

Early-stage atherosclerosis detection using deep learning over carotid ultrasound images

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Abstract

This paper proposes a computer-aided diagnosis tool for the early detection of atherosclerosis. This pathology is responsible for major cardiovascular diseases, which are the main cause of death worldwide. Among preventive measures, the Intima-Media Thickness (IMT) of the common carotid artery stands out as early indicator of atherosclerosis and cardiovascular risk. In particular, IMT is evaluated by means of ultrasound scans. Usually, during the radiological examination, the specialist detects the optimal measurement area, identifies the layers of the arterial wall and manually marks pairs of points on the image to estimate the thickness of the artery. Therefore, this manual procedure entails subjectivity and variability in the IMT evaluation. Instead, this article suggests a fully automatic segmentation technique for ultrasound images of the common carotid artery. The proposed methodology is based on Machine Learning and artificial neural networks for the recognition of IMT intensity patterns in the images. For this purpose, a Deep Learning strategy has been developed to obtain abstract and efficient data representations by means of Auto-Encoders with multiple hidden layers. In particular, the considered deep architecture has been designed under the concept of Extreme Learning Machine (ELM). The correct identification of the arterial layers is achieved in a totally user-independent and repeatable manner, which not only improves the IMT measurement in daily clinical practice but also facilitates the clinical research. A database consisting of 67 ultrasound images has been used in the validation of the suggested system, in which the resulting automatic contours for each image have been compared with the average of four manual seg-

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mentations performed by two different observers (ground-truth). Specifically, the IMT measured by the proposed algorithm is 0.625 ± 0.167 mm (mean \pm standard deviation), whereas the corresponding ground-truth value is 0.619 ± 0.176 mm. Thus, our method shows a difference between automatic and manual measures of only 5.79 ± 34.42 μ m. Furthermore, different quantitative evaluations reported in this paper indicate that this procedure outperforms other methods presented in the literature.

Keywords: Deep learning, Auto-encoders, Extreme learning machine, Intima-media thickness, Image segmentation

1. Introduction

Cardiovascular diseases (CVD) remain the major cause of death in the world [1]. A large proportion of CVD are caused by an underlying pathological process known as atherosclerosis. Thus, its early diagnosis is critical for preventive purposes. Atherosclerosis involves a progressive thickening of the arterial walls by fat accumulation, which hinders blood flow and reduces the elasticity of the affected vessels.

The Intima-Media Thickness (IMT) of the Common Carotid Artery (CCA) is considered as an early and reliable indicator of atherosclerosis [2] and it is extracted from ultrasound scans [3], i.e. by means of a non-invasive technique. As can be seen in Fig. 1 (left), blood vessels present three different layers, from innermost to outermost: intima, media and adventitia. The IMT is defined as the distance from the lumen-intima interface (LII) to the media-adventitia interface (MAI). The use of different protocols and the variability between observers are recurrent problems in the IMT measurement procedure. To ensure the repeatability and reproducibility of the process, according to the Mannheim consensus [2], the IMT should be measured preferably on the far wall of the CCA within a region free of atherosclerotic lesions (plaques), where a double-line pattern corresponding to the intima-media-adventitia layers can be clearly observed (see Fig. 1, right).

Figure 1: Diagram of the arterial layers in a transverse section (left) and longitudinal view of the CCA in an ultrasound image (right)

Usually, the IMT is manually measured by the specialist, who marks pairs of points corresponding to the LII and MAI on the ultrasound. It is possible to

23 reduce the subjectivity and variability of manual approaches and detecting the
24 IMT throughout the artery length by means of image segmentation algorithms.

25 In the last two decades, several solutions have been developed to perform the
26 carotid wall segmentation in ultrasound images [4, 5] for the IMT measurement.
27 Most of the proposed methods require user interaction [6–10]. However, some
28 fully automatic approaches have already been published [11–17].

29 It is possible to make a classification of techniques according to the used
30 methodology. In this sense, we can find algorithms based on edge detection and
31 gradient-based techniques [6, 8, 9, 18], and other proposals based on dynamic pro-
32 gramming [19–24], active contours [7, 13, 14, 25–27], neural networks [11, 12]
33 or in a combination of techniques [10, 16]. There are also techniques based in
34 statistical modelling [17, 28] or in Hough transform [15, 29].

35 This work addresses a fully automated segmentation technique completely
36 based on Machine Learning to recognize IMT intensity patterns in the carotid
37 ultrasound images. In particular, the developed system intends to emulate the
38 procedure followed by the specialist in the manual protocol. That is, firstly, the
39 detection of the optimal measurement area and, then, the identification of the arte-
40 rial wall layers. With this purpose, a Deep Learning strategy has been designed to
41 obtain abstract and efficient feature representations by means of Auto-Encoders
42 based on Extreme Learning Machine (ELM). The proposed method jointly ex-
43 tracts the LII and MAI from ultrasound CCA images in a totally user-independent
44 and repeatable manner. Therefore, it improves the reproducibility and objectivity
45 of the IMT evaluation to assist in the early diagnosis of atherosclerosis.

46 The remainder of this paper is structured as follows: Sect. 2.1 describes the
47 dataset of ultrasound CCA images and the manual segmentations, while Sect. 2.2
48 introduces the machine learning concepts used in this work. In Sect. 2.3, the
49 proposed segmentation method is explained in detail. The obtained results are
50 shown in Sect. 3. Finally, the main extracted conclusions close the paper.

