

1           **Theoretical Analysis of a Transcritical Power Cycle for Power**  
2           **Generation From Waste Energy at Low Temperature Heat**  
3           **Source**

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9  
10          **Abstract:**

11          The present paper reports the results obtained on a carbon dioxide transcritical  
12          power cycle using an energy and exergy analysis. The procedure consisted of  
13          modifying the inlet pressure to the turbine from 66 bar, by means of the  
14          software HYSYS®, maintaining constant each evaluated turbine inlet  
15          temperature (60, 90, 120 and 150 °C) until the net work was approximately  
16          zero. As a result, an increase up to 25% for the exergy efficiency, and up to  
17          300% for the energy efficiency are obtained when the inlet temperature to the  
18          turbine is risen from 60 to 150 °C. Consequently, the analysis shows the  
19          viability of implementing this process as alternative energy, because of the  
20          possibility to recovery energy from waste heat from industrial processes.

21          **Keywords:**

22          Carbon dioxide, energy efficiency, exergy efficiency, power generation, waste  
23          heat.

24 **Nomenclature**

25 CDTPC Carbon Dioxide Transcritical Power Cycle

26  $\dot{E}$  Exergy rate, kW

27 GWP Global Warming Potential

28  $h$  Specific enthalpy, kJ/kg

29  $\dot{I}$  Irreversibility rate, kW

30  $\dot{m}$  Mass flow, kg/s

31  $w_{ne}$  Net specific work

32 ODP Ozone Depletion Potential

33 ORC Organic Rankine Cycle

34  $P$  Pressure, bar

35  $\dot{Q}$  Heat flow, kW

36 state point 1, 2, 2<sub>is</sub>, 3, 4, 4<sub>is</sub>

37  $T$  Temperature, °C

38  $\dot{W}$  Power, kW

39

40 **Subscripts**

41 H Heat source

42 is Isentropic

43 L Heat sink

44 max Maximum

45 p Pump.

46 t Turbine.

47 0 Environmental state

48

49 **Greek symbols**

50  $\eta$  Efficiency

51

52 **1. Introduction**

53 After having detected environmental problems related to the use of fossil fuels, which  
54 influence in human health and ecosystems sustainability, there is a need of covering the  
55 growing energy demand with renewable energies and with an efficient use of the energy.  
56 Energy savings must be taken into account like an alternative energy source, where it is  
57 important to avoid waste heat by using new technologies that have emerged in market,  
58 with a cost saving approach as well.

59 A promising technology for satisfying this is the organic Rankine cycle "ORC" [1], which  
60 allows to use waste heat or low temperature sources such as some renewables [2-3]. This  
61 operates equal to the conventional Rankine cycle and the fact of working with an organic  
62 agent as the working fluid, makes possible to recovery low enthalpy energy sources.  
63 However, some limitations must be overcome as the pinching problem that can occur in  
64 the ORC's counter current heat exchanger evaporator, which can make unsuitable the use  
65 of this equipment because of the constant evaporation temperature of the organic  
66 substance [4].

67 Thus, with the purpose of employing sensitive heat sources as waste heat, some authors  
68 have proposed the use of working fluids in supercritical conditions [5-7] and/or zeotropic  
69 fluids [8-9] in the traditional Rankine cycle, obtaining therefore a better fit between the  
70 working fluid and the heat source when the heat is added. The results of an exhausted

71 thermodynamic analysis realized to a transcritical power cycle with carbon dioxide as  
72 working fluid are presented in [10]. The simulation carried out in the study showed that the  
73 proposed process is suitable for the production of useful energy utilizing heat sources  
74 between 60 and 150 °C and, additionally, emphasizes as, with an internal heat exchanger  
75 increases considerably the energy and exergy efficiency. However, the great complexity of  
76 the plant by the incorporation of this exchanger makes that the real application depends  
77 strongly on the operability and the cost of the equipment for the high pressures required  
78 for the operation of the cycle.

79 Carbon dioxide (CO<sub>2</sub>) as a natural refrigerant has been employed for refrigeration  
80 applications, but its excellent chemical and physical properties, make that is also  
81 considered as working fluid in power cycles. Some of these characteristics are the non-  
82 toxicity, environment-friendly with an Ozone Depletion Potential (ODP) of zero [11] and a  
83 Global Warming Potential (GWP) of 1 over 100 years [12], its moderate critical pressure  
84 (73.8 bar), relative inertness (for the temperature range of interest), non-explosivity, low  
85 cost and abundance in nature [3]. Moreover, its thermodynamic properties are well known  
86 and it is an environmentally friendly gas. Furthermore, it may have a great potential to  
87 improve energy conversion in a more efficient way while greatly reducing the global  
88 discharge of CO<sub>2</sub> in the world by using waste heat as the energy source of the system.  
89 Also, although with less influence, this is a way of capturing CO<sub>2</sub> when it is utilized as  
90 working fluid.

91 The current study presents the thermodynamic power cycle with CO<sub>2</sub> as working fluid that  
92 acts between subcritical and supercritical states, “a transcritical cycle”, due to its low  
93 critical temperature (31.1 °C). Despite the lack of information available in the use of this  
94 gas as working fluid in low temperature heat source for power generation, the excellent  
95 results obtained in the incipient research incite to continue in this field. In the last few  
96 years, the transcritical cycle with carbon dioxide has been studied in steady state with

97 solar energy as the heat source at a temperature near 200 °C [13], and an annual dynamic  
98 performance is simulated in [7]. A small-scale prototype has been built and started up [14],  
99 showing its feasibility and achieving efficiencies between 8.8%–9.5% [15]. According to  
100 the comparative study carried out in [3], the carbon dioxide transcritical power cycle  
101 (CDTPC) showed slightly higher power output than the ORC with a R123 as working fluid.  
102 Finally, the methodology presented in [4] has been applied for the study of a CO<sub>2</sub>  
103 transcritical cycle supplied by a steady stream of low temperature process gases. These  
104 results have been calculated varying the high pressure of the cycle and its net power  
105 output, for fixed temperature and mass flow rate of the heat source, fixed maximum and  
106 minimum temperatures in the cycle and fixed sink temperature. Some of the researchers  
107 of [4] developed the study of the influence of the inlet temperature in the turbine (80 – 99  
108 °C) on the total performance of the simple cycle, maintaining the same suppositions of the  
109 mentioned research, whose results are shown in [5].

