	✓	✓	✓							✓		✓		✓
α^{LRI} (8)								✓	✓					✓			
θ_{lc} (6)		✓	✓					✓	✓					✓			
ω_z zero cross. (9)	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓
β zero cross. (4)	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓

421 of components (2 through 5). All possible combinations of features
422 indicated in Table 3 have been tested.

423 Feature selection and classification performance assessment has
424 been carried out in a similar but sequential manner. For both, data
425 samples have been randomized and a *Leave-10-out* method has
426 been applied; the proportions of control/primary/secondary have
427 been kept unaltered along trials. Specifically, for feature selection
428 in the first classification stage, we classify the samples in controls
429 and primaries and calculate the accuracy; the feature set with the
430 highest figure is selected for this stage. In parallel, and for the sec-
431 ond stage, controls and secondaries are classified on one branch
432 (left branch) and primaries and secondaries on the other branch.
433 In this case, features are selected with the criterion of maximiz-
434 ing the sensitivity to secondaries so as to avoid bias towards the
435 groups with larger sample size, specially between HCM and SLVH.
436 This procedure has been labelled in Fig. 4 as *K-fold Feature Selec-*
437 *tion*. As for finding classification performance, a similar cross vali-
438 dation procedure has been carried out (labelled in Fig. 4 as *Leave-*
439 *10-out Classification*) on new randomizations. The classifiers tested
440 have been Fuzzy c-Means (FCM) (Bezdec, 1981) and Support Vector
441 Machines (Cortes and Vapnik, 1995) both with quadratic (SVMq)
442 and Gaussian (SVMg) kernels (Vert et al., 2004).

443 In order to assess the performance of a given feature in the
444 classification procedure we have measured its surviving percent
445 rate. This parameter shows the membership probability of the
446 given feature to the feature vector extracted from the feature se-
447 lection step; in other words, it is the frequency that the feature is
448 employed within any of the stages of the classification along trials.

449 3. Results

450 3.1. Rotation analysis

451 Torsion is known to be dependent on LV shape, with reduced
452 twist in more spherically shaped hearts and increased torsion with
453 concentric hypertrophy due to an increased lever arm for myocar-
454 dial fibers. In HCM, torsion has been reported to increase despite
455 reduced circumferential and longitudinal shortening (Young and
456 Cowan, 2012). These findings, together with others described in
457 Section 1, can be observed in the results included in Table 4, where
458 the mean and standard deviation of the twist and torsion dis-
459 tributions derived from the aforementioned rotation features are
460 shown.

461 In Fig. 5 we show snapshots of mid-ventricular slices of the
462 local rotation extracted by means of the vortical approach as de-
463 scribed in (10) for a HCM and a SLVH case as well as for a healthy
464 volunteer. In general, septal segments for HCM have shown higher
465 vorticity, specially when compared to lateral segments, whereas for

Table 4

Twist and torsion parameters extracted from the MR-T sequence (mean \pm std) for segments in Table 3 for each population. The number within braces indicates the equation that defines the parameter.

Populations	HCM	SLVH	Control
Twist ϑ (11)	10.46 \pm 2.11	9.23 \pm 2.28	7.33 \pm 2.08
Twist β (4)	13.53 \pm 2.50	13.80 \pm 3.37	9.87 \pm 2.81
Twist ϕ (7)	2.73 \pm 0.53	2.71 \pm 0.64	1.25 \pm 0.072
T (5)	7.26 \pm 1.14	6.85 \pm 1.90	4.63 \pm 1.68
E_{lc} (3)	0.02 \pm 0.003	0.022 \pm 0.01	0.011 \pm 0.006
θ_{lc} (6)	7.94 \pm 1.66	7.22 \pm 1.81	3.18 \pm 0.39
α^{LRI} (8)	1.83 \pm 1.57	2.08 \pm 1.98	2.82 \pm 1.79

466 secondary cases this behavior can be observed in any of the car-
467 diac segments. In healthy volunteers the extracted values are lower
468 compared to HCM patients independently of the cardiac segment.