51 **2. Material and Methods**

52 *2.1. Image Database and Manual Segmentations*

53 The set of images used in this work consists of 67 ultrasounds of the CCA
54 taken with a Philips iU22 Ultrasound System using three different ultrasound
55 transducers or probes, with frequency ranges of 9-3 MHz, 12-5 MHz and 17-5
56 MHz. All of them were provided by the Radiology Department of Hospital Uni-
57 versitario Virgen de la Arrixaca (Murcia, Spain). The parameters of the scanner
58 were adjusted in each case by the radiologist. The spatial resolution of the images

59 ranges from 0.029 to 0.081 mm/pixel, with mean and standard deviation equal to
60 0.051 and 0.015 mm/pixel, respectively. Some blurred and noisy images, affected
61 by intraluminal artifacts, and some others with partially visible boundaries are
62 included in the studied set.

63 To assess the performance of the proposed segmentation method, it is neces-
64 sary to compare the automatic results with some indication of reference values. In
65 our case, the *ground-truth* corresponds to the average of four manual segmenta-
66 tions for each ultrasound image. In particular, two different observers delineated
67 each image twice, with a mean period of one month between tracings. Each man-
68 ual segmentation of a given ultrasound image includes tracings for the LII and
69 MAI on the far carotid wall. The delineations were performed by marking at
70 least 10 points over the images for each contour, which were subsequently inter-
71 polated. Once the four manual contours have been interpolated, the ground-truth
72 for each IMT interface (LII and MAI, separately) is assessed by averaging these
73 in a column-wise manner, i.e., along the longitudinal axis of the image. Figure
74 2 illustrates the process for the manual segmentations and the definition of the
75 ground-truth for each contour. Hereinafter, we will refer to the different segmen-
76 tations as:

- 77 • MA1: first manual segmentation from observer A.
- 78 • MA2: second manual segmentation from observer A.
- 79 • MB1: first manual segmentation from observer B.
- 80 • MB2: second manual segmentation from observer B.
- 81 • GT: ground-truth, average of MA1, MA2, MB1 and MB2.
- 82 • AUT: proposed automatic segmentation.

Figure 2: Manual segmentations: application for manual delineation of the IMT interfaces (top); definition of the ground-truth (GT, green line) from four manual segmentations made by two different observers (bottom)

83 *2.2. Machine Learning Techniques*

84 In the last decade, Extreme Learning Machine (ELM) has emerged as a pow-
 85 erful tool in the learning process of Single-Layer Feed-Forward Networks (SLFN)
 86 by providing good generalization capability at fast learning speed [30]. Given N
 87 arbitrary distinct samples $(\mathbf{x}_n, \mathbf{t}_n)$, where $\mathbf{x}_n \in \mathbb{R}^d$ is an input vector and $\mathbf{t}_n \in \mathbb{R}^m$
 88 its corresponding target vector, the output of a SLFN with M hidden neurons and
 89 activation function $f(\cdot)$ is given by

$$\mathbf{y}_n = \sum_{j=1}^M \beta_j f(\mathbf{w}_j \mathbf{x}_n + b_j), n = 1, \dots, N; \quad (1)$$

90 where $\mathbf{w}_j = [w_{j1}, w_{j2}, \dots, w_{jd}]$ is the input weight vector connecting the input
 91 units and the j -th hidden neuron, $\beta_j = [\beta_{j1}, \beta_{j2}, \dots, \beta_{jm}]$ is the output weight
 92 vector connecting the j -th hidden neuron and the output units, and b_j is the bias
 93 of the j -th hidden neuron. If it is assumed that SLFN can approximate these N
 94 samples with zero error, then, there exist β_j , \mathbf{w}_j and b_j such that

$$\sum_{j=1}^M \beta_j f(\mathbf{w}_j \mathbf{x}_i + b_j) = \mathbf{t}_i, i = 1, \dots, N. \quad (2)$$

95 ELM is based on the randomly initialization of the input weights and biases of
 96 SLFN. Thus, the network can be considered as a linear system and the N equations
 97 in the expression (2) can be written compactly in the following form:

$$\mathbf{H}\mathbf{B} = \mathbf{T}; \quad (3)$$

98 where $\mathbf{T} \in \mathbb{R}^{N \times m}$ is the targets matrix, $\mathbf{B} \in \mathbb{R}^{M \times m}$ is the output weights matrix
 99 and $\mathbf{H} \in \mathbb{R}^{N \times M}$ is the hidden layer output matrix, which is defined as

$$\mathbf{H} = \begin{bmatrix} f(\mathbf{w}_1 \mathbf{x}_1 + b_1) & \dots & f(\mathbf{w}_M \mathbf{x}_1 + b_M) \\ \vdots & \dots & \vdots \\ f(\mathbf{w}_1 \mathbf{x}_N + b_1) & \dots & f(\mathbf{w}_M \mathbf{x}_N + b_M) \end{bmatrix} \quad (4)$$

100 Thereby, the training is reduced to solve the linear system in Eq. (3), whose
 101 smallest norm least-squares solution is given by:

$$\hat{\mathbf{B}} = \mathbf{H}^\dagger \mathbf{T}; \quad (5)$$

102 where \mathbf{H}^\dagger is the Moore-Penrose generalized inverse matrix of \mathbf{H} . Moreover, in
 103 order to improve the robustness and generalization performance, a regularization
 104 term (C) can be added to the solution [31]:

$$\hat{\mathbf{B}} = \left(\frac{\mathbf{I}}{C} + \mathbf{H}^T \mathbf{H} \right)^{-1} \mathbf{H}^T \mathbf{T} \quad (6)$$

105 Although ELM provides an efficient training for SLFN, the performance of
 106 machine learning methods and applications highly depends on the selected fea-
 107 tures for the representation of the problem. Thus, to make progress towards the
 108 Artificial Intelligence (AI), the new perspectives in Machine Learning are nec-
 109 essary based on learning data representations that make more accurate classi-
 110 fiers/predictors [32]. In this sense, Deep Learning has emerged as set of algo-
 111 rithms that attempt to model more abstract and useful representation of the data
 112 by means of architectures with multiple non-linear transformations [33].