110 In view of what has been stated, there is great interest in the use of this fluid for the energy  
111 use of sources below 150 °C. However, there are not many works reported in the literature  
112 on the CDTPC [3-7,10,13-15], and as it is commented in [10], it is notable the lack of  
113 studies in this theme. Therefore, the main novelty aspects provided in the present paper,  
114 are addressed to contribute in the increase of these studies showing, between others, the  
115 influence of the inlet temperature and pressure to the turbine in this process, avoiding all  
116 type of “distortions” or “noises” by external parameters on the behavior of the fluid within  
117 the cycle. Thus, in this paper, it is only calculated how much energy is required to heat the  
118 process flow directed to the turbine. Because the analysis of the heat source conditions is  
119 not our aim (i.e. it is not restricted the study to an only application), this study can be  
120 therefore used directly for analyzing its applicability with heat sources of low temperatures  
121 as waste heat from process industrial sectors, and from renewable sources, as solar,  
122 geothermal, biomass, etc.

## 123 **2. Description of the carbon dioxide transcritical power cycle.**

124 Water is the working fluid most frequently used in power systems with steam because is  
125 abundant, cheap, non-toxic, chemically stable and relatively non-corrosive. Water has also  
126 a large specific enthalpy when is vaporized at ordinary pressures in the steam generator,  
127 which allows to reduce the mass flow rate for a given net power of the cycle. The  
128 properties of liquid water and steam are also such that work ratios obtained are very small  
129 and the reheating and regeneration techniques are effective in improving the thermal  
130 performance of the plant. However, water is less satisfactory than some other working  
131 fluids with respect to other features. For instance, the critical temperature of water is  
132 374.14 °C. Therefore, to achieve a high average temperature of heat absorption and  
133 consequently to obtain a high thermal performance, it may be necessary for the steam  
134 generator operating at supercritical pressures. This requires expensive piping and heat  
135 exchanger tubes able to support high pressures. Another undesirable feature related to  
136 water is that the saturation pressure at normal temperature of the condenser is much lower  
137 than atmospheric pressure. As a result, the air can enter the system, requiring the use of  
138 special nozzles in the condenser of feedwater heaters with degassing to remove air.

139 Although water has some inconvenient as working fluid, it doesn't exist any other simple  
140 working fluid more satisfying for the electrical power generation plants. Thereby, the  
141 growing interest in extracting the mechanical energy from low temperature sources has  
142 induced the development of numerous conversion techniques. One of the most promising  
143 is this CDTPC, in which a pump pressurizes the liquid CO<sub>2</sub>, and it is injected in an  
144 evaporator to produce a vapor that is expanded in a turbine connected to a generator;  
145 finally, the exit vapor is condensed, starting the new cycle (Fig. 1).

146 According to the state points shown in the schematic diagram of the simple process in Fig.  
147 1, Fig. 2 presents the CDTPC in a T-s-diagram plotted with [16] data. As an example, an

148 ideal cycle process is shown by segments that are built from the state points 1, 2<sub>is</sub>, 3 and  
149 4<sub>is</sub> marked with (○). The line segment 1-2<sub>is</sub> represents an isentropic expansion with a  
150 production of output work. Heat is extracted from 2<sub>is</sub> to 3 along a constant subcritical  
151 pressure line. Then, an ideal compression of the subcooled liquid from pressure at state  
152 point 3 to state point 4<sub>is</sub> is carried out. Finally, the segment 4<sub>is</sub>-1 represents the heat  
153 addition at constant supercritical pressure to the highest temperature of the cycle at state  
154 point 1.

155 In the evaporator, the fluid temperature is increasing continuously because; being above  
156 the critical point, there is no coexistence between liquid and gas phases. Thereby, fewer  
157 and more uniform differences of temperature for the transcritical cycle will be produced  
158 with respect to the thermal source, causing a considerable reduction of irreversibilities.

159 The previous case, but operating in conditions in which the expansion process, as well as  
160 the compression process, have certain efficiency, i.e., a cycle more closer to the reality, is  
161 represented by the segments built from the state points 1, 2, 3 and 4 marked with (○) in  
162 the same Fig. 2, which are also related to Fig. 1. State point 3 is at the lowest temperature  
163 of the cycle and above the temperature of the heat sink (receiving reservoir). Net input  
164 heat to the cycle occurs from 4 to 1 at constant pressure. Net work output is the difference  
165 between output work from state points 1 to 2 and the input work pump from state points 3  
166 to 4.

167

### 168 **3. Modelling of the process.**

169 The modelling of the process, which allows analyzing the behavior and determining  
170 theoretically the performance of the CDTPC, is presented widely in [11]. However, in this  
171 section and using the first and second law of thermodynamic, it is presented a summary

172 with the main equations, assumptions and conditions used for the theoretical study  
 173 proposed. Thus, the performance of a CDTPC could be evaluated under diverse working  
 174 conditions, assuming constant isentropic efficiencies of 75% for the pump as well as for  
 175 the turbine, steady state conditions and no pressure drop or heat loss in the evaporator,  
 176 condenser or the pipes.