469 In Fig. 6, we show color codes of the mean \pm standard
470 deviation (respectively, inner and outer rings within each seg-
471 ment) of the rotation parameters over the 17-segment model
472 (Cerqueira, 2002), estimated from both the vortical approach given
473 in (10) and the traditional approach by (4) for the resulting dis-
474 tribution of the deformation vector field. Additionally, and for the
475 sake of comparison, rotation parameters extracted with the elastic
476 registration procedure over MR-C and from the deformable model
477 have been included as well in the second and third rows, respec-
478 tively.

479 Student t-tests² have been performed to highlight differences
480 on the mean of the vorticity modulus and the aforementioned ro-
481 tation distributions on each of the 17 cardiac segments. Each pop-
482 ulation of the study has been compared with the other two, sepa-
483 rately for each rotation parameter; the numerical results are shown
484 in Table 5 and graphically in Fig. 7 bull's eye display. It is notice-
485 able that the vortical approach seems to show larger differences
486 between populations compared to the traditional approach. Sep-
487 tal segments seem to bear higher discriminating capability, spe-
488 cially when twist is measured by the vortical approach. Addition-
489 ally, we have performed (two-way) ANOVA tests over the ϑ distri-
490 butions extracted from MR-C and MR-T sequences as well as using
491 the deformable model (over MR-T) for each population and car-
492 diac segment. Significant differences ($p < 10^{-3}$) have been found
493 in the vast majority of the comparisons. ϑ and β distributions were
494 not compared since the measured parameters do not represent the
495 same component of the physiological rotation motion.

² Similar conclusions have been obtained when performing Mann-Whitney U-Tests over these same distributions.

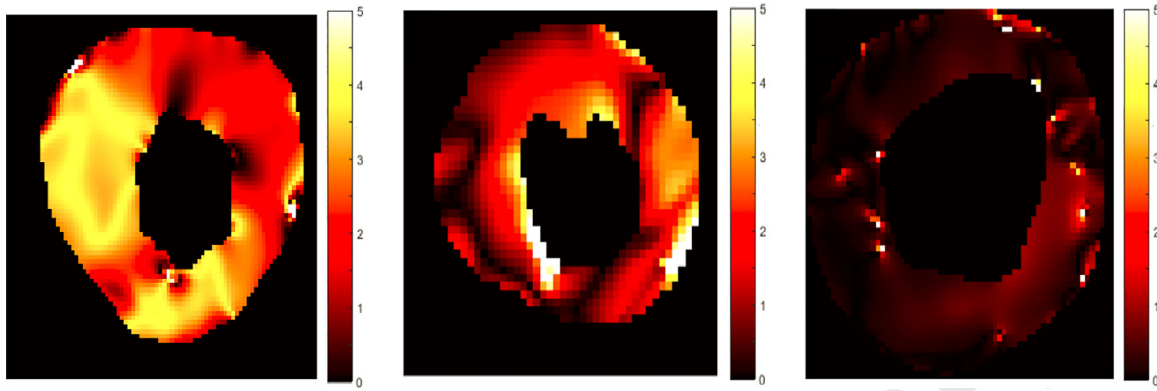


Fig. 5. Snapshots on vortical-based rotation measurement ω_z from (9) for HCM, SLVH and a healthy volunteer over mid-ventricular slices (from left to right).