113 Among the various deep learning architectures, this work focuses on deep
 114 networks based on Auto-Encoders (AE). In particular, the ELM Auto-Encoders
 115 (ELM-AE) introduced in [34] have been used to solve our segmentation task.
 116 Auto-encoders are SLFN performing unsupervised learning in the sense that an
 117 AE is trained to reconstruct its own inputs, i.e. $\mathbf{t}_n = \mathbf{x}_n$ (see Fig. 3). Therefore,
 118 in the hidden layer of the AE takes place a feature mapping: if $M < d$ (number
 119 of hidden neurons $<$ input data dimension), a compressed data coding is obtained
 120 as hidden layer output (\mathbf{H}); while if $M > d$, the result is a sparse representation
 121 of data.

Figure 3: Structure of a generic Auto-Encoder

122 2.3. Segmentation Procedure

123 Figure 4 shows an overview of the proposed segmentation methodology. As
 124 can be seen in Fig. 1 (right), the raw images contain not only the CCA ultra-
 125 sound, but also a frame with patient data and additional information is incorpo-
 126 rated. Therefore, in order to remove this unwanted frame, the images are automati-
 127 cally cropped at the start. This is done by using Mathematical Morphology to de-
 128 termine the adequate borders of the ultrasound region, because the DICOM fields
 129 that provide these parameters are often empty. In particular, an image binarization
 130 takes place firstly, then, a procedure is applied to the obtained binary image in
 131 order to remove spurious objects and to fill regions or holes. It is based on two

132 basic morphological operators: opening and reconstruction. In this way, a binary
133 mask that matches with the ultrasound region is obtained and the unwanted frame
134 with metadata can be cropped. The process is simple and it does not show any
135 error on the tested images, i.e., the 67 ultrasound images are correctly cropped.

136 Once the CCA ultrasound is isolated, it is pre-processed to automatically detect
137 the region of interest (ROI), which is the far wall of the blood vessel. Then,
138 those pixels belonging to the ROI are classified for the LII and MAI recognition.
139 The final contours are extracted from the obtained classification results and the
140 IMT can be evaluated on them.

Figure 4: Flow chart of the proposed method for the CCA segmentation

141 2.3.1. ROI Detection

142 This section describes the first stage of the proposed methodology, in which
143 the carotid far wall (ROI, where the IMT will be evaluated) is located by means
144 of a system for Pattern Recognition. The scheme of the adopted strategy for this
145 purpose is shown in Fig. 5.

Figure 5: Overview of the strategy for the ROI (far wall of the artery) detection in CCA ultrasounds. An ELM-AE provides a compressed representation of input image blocks at its hidden layer output to improve the classification performance

146 Specifically, a given CCA ultrasound is split into blocks (squared sections)
147 to proceed with the processing. An ELM-AE has been designed to obtain useful
148 and efficient representations of image blocks for their posterior classification as
149 ‘ROI-block’, if a typical pattern of the far wall is recognized, or ‘non-ROI-block’,
150 otherwise. The size of the image blocks to process is 39×39 pixels, which ensures
151 that the intima-media complex can be contained in a block even if the arterial wall
152 is thick and the radiologist selects high resolutions. Thus, the ELM-AE has an
153 input data dimension of 1521 features.

154 For the configuration of the ELM-AE, an exhaustive search of the number of
155 hidden neurons and the regularization parameter (M and C, respectively) by means
156 of a validation procedure has been performed. As it is verified later in Sect. 3.1.1,
157 the optimal coding is obtained with 850 hidden sigmoidal neurons. Once the
158 architecture of the AE is fixed, the connections between the new features (hidden
159 layer outputs, \mathbf{h}) and the system output (\mathbf{y}) are analytically calculated according
160 to Eq. (6).

161 The dataset used in the design of this system consists of 13776 observations
162 (50% from each class): two thirds for training and the remaining for testing. In
163 particular, the samples were carefully taken from five heterogeneous images (with
164 different orientations of the CCA, spatial resolutions, IMT values, etc.) to assem-
165 ble a representative and consistent dataset. Table 1 specifies the distribution of the
166 selected samples.

Table 1: Specification of samples used in the design of the system for far wall detection

167 2.3.2. Arterial Layers Recognition

168 The segmentation of the LII and MAI in the ultrasound images is carried out
169 by means of a classification of pixels belonging to the ROI. In particular, the inten-
170 sity values from a certain neighbourhood centred on the pixel to classify provide
171 the necessary contextual information to the classifier for the recognition of the
172 arterial layers. Specifically, the neighbourhoods consist of 51×5 pixels (i.e., 255
173 input features) and four different classes have been considered as possible sys-
174 tem outputs: ‘*LII-pixel*’, ‘*MAI-pixel*’, ‘*IMC-pixel*’ (intima-media complex) and
175 ‘*non-IMC*’ (out of the intima-media complex). As in the previous stage, repre-
176 sentational learning techniques have been applied to improve the precision of the
177 classifier. With the aim of obtaining meaningful representations from the inputs
178 corresponding to LII and MAI, two different multilayer ELM-AE (with multiple
179 hidden layers) have been implemented. These multilayer auto-encoders (MLAE)
180 are based on the concept set forth in [34], where ELM is used to perform layer-
181 by-layer unsupervised learning. The diagram of the proposed deep architecture
182 can be seen in Fig. 6.