177 The cycle's total energy efficiency is:

$$\eta = \frac{\dot{W}_t - \dot{W}_p}{\dot{Q}_e} \quad (1)$$

178 where  $\dot{W}_t$  is the power out from the turbine;  $\dot{W}_p$  is the power input in the pump defined as:

$$\dot{W}_t = \dot{m} \times (h_1 - h_2) \quad (2)$$

$$\dot{W}_p = \dot{m} \times (h_3 - h_4) \quad (3)$$

179 and the  $\dot{Q}_e$  is the heat input in the evaporator defined as:

$$\dot{Q}_e = \dot{m} \times (h_1 - h_4) \quad (4)$$

180 The exergy efficiency is defined as:

$$\eta_E = 1 - \left( \frac{\sum_i \dot{I}_i}{\sum_i \left( 1 - \frac{T_0}{T_i} \right) \times \dot{Q}_i + \sum_i \dot{E}_{in,i}} \right) \quad (5)$$

181 where  $\dot{I}_i$  is the exergy loss (destruction) of each component  $i$  (evaporator, turbine,  
 182 condenser and pump) that can be found from an exergy balance:

$$\dot{I}_i = \sum_i \left( 1 - \frac{T_0}{T_i} \right) \times \dot{Q}_i + \sum_i \dot{E}_{in,i} - \sum_i \dot{E}_{out,i} - \dot{W}_i \quad (6)$$

183 The term  $\dot{Q}_i$  represents the flow of heat transfer at the location on the boundary where the  
 184 instantaneous temperature absolute is  $T_i$  and the 0 subscripts are relative to the

185 environmental state from which no interaction is possible. Finally, the exergy rate for each  
186 state point is expressed as:

$$\dot{E} = \dot{m}[(h - h_0) - T_0(s - s_0)] \quad (7)$$

187 An inlet temperature of the condensation water  $T_7=15$  °C, dead state  $T_0=15$  °C and a  
188 working fluid condensation temperature  $T_3=25$  °C are considered. Otherwise, a pinch point  
189 of 5 °C is maintained between  $T_3$  and the output temperature of the condensation water  
190 ( $T_8$ ). In the heating process, the temperature  $T_i$  in the high temperature reservoir, i.e. the  
191 waste heat of the heat source, can be treated as a constant heat source at  $T_H$ . In order to  
192 transfer heat, a differential temperature  $\Delta T=20$ ° C is considered and therefore,

$$T_H = T_i + \Delta T_H \quad (8)$$

193 In the condensation process the temperature  $T_i$  is the temperature of the low-temperature  
194 reservoir  $T_L$ . This temperature is considered to be equal to  $T_L = T_7$ .

195 The thermodynamic analysis of the CDTPC was performed using a process simulator  
196 HYSYS® (Hyprotech Co., Canada). The simulation flow diagram is the same as that  
197 presented in Fig. 1.

198

### 199 **3. Results and discussion.**

200 The procedure for analyzing the behavior of the CDTPC was to evaluate the  
201 thermodynamic cycle in terms of net specific work and energy and exergy efficiency, the  
202 behavior of the cycle, for different temperatures: 60, 90, 120 and 150 °C and varying the  
203 inlet pressure to the turbine from 66 bar until the net work was nearly zero or until pressure  
204 and temperature conditions no longer allowed the fluid to be in a gaseous state for  
205 injection to the turbine. These values of temperature are selected with base on typical  
206 temperatures found in different conditions of heat waste at the industry; e.g. wet gas from

207 drying process, hot gas from heating process, waste hot water at textile industry and other  
208 more.

209

### 210 **3.1. Energy analysis.**

211 Results achieved in the simulations carried out are shown in Fig. 3, where the blue  
212 tendency lines and the blue open symbols indicate the energy efficiencies ( $\eta$ ) and the  
213 discontinuos green tendency lines represent the evaporator heat flow ( $\dot{Q}_e$ ) or quantity of  
214 waste heat. On the other hand, in Fig. 4, the red tendency lines represent the net specific  
215 work ( $w_{ne}$ ). Symbols represented with triangle ( $\blacktriangle$ ), square ( $\blacksquare$ ), circle ( $\bullet$ ) and the rhombus  
216 ( $\blacklozenge$ ) are linked with the analyzed temperatures of 150°C, 120°C, 90°C and 60 °C,  
217 respectively.

218 A glance at Figs. 3 and 4 shows a parabola-like behavior and, hence, the existence of a  
219 maximum for both the energy efficiency and the net specific work for the four inlet  
220 temperatures to the turbine. However, it is also appreciated that these maximum points, in  
221 energy efficiency as net specific work are different. The reason for this variation is due to  
222 the different amount of heat flow required in the evaporator ( $\dot{Q}_e$ ) for achieving the inlet  
223 conditions imposed in the turbine.

224 In the same Fig. 3 it is analyzed this behavior for the four inlet temperatures to the turbine  
225 and, as it was expected, the  $\dot{Q}_e$  decreases as the inlet pressure to the turbine increases.  
226 This is because of the rise in the outlet temperature of the pump due to the heat given off  
227 by the pump inefficiencies, achieving thus a higher temperature to the entrance of the  
228 evaporator, which supposes a lower heat transfer requirement in this equipment.

229 Tables 1 and 2 have been included to summarize the results and provide a better  
230 visualization of the information exhibited in previous paragraphs, according to the values

231 presented in Figs. 3 and 4, respectively. That is, Table 1 presents for each one of the four  
232 inlet temperatures to the turbine studied, the point of maximum energy efficiency and net  
233 specific work and the pressure corresponding to this mentioned maximum point of  
234 efficiency. Also, Table 2 shows for each one of the four inlet temperatures to the turbine  
235 studied, the maximum values for the net specific work and the values of energy efficiency  
236 and pressure corresponding to this point of maximum net specific work.