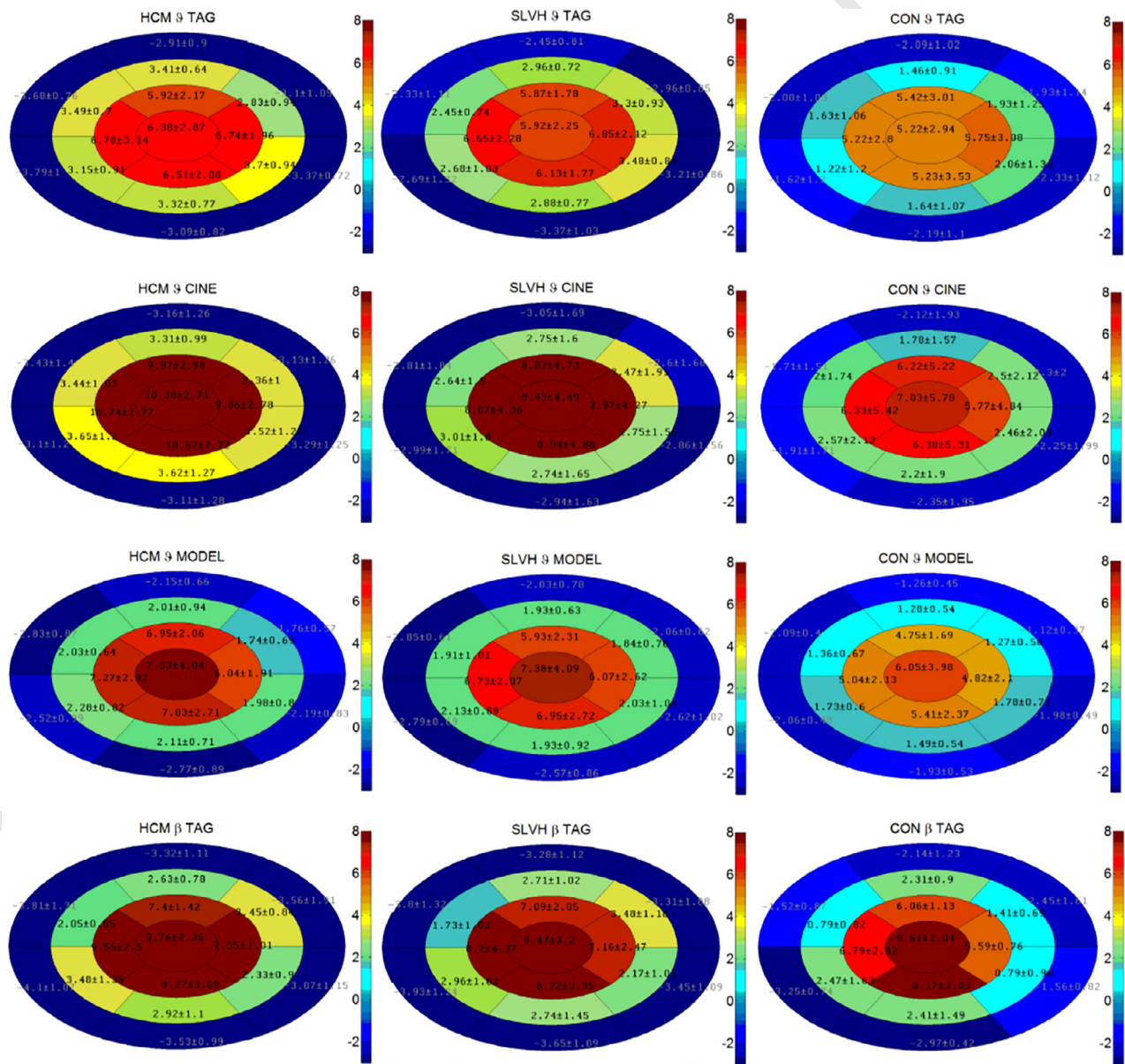


Fig. 6. Regional study of the aforementioned vortical rotation parameters obtained from the MR-C and MR-T sequences, as well as using the deformable model over the latter, for the different populations. Traditional rotation is also depicted in the last row. For each cardiac segment two colors are depicted, the inner showing mean \pm std and the outer for mean = std.

Table 5

p-values for the comparisons between distributions (H, S and C stand for HCM, SLVH cases and controls, respectively) of the given rotation parameters indexed by number of segment. When unspecified, MR-T is the image source. Significance level after Bonferroni correction is 0.017.