Figure 6: Deep-architecture designed for the LII and MAI segmentation. Two different multilayer ELM-AE produce sparse coding of the input patterns at the output of their second hidden layer. Then, the union of the learned representations is classified for the recognition of the arterial layers

183 To perform the design and training process of this architecture, a labelled
184 dataset composed of 38908 patterns was assembled by taking samples from 8
185 manually segmented images. The distribution per class and image of the sam-
186 ples is shown in Table 2: 50% of them belong to the IMT boundaries (‘LII’ and
187 ‘MAI’ classes), and the remaining 50% are distributed between ‘IMC’ class (8904
188 samples) and ‘non-IMC’ class (10554 samples). Besides, the dataset is carefully

Table 2: Specification of dataset used in the design of the system for arterial layers recognition

189 divided into three subsets: one-third of samples for testing, 80% of the remaining
 190 two thirds for training and 20% for validation.

191 The configuration of the LII-MLAE has been done by means of a layer-wise
 192 unsupervised training with the 5877 LII samples (training and validation sets). As
 193 commented before, the learning process is carried out in a layer-by-layer man-
 194 ner, i.e., each hidden layer is trained as a simple single layer ELM-AE (see Fig.
 195 6) by taking the hidden layer outputs of the previous AE as inputs and desired
 196 outputs (unsupervised learning, $t_n = x_n$). Therefore, the final LII-MLAE archi-
 197 tecture consists of the succession of the hidden layers of the designed single layer
 198 auto-encoders along with their corresponding connection weights. Moreover, it is
 199 necessary to establish the optimal number of layers for the LII-MLAE. Thus, after
 200 designing each layer, it is added to the LII-MLAE architecture only if it allows an
 201 improvement in the recognition of LII patterns. In order to know if this happens,
 202 the performance of a binary auxiliary classifier (*‘LII-pixels’* or *‘non-LII-pixels’*)
 203 is examined using the whole dataset (more details in Sect. 3.1.2). Taking into
 204 account this consideration, the optimal architecture for the LII-MLAE consists of
 205 two stacked stages, which perform a ‘255-1100-1900’ feature mapping.

206 On the other hand, using exclusively MAI samples (5672 for training and 1417
 207 for validation), the MAI-MLAE has been configured in a similar manner to repre-
 208 sent better the MAI patterns. In this case, the optimal coding is also obtained with
 209 two hidden layers (‘255-1000-1900’ mapping).

210 In accordance with the suggested system (return to Fig. 6), a given input \mathbf{x}
 211 is transformed into two different feature vectors with 1900 dimensions each one.
 212 These new representations of the system input (\mathbf{h}_{LII} and \mathbf{h}_{MAI}) are then joined
 213 for proceeding to their classification. The connections between the union of out-
 214 puts from the second hidden layer of both AE (\mathbf{h}) and the system output (\mathbf{y}) are
 215 computed in accordance with the expression (6).

216 2.3.3. Extraction of Final Contours

217 Once a CCA ultrasound is processed by means of the proposed system, the
 218 IMT boundaries are properly identified (see Fig. 7, right-central, where the LII
 219 and MAI pixels detected are depicted in red and blue, respectively). However,
 220 due to the poor definition of the ultrasound images, thick boundaries are obtained.
 221 This happens because the system finds the searched intensity patterns in all these
 222 pixels. In fact, the classification results cover the variability of the manual seg-

223 mentations, as can be seen in Fig. 7 (right-central), where the points marked by
 224 the two specialist are superimposed.

Figure 7: Example of a good quality processed image: far wall detected (left); ROI with manual segmentations (right-top); recognition of IMT boundaries and manually marked points (right-central); final LII and MAI contours (right-bottom)

225 Therefore, it is necessary to define the final contours from the system output.
 226 For this purpose, the gradient image is evaluated by using morphological operators
 227 (Fig. 8, top). Then, the search for the peaks of the intensity gradient is performed
 228 (Fig. 8, central). Specifically, the points of maximum gradient which fall within
 229 pixels classified as ‘*LII-pixel*’ or ‘*MAI-pixel*’ are considered (Fig. 8, bottom).
 230 From these points, two curves corresponding to LII and MAI interfaces are defined
 231 by means of a smoothing process based on a moving average filter. The final
 232 contours of IMT are determined in this way (see Fig. 7, right-bottom).

Figure 8: Extraction of final contours: gradient image corresponding to Fig. 7 (top); peaks of the intensity gradient (central); points of maximum gradient which fall within pixels classified as ‘*LII-pixel*’ or ‘*MAI-pixel*’ by the system (bottom)

233 3. Results and Discussion

234 3.1. Architecture Configuration and Classification Performance

235 This section includes the results of the performed study for the configuration
 236 of the system, as well as the evaluation of its classification performance. For
 237 this analysis, several metrics have been used: the *accuracy* (ACC), *specificity*
 238 (*SPEC*), *sensitivity* (SEN), and the *Mathews correlation coefficient* (MCC) of a
 239 given classification, which are defined as follows:

$$ACC = \frac{TP + TN}{TP + TN + FP + FN} \quad (7)$$

$$SPEC = \frac{TN}{TN + FP} \quad (8)$$

$$SEN = \frac{TP}{TP + FN} \quad (9)$$

$$MCC = \frac{TP \cdot TN - FP \cdot FN}{\sqrt{(TP + FP) \cdot (TP + FN) \cdot (TN + FP) \cdot (TN + FN)}}, \quad (10)$$

240 where TP is the number of true positives; TN is the number of true negatives; FP
241 and FN are the number of false positives and false negatives, respectively.