237 From this Fig. 3 and 4, and therefore, from Tables 1 and 2, it is inferred that the benefits  
238 from the inlet temperature of the turbine and the design criteria for the chosen cycle  
239 (maximum energy efficiency, maximum net specific work or a value between both) are  
240 different. A more exhaustive analysis of this appreciation is explained in the following  
241 sections.

242

### 243 **3.1.1. Effect of the inlet temperature to the turbine regarding to the maximum energy** 244 **efficiency.**

245 In Fig. 3 it is observed that for a concrete pressure value, the energy efficiency increases  
246 as the inlet temperature to the turbine increases (a similar behavior can be inferred from  
247 the results in [9]). Considering the maximum value of the energy efficiency obtained (see  
248 Table 1), the effect of rising the inlet temperature to the turbine, from 60 to 150 °C, causes  
249 an increase in the energy efficiency of 5.6% (a change from 2.5% to 8.1%, i.e., 224%  
250 more). For these same maximum points presented in Fig. 3, and comparing with the  
251 results showed for the inlet temperatures to the turbine from Fig. 4, the value of net  
252 specific work increases as well. According to Table 1, this increase is 14.2 kJ/kg (from 3.3  
253 to 17.5 kJ/kg, i.e., 430% more). However, these points which reflect maximum efficiency  
254 energy suppose an increase in the pressure of the system in 77 bar (a change from 95 to

255 172 bar, i.e., 81% more); which can suppose technical problems as well as an increase of  
256 the costs.

### 257 **3.1.2. Effect of the inlet temperature to the turbine regarding the maximum net** 258 **specific work.**

259 In Fig. 4 it is observed as, for other value of pressure and at equal than occurs with the  
260 energy efficiency (Fig. 3), the net specific work increases with the rise of the inlet  
261 temperature to the turbine. Thus, and according to Table 2, if the obtained maximum value  
262 is taken, the effect of increasing the inlet temperature to the turbine, from 60 to 150 °C,  
263 causes a rise in the net specific work of 14.7 kJ/kg (a change from 3.5 to 18.2 kJ/kg, i.e.,  
264 420% more). In these points, the value of the energy efficiency rises 5.3% (from 2.4% to  
265 7.8%, i.e., 218% more). However, these maximum points of net specific work suppose an  
266 increase in the pressure of the system in 60 bar (a change from 90 to 150 bar, i.e., 66%  
267 more). According to previous remarks, the effect of increasing the inlet temperature of the  
268 turbine, whereas it is possible, supposes an enormous increase of the energy efficiency in  
269 the system as well as the net specific work.

270

### 271 **3.2. Exergy analysis.**

272 In this process, the pressure ratios ( $P/P_{critical}$ ), on one hand, must be sufficiently high as for  
273 producing an approach of temperatures as more uniform as possible between the heat  
274 source and the fluid during the heat transfer. On other hand, the pressure should not be  
275 too high to prevent the expansion in the turbine in the two-phase region, with the  
276 consequent deterioration of the latter and the decrease in performance. A fluid such as  
277 CO<sub>2</sub> than allows to work in the supercritical region with significantly lower temperature  
278 values and, additionally, increase the conversion of energy from a more efficient way to

279 use waste heat or renewable as energy sources (reducing, thus, the emission of CO<sub>2</sub> to  
280 the environment).

281 An exergy analysis of the process has been carried out on the basis of the results obtained  
282 from the simulations using both the model and the suppositions and parameters  
283 mentioned in section 2. The procedure used to analyze the behavior of the CDTPC was  
284 the same as that mentioned in section 3.1, whose results were shown in Figs. 3 and 4.  
285 The realization of the process exergy analysis reveals that, contrary to what happens to  
286 energy efficiency, exergy performance ( $\eta_E$ ) has not a maximum at the conditions in that we  
287 had evaluated the cycle, but with the increase of operating pressure of the process, rises  
288 the exergetic performance for all four inlet temperatures to the turbine, as it is shown in  
289 Fig. 5.

290 Figure 5 presents how, unlike what happens with the energy efficiency, the exergy  
291 efficiency has not a maximum, since that with the definition which we had proposed here, if  
292 inlet pressure to the turbine increases, the exergy efficiency also rises, (similar results are  
293 mentioned in [4]).

294 However, it can be concluded that, depending on the turbine inlet temperature and  
295 pressure, there can be differences in the value of the exergy efficiency; hence, they can  
296 condition the design criterion for the obtaining of a maximum energy efficiency or a  
297 maximum net specific work. A more exhaustive analysis of this appreciation is explained in  
298 the following sections.

299

### 300 **3.2.1. Effect of the inlet temperature to the turbine on the exergy efficiency.**

301 It can be seen in Fig. 5, that for a specific pressure, the rise in the inlet temperature to the  
302 turbine causes a decrease of the exergy efficiency of the cycle as a result of the increase

303 of irreversibility due to the rise in heat flow required. For instance, at a pressure of 150 bar,  
304 and two different turbine inlet temperatures of 120 °C and 150 °C, the exergy efficiency  
305 decreases by 10% (a change from 40% to 36%, respectively).