Seg.	Differences on ϑ distributions			Differences on β distributions			Differences on ϑ CINE distributions			Differences on ϑ MODEL distributions		
	H. vs S.	C. vs S.	H. vs C.	H. vs S.	C. vs S.	H. vs C.	H. vs S.	C. vs S.	H. vs C.	H. vs S.	C. vs S.	H. vs C.
1	0.078	0.001	$\leq 10^{-6}$	0.91	0.01	0.001	0.20	0.008	$\leq 10^{-6}$	0.19	0.033	$\leq 10^{-6}$
2	0.022	$\leq 10^{-6}$	$\leq 10^{-6}$	0.97	$2.49 \cdot 10^{-6}$	$\leq 10^{-6}$	0.47	$\leq 10^{-6}$	$\leq 10^{-6}$	0.12	$\leq 10^{-6}$	$\leq 10^{-6}$
3	0.065	$\leq 10^{-6}$	$\leq 10^{-6}$	0.65	$5.82 \cdot 10^{-5}$	$\leq 10^{-6}$	0.10	0.002	$\leq 10^{-6}$	0.24	$\leq 10^{-6}$	$\leq 10^{-6}$
4	0.33	$\leq 10^{-6}$	$\leq 10^{-6}$	0.71	$1.77 \cdot 10^{-6}$	$\leq 10^{-6}$	0.66	$\leq 10^{-6}$	$\leq 10^{-6}$	0.093	$8.23 \cdot 10^{-5}$	$\leq 10^{-6}$
5	0.52	$\leq 10^{-6}$	$\leq 10^{-6}$	0.31	$5.48 \cdot 10^{-6}$	$\leq 10^{-6}$	0.090	0.002	$\leq 10^{-6}$	0.073	$6.88 \cdot 10^{-5}$	$\leq 10^{-6}$
6	0.092	$\leq 10^{-6}$	$\leq 10^{-6}$	0.23	$8.04 \cdot 10^{-5}$	$3.05 \cdot 10^{-5}$	0.057	$1.17 \cdot 10^{-4}$	$\leq 10^{-6}$	0.55	0.0095	$\leq 10^{-6}$
7	0.64	0.002	$3.12 \cdot 10^{-5}$	0.78	0.26	0.21	0.18	0.022	$3.29 \cdot 10^{-5}$	0.055	0.0037	$\leq 10^{-6}$
8	0.011	$7.32 \cdot 10^{-5}$	$\leq 10^{-6}$	0.16	0.008	$3.03 \cdot 10^{-6}$	0.042	0.098	$6.34 \cdot 10^{-5}$	0.038	0.002	$\leq 10^{-6}$
9	0.049	0.17	0.002	0.27	0.41	0.028	0.09	0.010	$4.29 \cdot 10^{-4}$	0.013	0.051	$6.81 \cdot 10^{-5}$
10	0.12	0.27	0.044	0.29	0.89	0.20	0.53	0.016	$3.52 \cdot 10^{-5}$	0.34	0.046	$2.25 \cdot 10^{-4}$
11	0.018	$6.88 \cdot 10^{-6}$	$\leq 10^{-6}$	0.58	$5.79 \cdot 10^{-4}$	$1.37 \cdot 10^{-6}$	0.25	0.037	$1.98 \cdot 10^{-5}$	0.091	0.047	0.12
12	0.006	$8.21 \cdot 10^{-6}$	$\leq 10^{-6}$	0.94	0.004	$6.94 \cdot 10^{-5}$	0.26	0.18	$1.34 \cdot 10^{-4}$	0.65	0.059	0.064
13	0.10	0.092	0.002	0.57	0.085	0.002	0.040	0.092	$2.69 \cdot 10^{-4}$	0.021	0.0068	$\leq 10^{-6}$
14	0.79	0.068	$5.38 \cdot 10^{-5}$	0.54	0.017	0.001	0.055	0.003	$\leq 10^{-6}$	0.032	0.0082	$\leq 10^{-6}$
15	0.18	0.061	0.003	0.56	0.58	0.24	0.018	0.019	$\leq 10^{-6}$	0.76	0.019	$2.16 \cdot 10^{-5}$
16	0.46	0.045	$\leq 10^{-6}$	0.25	0.019	0.001	0.18	0.38	0.018	0.083	0.025	$\leq 10^{-6}$
17	0.87	0.86	0.22	0.73	0.88	0.82	0.14	0.17	0.27	0.81	0.17	$3.76 \cdot 10^{-4}$