242 3.1.1. ROI Detection

243 As commented in Sect. 2.3.1, a validation procedure becomes necessary for
244 the configuration of the ELM-AE. The design parameters to select are the number
245 of hidden neurons (M) and the regularization term (C). In our case, 28 different
246 values for M (10, 20, ..., 100, 150, 200, ..., 1000) and 38 different values for C
247 (2^{-18} , 2^{-17} , ..., 2^{19}) have been considered. The ELM-AE was retrained 50 times
248 for every pair of values ($50 \times 28 \times 38$) and its mean performance has been analysed.
249 Moreover, 20% of training samples were randomly selected as validation set in
250 each trial.

251 The learning process is carried out in an unsupervised manner, i.e. with tar-
252 get values identical to inputs. However, the selection of its design parameters has
253 been performed by analysing the classification accuracy of the system over the
254 validation samples. For this purpose, a provisional output is computed according
255 to Eq. (5) in each case. Thus, it is possible to analyse the surface of the classifica-
256 tion performance (see Fig. 9, left). In view of this result, the optimal compressed
257 coding is obtained with 850 hidden neurons and $C_1 = 2^{-6}$.

258 Once the single hidden layer of the ELM-AE is adjusted, the output connec-
259 tions of the system must be determined according to Eq. (6). Therefore, a new
260 tuning of another regularization parameter ($C_2 = 2^{-18}$, 2^{-17} , ..., 2^{24} , 2^{25}) is per-
261 formed. The analysis of the mean validation accuracy (see Fig. 9, right) shows
262 that the optimal value is $C_2 = 2^{19}$, because from that point, the saturation is
263 reached.

Figure 9: Classification accuracy over validation set. Mean performance of the ELM-AE (50 trials) according to M and C_1 , i.e. number of hidden neurons and regularization term (left). Analysis for the tuning of the second regularization parameter (C_2) related to the computation of the output connections (right)

264 Finally, note that the proposed system has proved its good performance. The
265 confusion matrix of the system over the test samples, which are completely unre-
266 lated to the training/validation process, is shown in Table 3. From this informa-
267 tion, it is possible to deduce that the accuracy of the classification between ROI

268 and non-ROI image blocks is 98.45 ± 0.06 % (mean and standard deviation from
 269 50 trials). Moreover, the sensitivity is 99.38 ± 0.06 % and the specificity is 97.56
 270 ± 0.11 %, which describe the ability of the system to identify positive results (ROI
 271 observations) and negative results (non-ROI observations), respectively.

Table 3: Confusion matrix of the system for ROI detection

272 3.1.2. Detection of IMT Boundaries

273 Two different multilayer ELM-AE are part of the system developed for the
 274 recognition of the arterial layers in CCA ultrasounds (see Fig. 6). The configura-
 275 tion of these machines has been performed in a layer-wise unsupervised manner.
 276 For each layer, the number of hidden neurons and the regularization parameter
 277 were varied as follows: $M = \{10, 20, \dots, 500, 550, \dots, 1000, 1100, \dots, 2000\}$; and
 278 $C = \{2^{-18}, 2^{-17}, \dots, 2^{50}\}$. Fifty trials were conducted for each pair of values.
 279 In each case, the Root-Mean-Square Error (RMSE) between the equivalent in-
 280 puts and outputs of the LII-MLAE and MAI-MLAE was evaluated. The optimal
 281 parameters (M_{opt} and C_{opt}) for every layer have been selected according to the
 282 minimal validation RMSE obtained.

283 An additional parameter of the architecture to optimize is the number of hid-
 284 den layers constituting the LII-MLAE and the MAI-MLAE. As it is mentioned
 285 in Sect. 2.3.2, a layer is appended to the LII-MLAE or MAI-MLAE architec-
 286 ture only if this fact implies an improvement in the recognition of LII patterns or
 287 MAI patterns, respectively. With the aim of determining this enhancement, the
 288 whole dataset is passed through the corresponding AE and the performance of a
 289 binary classification between ‘LII-pixels’ and ‘non-LII-pixels’ (or between ‘MAI-
 290 pixels’ and ‘non-MAI-pixels’) is analysed. Note that this provisional labelling of
 291 the dataset involves an imbalanced class distribution. Therefore, the connections
 292 between the outputs of the hidden layer under analysis and these provisional bi-
 293 nary outputs have been assessed according to the Weighted-ELM [35].

294 The results obtained in the design process of the LII-MLAE and the MAI-
 295 MLAE are summarized in Table 4, where ACC and MCC represent the accuracy
 296 and Mathews correlation coefficient of the related binary classification, respec-
 297 tively. The latter is generally regarded as a balanced measure which can be used
 298 even if the classes are of very different sizes. Thus, the optimal architecture for
 299 the LII-MLAE consists of two stacked stages, which perform a ‘255-1100-1900’
 300 feature mapping; whereas in the case of the MAI-MLAE, the optimal coding is
 301 also obtained with two hidden layers (‘255-1000-1900’ mapping).

Table 4: Specification of the analysis for LII-MLAE and MAI-MLAE configuration

302 The final deep architecture achieves a high success rate over the testing dataset.
303 Table 5 shows the confusion matrix of the system in terms of mean and standard
304 deviation from 50 trials. The overall success rate is $99.44\pm 0.05\%$ (considering
305 the four classes), with $99.76\pm 0.03\%$ of accuracy in the recognition of LII patterns
306 and $99.69\pm 0.04\%$ for the classification of MAI samples.