### 306 **3.2.2. Effect of the inlet pressure to the turbine on the exergy efficiency.**

307 When a high discharge pressure is imposed on a pump (and therefore on the turbine inlet),  
308 the output temperature of the work fluid rises, causing a decrease in the irreversibility by  
309 heat flow in the evaporator, as the temperature of this fluid approaches to the heat source.  
310 Hence, a rise of the inlet pressure to the turbine causes an increase in the exergy  
311 efficiency, as presented in Fig. 5. Therefore, the increase in the inlet pressure to the  
312 turbine makes to rise the exergy performance asymptotically (above 50% as maximum for  
313 temperatures of 90, 120 and 150 °C, while for the temperature of 60 °C is limited by its  
314 maximum operating pressure to 40%).

315 Nevertheless, a decrease in the inlet temperature to the turbine causes a decrease in the  
316 sensitivity of the process in relation with the exergy efficiency. In other words, the lower the  
317 inlet temperature to the turbine, the lower the exergy performance gains for a slight  
318 increase in pressure. This effect evidently decreases whenever it approaches the value of  
319 its asymptote in each case. For instance, an increase of 20 bar (from 80 to 100 bar) and  
320 for the temperature of 150 °C, causes an increase in the exergy efficiency of 110% (a  
321 change from 10% to 21%). While the same increase of pressure for the temperature of 90  
322 °C produces an increase of 87% (a change from 15% to 28%).

### 323 **3.2.3. Irreversibilities of the process in each device.**

324 Figure 6 presents the effects of the inlet pressure to the turbine over the irreversibilities of  
325 each one of process devices for the turbine inlet temperature at 150 °C. Due to a similar  
326 behavior of the rest of the temperatures evaluated, only the results for this inlet  
327 temperature are represented.

328 Furthermore, Fig. 6 shows that when increases the inlet pressure turbine, the irreversibility  
329 of the heat flow decreases in the evaporator, as well as in the condenser and it increases  
330 at the turbine and pump; therefore we will have the conditions with which the total effects  
331 cause a maximum in exergy efficiency. The explanation for this is related to the rise in the  
332 output temperature of the fluid in the pump when a higher discharge pressure is imposed  
333 on the pump (and therefore on the inlet pressure to the turbine). This causes the  
334 irreversibility by heat flow in the evaporator to decrease when the temperature of the fluid  
335 approaches the temperature of the heat source (a hypothesis in keeping with that  
336 explained in [17]). The same happens with respect to the condenser when a lower  
337 discharge temperature is produced. However, the increase of the exergy destruction by  
338 work is less than that of these exchangers, and hence the total exergy destruction  
339 decreases in line with the increase in the inlet pressure to the turbine, being more  
340 appreciable at pressures below 150 bar, as it is showed in the same Fig. 6.

341

### 342 **3.3. Optimum conditions of design.**

343 Optimum conditions for the design have been considered taken into account the results  
344 presented in the previous section, these optimum points selected linked with the mean  
345 values located between the maximums of the energy efficiency and the net specific work  
346 for each of the temperatures studied. Table 3 compiles these results where the values of  
347 net specific work and the energy and exergy efficiency corresponding to this optimum  
348 pressure point. The fact of considering mean values supposes a drop of the energy  
349 efficiency of 0.15% (equivalent to 2.3%) when is compared with the maximum values  
350 whereas for the case of net specific work, a decrease of only 0.3 kJ/kg as maximum (also  
351 equivalent to only 2.3%). On the other hand, the exergy efficiency is always increasing, so  
352 that taking into account a mean design point, it is influenced in a variation (decrease or  
353 increase) of around 2% as maximum (equivalent to 6%), depending on the variable which

354 it is compared ( $\eta$  or  $wne$ ). This means that the exergy efficiency drops when is related with  
355 the one obtained with the point of maximum energy efficiency and it increases if it is  
356 compared with the point of maximum net specific work obtained.

357 Figure 7, provides for the four inlet temperatures to the turbine studied, the percentage of  
358 the irreversibilities of each of the devices that make up the cycle of the process proposed  
359 in the optimum operating conditions suggested (midpoint between the maximus of energy  
360 efficiency and net specific work). In general lines, it can be inferred of this figure which was  
361 discussed in section 3.2.2, i.e, a decrease in the inlet temperature to the turbine causes a  
362 decrease in the sensitivity of the process in relation with the exergy efficiency. In other  
363 words, the lower the inlet temperature to the turbine, the lower the exergy yield increases  
364 (mainly due to a larger percentage of irreversibilities in the evaporator). Additionally, it is  
365 interesting to note in this Fig. 7, the proportion of participation of the irreversibilities of each  
366 one of the devices on the proposed process, which occurs mainly in the evaporator,  
367 followed by the condenser and in a lesser way, by the turbine and pump (the  
368 irreversibilities of the pump are less than half related to the turbine).

369

## 370 **Conclusions.**

371 The CDTPC are suitable to be used in heat waste recovery at the industry, which permits  
372 to take advantage of hot streams that are wasted to atmosphere. It is possible to produce  
373 power from heat waste at low temperature (e.g. 60 °C), like those occurred in drying  
374 process. The technology is simple, compact and easy enough to be transported from one  
375 point to other and it is recommendable to select the operation conditions of CDTPC with  
376 base on the criterion of maximum work generated instead of maximum energy efficiency.

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378

379

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385

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435

**TABLES.**

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*Table 1. Main results obtained at maximum energy efficiency conditions.*

Temperature, $T_1$ (°C)	Parameter		
	Pressure, $P_1$	$\eta_{max}$	$wne$
	(bar)	(%)	(kJ/kg)
150	172.0	8.1	17.5
120	145.0	6.5	12.0
90	120.0	4.6	7.4
60	95.0	2.5	3.3

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*Table 2. Main results obtained at maximum net specific work conditions.*

Temperature, $T_1$ (°C)	Parameter		
	Pressure, $P_1$	$\eta$	$wne_{max}$
	(bar)	(%)	(kJ/kg)
150	150	7.8	18.2
120	128	6.2	12.8
90	108	4.4	7.8
60	90	2.4	3.5

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Table 3. Optimum conditions of design.