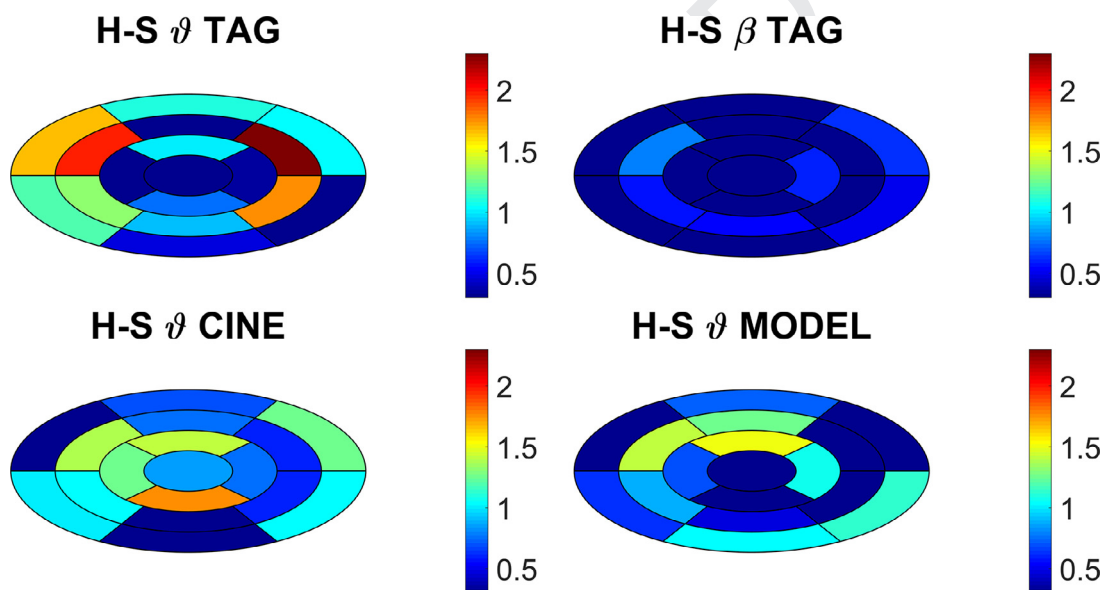


Fig. 7. *p*-value bull's-eye plots from intra-segment comparisons between primary HCM and SLVH patients for ϑ distributions obtained with different methodologies, as well as traditional rotation β distribution. Scale is defined as $-\log_{10}(p\text{-value})$.

496 3.2. Classification analysis

497 We have assessed the survival rate of the feature selection stage
 498 of the classifier (recall Fig. 4). Results are shown in Table 6 for
 499 the features described in Table 3; features obtained from both the
 500 MR-C elastic registration as well as from the spheroidal deformable
 501 model have also been included. Additionally, we have also included
 502 conventional indices of cardiac motion used in clinical practice,
 503 such as wall thickening (WT) over mid-ventricular slices (see Dong
 504 et al., 1994; Prasad et al., 2010 for more details), ejection fraction
 505 (EF) and LV volume, with the latter both at ED (EDLVV) and ES
 506 phases (ESLVV).

507 The most repeated configuration of the classifier consisted of
 508 FCM for stages 1 and 2.2 and SVMg for stage 2.1. The best accu-
 509 racy figures were obtained when using diagonal strain tensor
 510 components on stage 1, whereas for stages 2.1 and 2.2, the best
 511 feature vectors turned out to be $[E_{II}, \text{Twist}_{\vartheta\text{TAG}}, |\text{Twist}\phi|]$ and
 512 $[E_{II}, E_{CC}, \text{Twist}_{\vartheta\text{TAG}}, |\dot{\omega}|]$, respectively. If we take into account not
 513 only the best classifier but we also rank performance and analyze
 514 the first, say, ten results, the composition of the selected feature

vectors shows some degree of variability which seems very much
 515 in accordance with the results in Table 6.