Table 5: Confusion matrix of the system for the arterial layers segmentation

307 3.2. Visual Results

308 The proposed segmentation method has been tested on a set of 67 ultrasound
309 images of the common carotid artery. Fig. 7 shows an example of processed im-
310 age. Left image depicts the result of the stage for the far wall detection, whereas
311 right pictures show the ROI in detail, where the manual segmentations (top), the
312 classification results and manually marked points (central) and the final IMT con-
313 tours (bottom) are superimposed on the ultrasound. The correct detection of the
314 far wall is achieved in all the tested images, even in noisy and blurred ones. Some
315 examples can be seen in Fig. 10.

Figure 10: Examples of correct far wall detection in CCA ultrasounds

316 To ensure an optimal visualization of the IMT boundaries in the ultrasound, a
317 straight and horizontal appearance of the carotid artery in the image is desirable.
318 However, this projection is not always possible. Sometimes, the CCA may be
319 tilted or curved because of the probe position or the own anatomy of the subject.
320 In the case of algorithms using human interaction, the operator can select the
321 optimal area of the image for the IMT measurement. Nevertheless, fully automatic
322 methods must be able to correctly handle the different morphologies of the artery.
323 The examples of final results included in Fig. 11 reveals that the fully automatic
324 segmentation approach proposed in this paper is robust against the orientation and
325 appearance of the CCA in the ultrasound image (slope and curvature).

Figure 11: Final IMT boundaries obtained for the images in Fig. 10

326 3.3. Segmentation Accuracy

327 In order to validate the precision of the obtained segmentation results, four
328 manual tracings performed by two different experts are taken into consideration.
329 On the one hand, manual segmentations are compared between themselves in order
330 to characterize the uncertainty and variability of the manual procedure. Thus,
331 the intra-observer errors (MA1 vs MA2 and MB1 vs MB2) as well as the inter-
332 observer errors (MA1 vs MB1, MA1 vs MB2, MA2 vs MB1 and MA2 vs MB2)
333 have been evaluated. On the other hand, the inter-method error is evaluated by
334 comparing our automatic segmentations with those considered as ground-truth
335 (AUT vs GT). In addition, in order to complete the characterization of the auto-
336 matic IMT contours, comparisons between each of the four manual segmentations
337 and the automatic ones (AUT vs MA1, AUT vs MA2, AUT vs MB1 and AUT vs
338 MB2) have been studied. The different segmentation errors are calculated sep-
339 arately for LII and MAI contours using the Mean Absolute Difference (MAD),
340 which is the most used quantitative metric to evaluate IMT and the accuracy of
341 a segmentation method [4, 5]. This metric represents the average of the vertical
342 distances between two contours along the longitudinal axis of an image.

343 The box-plot in Fig. 12 shows the distributions of the segmentation errors for
344 LII and MAI over the 67 tested ultrasound images. Moreover, Table 6 includes the
345 maximum, minimum, mean and standard deviation values of the different errors
346 over the image database. Since the scale resolution varies from one image to
347 another, the results are expressed in μm and pixels, for a better description of the
348 difference between segmentations. This statistical analysis reveals that a greater
349 variability exists for the MAI, which is much more noticeable between manual
350 segmentations. This is due to the fact that, in general, transitions from lumen to
351 intima layer are clearer than transitions from media to adventitia layer.

352 The difference between manual tracings of LII ranges, on average, from 29.7
353 μm to 40.6 μm , whereas manual segmentation error for MAI varies between 43.5
354 and 53.9 μm . Despite the greater error and the higher dispersion of the error for
355 the MAI boundaries, there is a good agreement between manual tracings, since
356 the mean differences are around one pixel.

357 Nevertheless, when the comparisons are made between automatic contours
358 and GT, the segmentation errors for LII and MAI are considerably reduced. Be-
359 sides, although the MAI error remains slightly greater on average, its distribution
360 is more comparable to the distribution of LII error. In view of the results, it is pos-
361 sible to appreciate that our automatic segmentation reduces the uncertainty and
362 variability of the manual procedure and, therefore, it will lead to a more reliable
363 and precise measurement of the IMT.

Figure 12: Statistical distribution of Mean Absolute Difference (mm) between different segmentations for LII and MAI. Box-plot: in each box, the whiskers extend to the most extreme not outliers values (marked as black crosses), upper and lower box limits represent the 75th and 25th percentile, respectively; the median is depicted by the inner line in the box

Table 6: Mean absolute difference between different segmentations for LII and MAI

364 3.4. *IMT Measurements*

365 Given an ultrasound image and the corresponding boundaries of the arterial
 366 wall, manually or automatically segmented contours, the IMT is estimated by
 367 using three different metrics: Mean Absolute Difference (MAD), Poly-Line Dis-
 368 tance (PLD) and Center Line Distance (CLD). As commented in Sect. 3.3, MAD
 369 is the most used metric to evaluate IMT. It is based on the vertical distance be-
 370 tween contours along the longitudinal axis of an image. In particular, it is nec-
 371 essary that both contours have the same number of points (N) to calculate the
 372 average of these vertical distances (see Fig. 13, top) as follows:

$$IMT_{MAD} = \frac{1}{N} \sum_{x=1}^N |LII(x) - MAI(x)| \quad (11)$$

373 Nevertheless, MAD may deviate from the actual distance between LII and MAI
 374 when these contours present certain slope or curvature. To avoid the overesti-
 375 mation in these cases, PLD was proposed in [36] as a more robust and reliable
 376 indicator of the distance between two boundaries. It is based on trigonometry
 377 and, in this case, it is not a necessary condition that the contours to compare have
 378 the same number of points. Given the IMT contours, LII with N_1 points and MAI
 379 with N_2 points (see Fig. 13, centre), the distance between a vertex $v = (x_0, y_0)$ in
 380 LII and the segment s in MAI (from $v_1 = (x_1, y_1)$ to $v_2 = (x_2, y_2)$) is defined as:

$$d(v, s) = \begin{cases} |d_{\perp}|, & \text{if } 0 \leq \lambda \leq d_{12} \\ \min(d_1, d_2), & \text{otherwise} \end{cases} \quad (12)$$