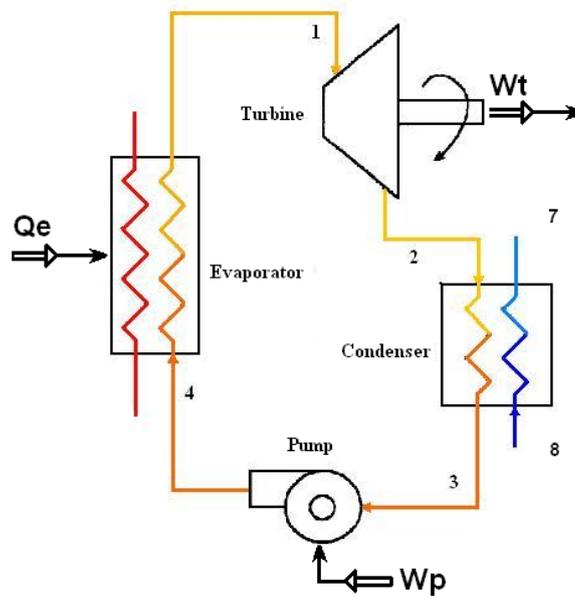
Temperature, $T_1$ (°C)	Parameter			
	Pressure, $P_1$ (bar)	$\eta$ (%)	$\eta_E$ (%)	$w_{ne}$ (kJ/kg)
150	161.0	8.0	38	18
120	136.5	6.4	36	12.5
90	114.0	4.5	34	7.6
60	92.5	2.5	30	3.4

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# FIGURES.

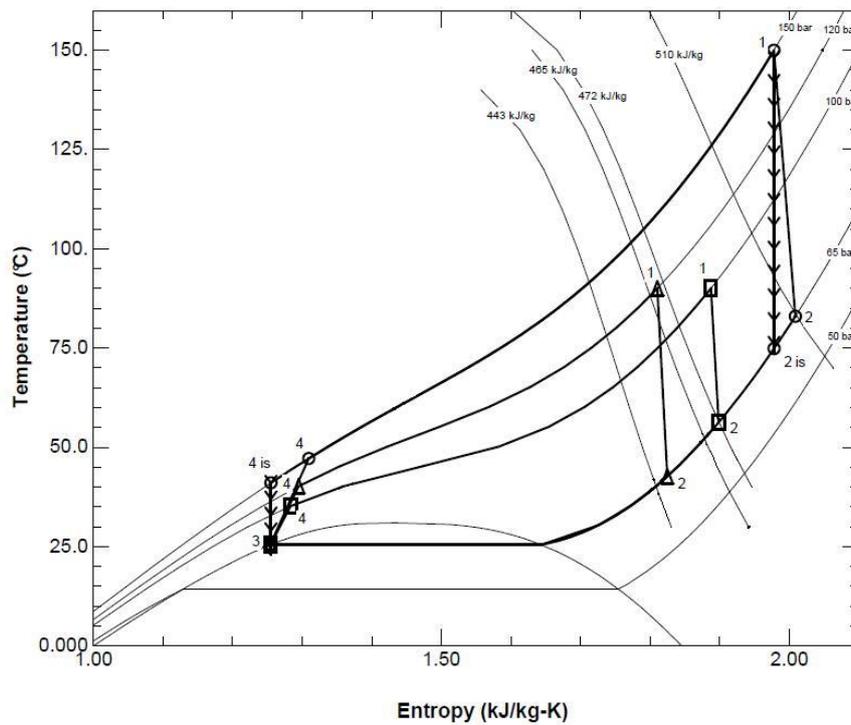


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Fig. 1. Schematics diagram of the process.

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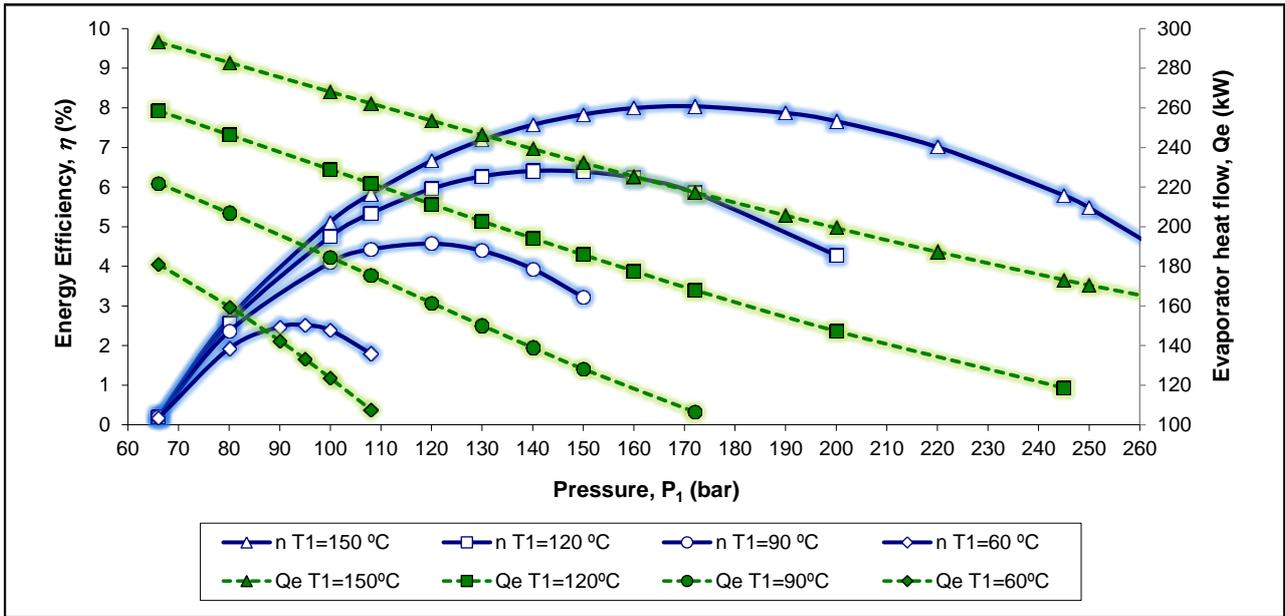


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Fig. 2. T-s Diagram for different CO<sub>2</sub> transcritical power cycles.