516 In terms of end-to-end performance, the obtained accuracy
 517 (86%) seems comparable in classification figures with other proce-
 518 dures (see Gopalakrishnan et al., 2014; Puyol-Antón et al., 2017)
 519 although, in these cases, no SLVH are analyzed, so comparisons
 520 have to be made cautiously. In disaggregated terms, the sequential
 521 classifier has obtained sensitivity figures higher than 70% for each
 522 group (specifically, 81% for control, 72% for secondary hypertrophy
 523 patients and 95% for primary HCM patients). It is worth mention-
 524 ing that no primary is classified as control and viceversa; therefore,
 525 the pipeline proposed seems a proper screening tool. Secondary
 526 patients performance is clearly lower as compared with both con-
 527 trols and primary HCM patients, possibly due to a smaller sample
 528 size as well as the subtle differences they show.

529 Finally, in order to assess the relative strength of the differ-
 530 ent measures in classification performance, we have run the clas-
 531 sification pipeline with different features subsets. In particular, in
 532 Table 7 we have compared confusion matrices obtained with the
 533 full feature set (MR-T + MR-C + Deformable model + Conventional
 534

Table 6

Surviving percent rate of the features employed in the classification procedure (see notation in Fig. 4). Stage 2.2 is devised to SLVH-to-HCM sensitivity, while stage 2.1 refers to SLVH-to-Control sensitivity.

Features	Stage 2.2	Stage 2.1	Stage 1
E_{rr}	7	38	35
E_{cc}	54	24	60
E_{ll}	49	50	37
E_{lc}	22	11	6
$ \vec{\omega} $	43	25	19
Twist ϑ TAG	42	32	27
Twist ϑ CINE	7	2	13
Twist ϑ MODEL	15	8	7
Twist β TAG	19	16	16
Twist β CINE	8	5	4
Twist β MODEL	12	3	0
Twist ϕ	18	20	24
T	8	13	18
θ_{lc}	3	0	1
α^{LRI}	7	9	10
ω_z zero cross. TAG	21	13	4
ω_z zero cross. CINE	2	5	2
ω_z zero cross. MODEL	12	3	0
β zero cross. TAG	14	1	3
β zero cross. CINE	0	2	1
β zero cross. MODEL	3	1	0
WT	0	8	10
EF	0	6	3
EDLVV	0	0	1
ESLVV	0	2	0

clinical indices) and with MR-T features only. From the latter, we have also shown classification performance obtained discarding traditional and vortical rotation features, respectively.

4. Discussion

The relationship between myocardial fibrosis and local mechanics is important for the diagnosis and treatment of cardiomyopathies (Karamitsos and Neubauer, 2011). This paper shows that LV rotation is essential for proper myocardial function. In our case, most of the measurements shown in Table 4 indicate that LV rotation can be considered as a marker for cardiac disease identification and might be helpful for cardiomyopathy understanding, thus providing complementary information to standard pump function indices.

The diagonal components of the strain tensor (E_{cc} , E_{ll} and E_{rr}), defined in (3), have provided the highest separability between pathologic and healthy groups (cardiomyopathy screening) as shown in Table 6; our results are in accordance with this finding (Saltijeral et al., 2010). Twist parameters seem to be also valuable in this step, showing higher survival rate than shear strains and torsion parameters. For the refinement step for controls/SLVH (stage 2.1 in Fig. 4) the E_{cc} component in mid-ventricular areas is the most discriminative. Amongst the rotation-based parameters, vorticity modulus $||\vec{\omega}||$ and twist ϑ_{TAG} remain the most discriminative features.

In parallel, for the classifier stage 2.2, lower figures on the global performance are obtained. Besides, the selected feature vec-

tor presented one more component and two curl-derived entries; it consisted of a combination of two diagonal strain parameters, the vorticity modulus (9) and the twist extracted from the vortical approach (10). Extending the analysis to more (than one) high-ranked features vectors, we observe a greater degree of heterogeneity as well as the frequent presence of ω_z (9). Consequently, the proposed curl-derived parameters (9)–(11) have turned out to be particularly useful for the discrimination of primary and secondary cases as reflected by sensitivity figures extracted from Table 7.

To the best of our knowledge, this is the first study in HCM patients that relates vorticity in cardiac deformation fields with local myocardial mechanics and its abnormalities; our results suggest that vorticity may help deepen on the underlying characteristics behind primary and secondary cases of LV hypertrophy. For these parameters, neither the length nor the center of the heart are needed, so no bias is introduced in their estimation; as we have described above, vorticity is directly related to the deformation gradient tensor and, consequently, it can be estimated from the same information used in the strain tensor (3) analysis. In addition, they show higher survival rates than techniques that use fixed LV axis and center representations, giving rise to a more reliable parameter.