381 where d_1 and d_2 are the euclidean distances between the vertex v and the vertices
 382 in the segment s (v_1 and v_2 , respectively); whereas d_{12} is the euclidean distance
 383 between v_1 and v_2 . As can be seen in Fig. 13 (centre), d_{\perp} is the perpendicular
 384 distance from s to v , and λ is the distance along the segment s between v_1 and the
 385 intersection with the perpendicular. In this way, the distance from $v \in$ LII to MAI
 386 is calculated as:

$$d(v, MAI) = \min_{s \in MAI} d(v, s) \quad (13)$$

387 The distance between LII and MAI is evaluated as the sum of the distances from
 388 all the vertices in LII to the closest segment in MAI:

$$d(LII, MAI) = \sum_{v \in LII} d(v, MAI) \quad (14)$$

389 Similarly, the distance from MAI to LII is assessed ($d(MAI, LII)$). And finally,
 390 the IMT can be measured by using PLD in the following form:

$$IMT_{PLD} = \frac{d(LII, MAI) + d(MAI, LII)}{N_1 + N_2} \quad (15)$$

391 The third of the three considered metrics is CLD [37], which also takes into ac-
 392 count the local orientation of the IMT boundaries. CLD is based on the calculation
 393 of the center line between LII and MAI (see Fig. 13, bottom). Once this line is
 394 found, a segment perpendicular to the center line, which intersects with the two
 395 boundaries, is considered at each point, and CLD is defined as the mean length of
 396 all these segments:

$$IMT_{CLD} = \frac{1}{N} \sum_{i=1}^N l_i \quad (16)$$

397 where l_i is the length of the i -th segment and N is the number of points of the
 398 center line. In this case, just like in the MAD metric, the number of points of LII
 399 and MAI must be the same.

Figure 13: Diagrams of the three different metrics used to evaluate the IMT: Mean Absolute Difference, MAD (top); Poly-Line Distance, PLD (centre); Center Line Distance, CLD (bottom)

400 For each ultrasound image, the IMT has been evaluated for manual and auto-
 401 matic segmentations using the aforementioned metrics (MAD, PLD and CLD) to
 402 quantify the distance between the corresponding LII and MAI contours. Similar
 403 distributions of the IMT values are obtained for the 4 manual measures and the
 404 automatic one, as can be seen in Table 7. It is possible to note the slight overesti-
 405 mation produced by the MAD metric in the IMT measurement.

Table 7: Statistics of the IMT measurements ($n = 67$ images) in millimetres using different metrics (MAD, PLD and CLD)

406 As in Sect. 3.3, intra and inter-observer IMT errors have been estimated for
 407 the manual measurements to be compared with the error between automatic IMT

408 and GT. Given two different segmentations S_1 and S_2 , the degree of agreement
 409 between its IMT measures over the 67 images is assessed by calculating three
 410 figures of merit: the correlation coefficient (ρ), the absolute error value ($\varepsilon_{IMT_i} =$
 411 $|IMT_i^{S_1} - IMT_i^{S_2}|$, for each image) and the difference between measurements
 412 ($\Delta_{IMT_i} = IMT_i^{S_1} - IMT_i^{S_2}$, $i = 1, \dots, 67$). Table 8 shows the results of the IMT
 413 measurement error analysis.

414 The IMT intra-observer reproducibility is of 98.4% for observer A and prac-
 415 tically 98% for observer B (see the corresponding correlation coefficients in Ta-
 416 ble 8). Moreover, the inter-observer reproducibility of the IMT measurements is
 417 around 97%. This high grade of agreement between manual measures confirms
 418 the goodness of the 4 manual segmentations and, consequently of the GT, which
 419 is defined as the average of these ones. The absolute errors and the standard devi-
 420 ations of the differences indicate a greater IMT inter-observer error in comparison
 421 with the error between IMT measures from the same observer, which seems logi-
 422 cal.

Table 8: Comparison between IMT measurements (MAD, PLD and CLD metrics) from different segmentations. $n = 67$ images; ρ : Correlation coefficient; ε_{IMT} : Mean \pm standard deviation of the absolute errors; Δ_{IMT} : Mean \pm standard deviation of the differences

423 The difference between automatic IMT and GT is of $5.8 \pm 34 \mu\text{m}$ for MAD
 424 and PLD metrics ($6.7 \pm 34 \mu\text{m}$ for CLD), whereas the absolute error of the au-
 425 tomatic measurements is $27.3 \pm 21 \mu\text{m}$ for MAD and PLD ($27.2 \pm 22 \mu\text{m}$ for
 426 CLD). These values reveal that the measurement error associated with the pro-
 427 posed method is lower than the inter-observer errors and it is in the rank of the
 428 intra-observer errors. In addition, the correlation coefficient (98.1%) is compar-
 429 able to the intra-observer variability.