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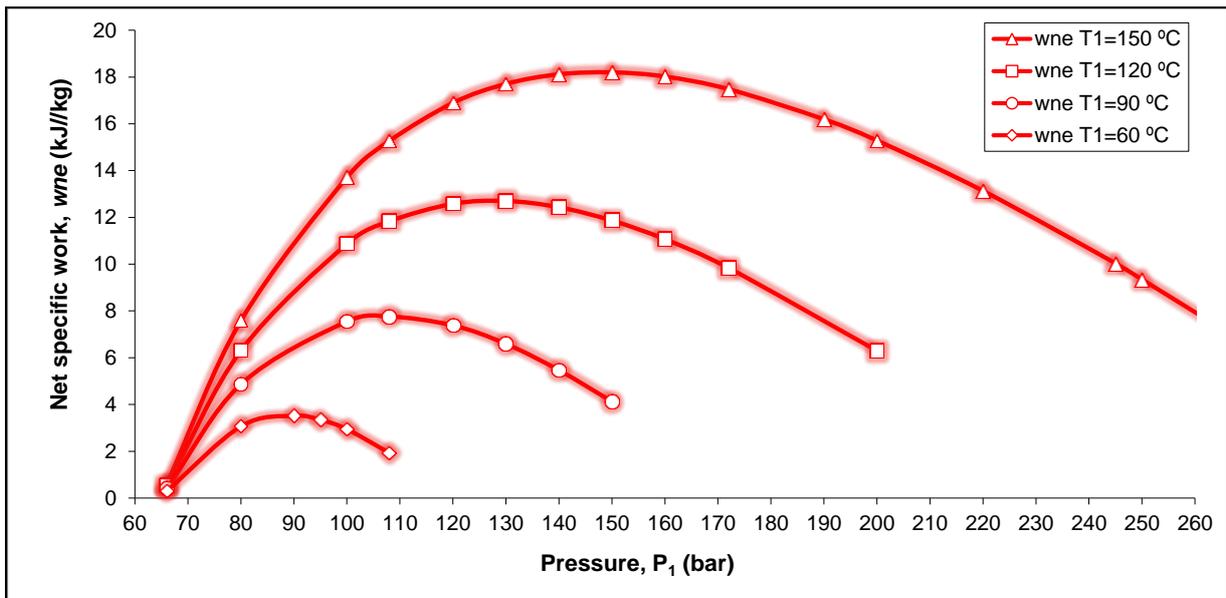


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456 *Fig. 3. Energy efficiency (open symbols) and heat flow required in the evaporator (bold*  
 457 *symbols) vs. Pressure  $P_1$  for  $T_1= 150$  °C (triangle),  $120$  °C (square),  $90$  °C (circle) and  $60$*   
 458 *°C (rhombus).*

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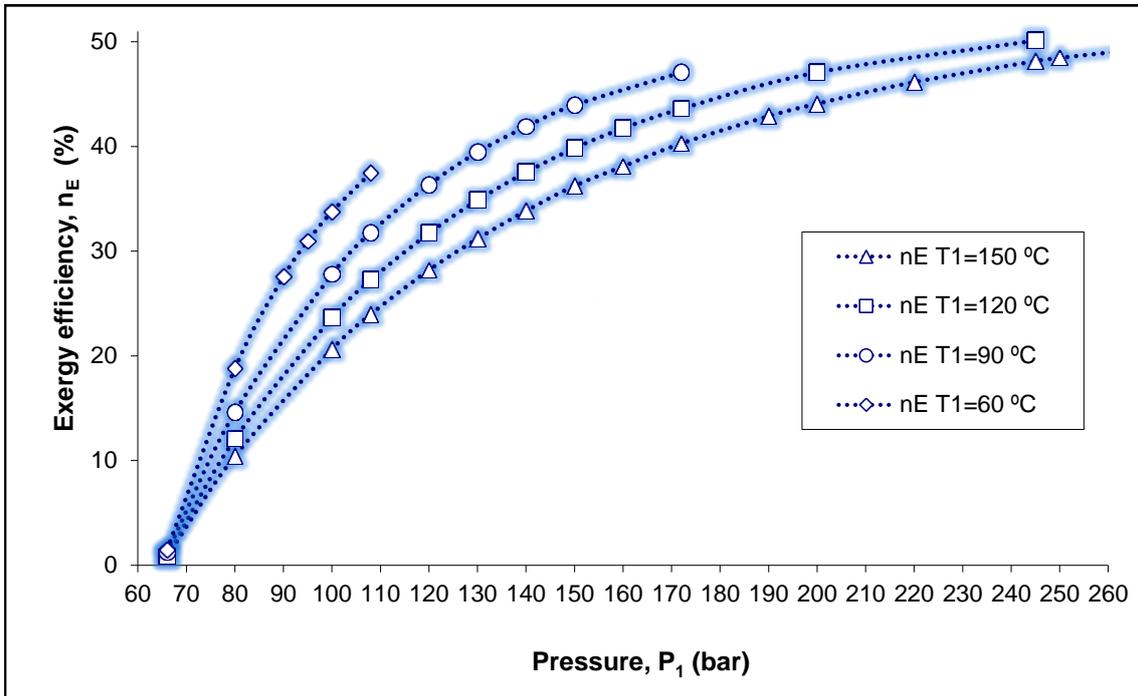