The color-coded results shown in Fig. 6 reveal that patients with both forms of ventricular hypertrophy present greater rotation distributions as compared with controls over most segments both for vortical (10) and traditional (4) rotations. As for primary HCM patients, there is a clear increased rotation (in modulus) for all segments, but high vorticity areas are mainly located on septal segments. SLVH patients showed a somewhat different pattern in mid-ventricular and basal regions of the heart, presenting higher values than controls; those values are not focused on septal segments but a slight bias to lateral segments may exist. Other regional analyses have also been performed by means of automatic LV segmentation (Bai et al., 2016; Liang et al., 2015). However, the presence of hypertrophic tissue and other pathologies may bias the final parcellation of the cardiac segments. For this reason, we have made use of the 17-segment model as a consistent and well-established model for motion analysis (Smiseth et al., 2016). The usefulness of the vortical parameters has also been reflected by the improvement shown in Table 7 with respect to traditional rotation parameters and the minor degradation with respect to the full-feature option when curl-derived parameters are used in isolation.

Our results also indicate a higher performance of MR-T for motion estimation with respect to MR-C; however, it is well-known that HARP procedures have some difficulties in correctly estimating the phase in the vicinity of boundaries. In those areas, elastic registration procedures over MR-C is usually more robust. For this reason, a coordinated procedure that weighs both information sources according to position may potentially provide better figures.

Additionally, vortical measures were compared when extracted both from the HARP method and by deforming a spheroidal model previously fit. Similar vorticity values were obtained although the extracted vortical patterns from the spheroidal model showed

Table 7

Confusion matrices for classification performance with different feature subsets. Matrices have been normalized with respect to the total number of patients. Each column represents the instances in a predicted class while rows represent the instances in an actual class.

	Full Feature Set			MR-Tagging only			Vortical only			Traditional only		
	C	S	H	C	S	H	C	S	H	C	S	H
C	0.236	0.064	0	0.243	0.057	0	0.24	0.06	0	0.234	0.066	0
S	0.023	0.145	0.032	0.038	0.144	0.018	0.021	0.141	0.038	0.038	0.127	0.035
H	0	0.017	0.483	0	0.025	0.475	0	0.022	0.478	0	0.023	0.477

616 higher spatial smoothness due to the regularized functions used
617 to define the deformation, thereby reducing its usefulness for clas-
618 sification (see Table 6).

619 Finally, conventional global indices in HCM diagnosis (see
620 Table 1) have also been tested in the classifier. Neither of them
621 presented a very representative survival rate (even in stage 1),
622 hence, their influence on final performance does not seem rele-
623 vant.

624 5. Conclusions and future lines

625 In this paper we have related anomalies on local vortical pat-
626 terns with the presence of fibrotic tissue by means of an im-
627 age processing pipeline and a two-stage sequential classification
628 method. Local rotation parameters are estimated by means of a ro-
629 bust motion and tensor analysis so that potential biases of global
630 analyses are avoided.

631 Local rotation was significantly increased in primary HCM pa-
632 tients, specially in the septum, compared to controls and secondary
633 cases; in the latter, vortical abnormalities may show a slight trend
634 to lateral segments and with values less pronounced than pri-
635 maries. These findings may provide important information in hy-
636 pertrophic diseases to establish a differential diagnostic between
637 these two classes.

638 Classification figures, although collateral in the paper, are
639 promising; clearly, discrimination between primary HCM and sec-
640 ondary cases is more challenging than between HCM and controls.
641 Therefore, figures related to the former problem have been lower
642 than those related to the latter. A larger cohort may let us increase
643 this number in the near future. Classification of SLVH cases has
644 proven to be a challenging task but figures, despite not being re-
645 markable, are likely to improve when equalizing the number of
646 subjects in the study or by introducing features that take into ac-
647 count the position of vortical peaks.

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