430 Figure 14 (right) depicts the linear regression analysis between automatic IMT
 431 and GT (MAD, PLD and CLD metrics), where the high degree of agreement can
 432 be observed. Furthermore, Fig. 14 (left) shows the corresponding Bland-Altman
 433 plots (MAD, PLD and CLD metrics) with the following limits of agreement (mean
 434 $\pm 2 \times$ standard deviation): $5.8 \pm 68.8 \mu\text{m}$ for MAD, $5.8 \pm 68.5 \mu\text{m}$ for PLD, and
 435 $6.7 \pm 68.5 \mu\text{m}$ for CLD. The vertical axis in the Bland-Altman plot represents
 436 the difference between AUT and GT measures of the IMT, whereas the horizontal
 437 axis represents the average of the values compared. Therefore, the precision in
 438 the automatic IMT measurements is full well justified.

Figure 14: Analysis of automatic IMT measurements: Bland-Altman plot (left) and linear regression analysis (right)

439 **4. Conclusions**

440 This paper proposes a fully automated segmentation method for CCA ultra-
441 sounds to accurately measure the IMT, an early indicator of atherosclerosis and
442 cardiovascular risk. This proposal is completely based on Machine Learning, in
443 order to detect the arterial far wall and to extract the IMT contours (LII and MAI)
444 in a reliable and automatic way. In particular, the suggested architecture is based
445 on the Extreme Learning Machine (ELM). Furthermore, Auto-Encoders (AE) and
446 Deep Learning concepts have been used to obtain useful data representations for
447 solving the segmentation task, which is posed as a Pattern Recognition problem.
448 Following the developed strategy, the IMT can be measured in a totally user-
449 independent and repeatable manner.

450 The method has been tested over a database of 67 images with different spatial
451 resolutions. The validation of the technique is carried out by comparing the auto-
452 matic contours with the average of four manual segmentations performed by two
453 different observers. The results show a mean segmentation error of 0.028 mm for
454 the LII and 0.035 mm for the MAI and demonstrate that the proposed methodol-
455 ogy reduces the uncertainty and variability of the manual procedure. In reference
456 to the IMT measurements, a high grade of agreement between manual and auto-
457 matic observations is obtained with a difference of only $5.8 \pm 34 \mu\text{m}$ (mean and
458 standard deviation).

459 With these error values, the algorithm outperforms both automatic and semi-
460 automatic methods presented in the literature. Table 9 summarizes the results
461 reached by other IMT measurement methods. All methods included in Table 9
462 do not consider ultrasound images with atherosclerotic plaques, and use MAD
463 metric to evaluate the IMT and the different errors. Although direct comparisons
464 between different studies are difficult due to the dependence on the measurement
465 protocol, characterization of the results, number and type of patients, tissue to
466 be segmented and image quality, it can be seen that our automatic segmentation
467 compares favourably to other semi-automatic and automatic algorithms.

Table 9: Some IMT measurement methods

468 It is important to pay special attention to the works [11] and [12], which cor-
469 respond to previous contributions from the authors of this paper. In the previous

470 papers [11, 12], as well as in this one, a novel point of view is presented for this
471 specific application and the posed problem is solved by means of Pattern Recog-
472 nition techniques. This new proposal is oriented to improve the generalization
473 capability and the performance of the method in order to achieve the best system
474 configuration.

475 In particular, the new approach is completely based on Machine Learning
476 (ML), both the recognition of the carotid far wall (region of interest, ROI) and
477 the identification of the IMT contours (LII and MAI). Whereas in [11, 12], dif-
478 ferent image processing techniques were applied to detect the ROI, none of them
479 based on ML. The use of a new pattern recognition strategy based on ML for the
480 recognition of the ROI implies that the system is able to adapt to the optimal area
481 for the measurement, by avoiding those uncertain regions in which the character-
482 istic IMT pattern is unclear, blurred or even hidden. Moreover, in this work, it has
483 been studied the utilisation of ELM multilayer AE to obtain sparse data represen-
484 tations with the aim of obtaining a high performance classifier. With the proposed
485 architecture, the obtained results show an overall success rate exceeding 99% in
486 the classification of the nearly 13000 test samples. In [12], single-layer AE were
487 considered only to reduce the data dimension. ELM algorithm was not used in the
488 previous contributions [11, 12], but in the present study it has provided advantages
489 in the learning process (training and design) of the proposed system, because of
490 its good performance at fast speed even with high-dimensional data. Furthermore,
491 the suggested strategy has been designed to recognize jointly LII and MAI and it
492 is able to identify and differentiate both contours by means of the developed mul-
493 ticlass classifier (4 classes); whereas in the previous works [11, 12], only binary
494 classifications were considered. In this way, the post-classification stage of the
495 new proposal does not require hard efforts for debugging the results and for the
496 extraction of the final IMT boundaries and it has been simplified notably.

497 To summarize, the main contributions and improvements of the proposed method
498 are the following: a greater intelligence and autonomy of the system; the high de-
499 gree of robustness against the anatomical and instrumental variability of the ultra-
500 sound images; and the noteworthy reliability and precision in the evaluation of the
501 IMT. Finally, it is important to emphasize that these positive aspects are crucial
502 for a fully automatic method which has been designed to assist in the early detec-
503 tion of atherosclerosis and the prevention of cardiovascular diseases. According
504 to this, it can be concluded that the proposed methodology is suitable for the eval-
505 uation of IMT not only in the daily clinical practise, but also in clinical research
506 studies.

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