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462 *Fig. 4. Net specific work ( $w_{ne}$ ) vs. Pressure  $P_1$  for  $T_1= 150$  °C (triangle),  $120$  °C (square),*  
 463  *$90$  °C (circle) and  $60$  °C (rhombus).*

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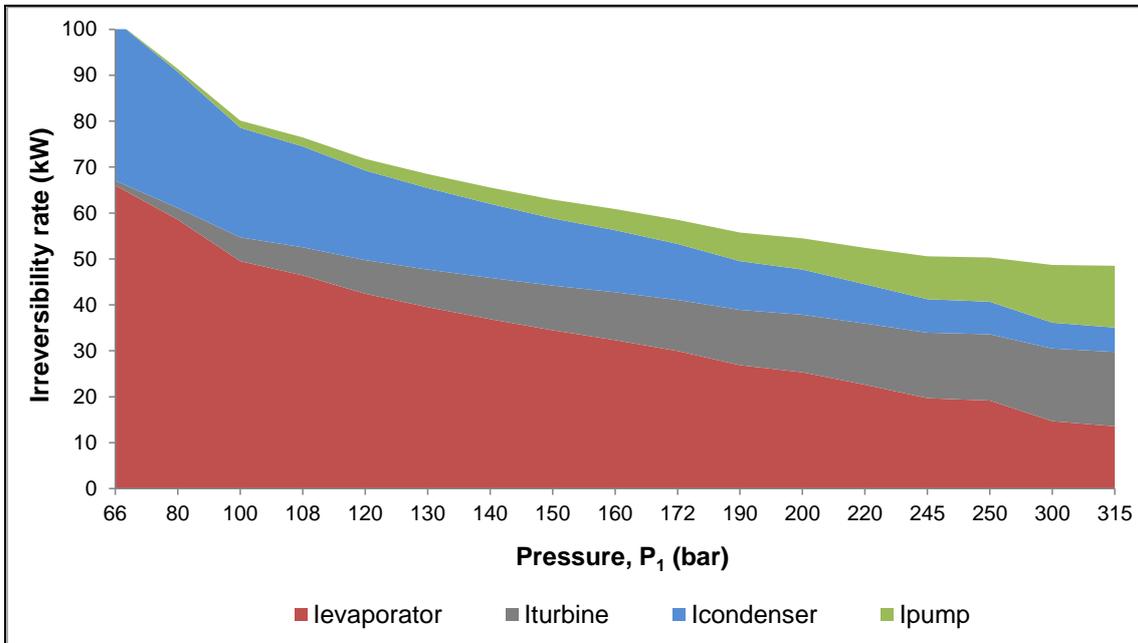


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Fig. 5. Exergy efficiency vs Pressure  $P_1$  for the studied temperatures.

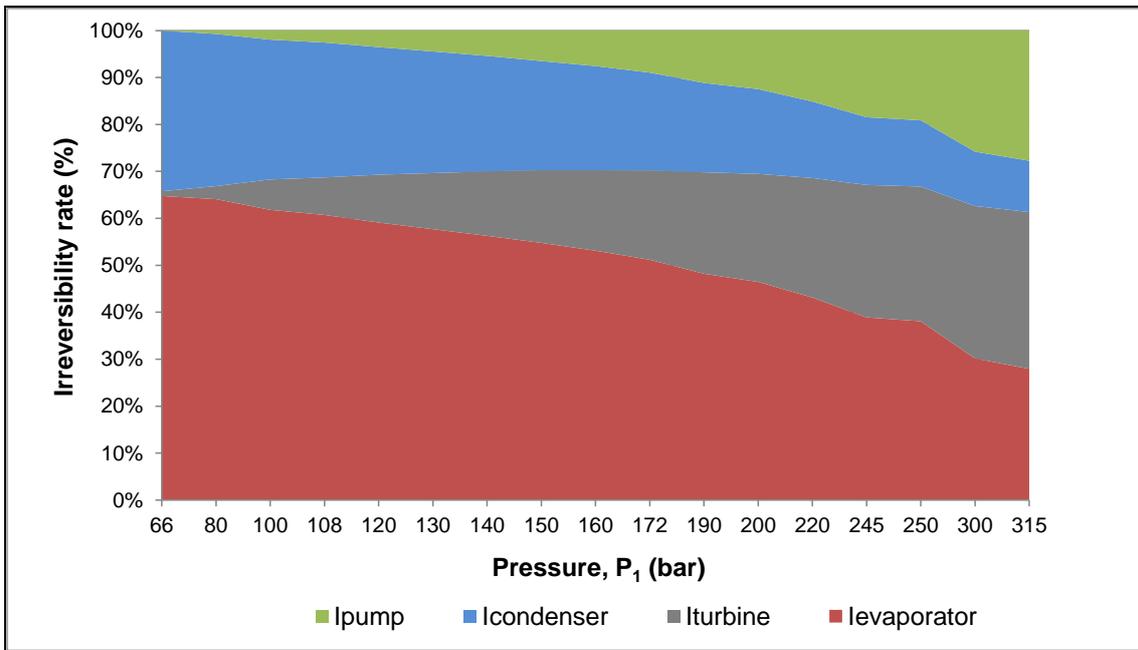
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a.



b.

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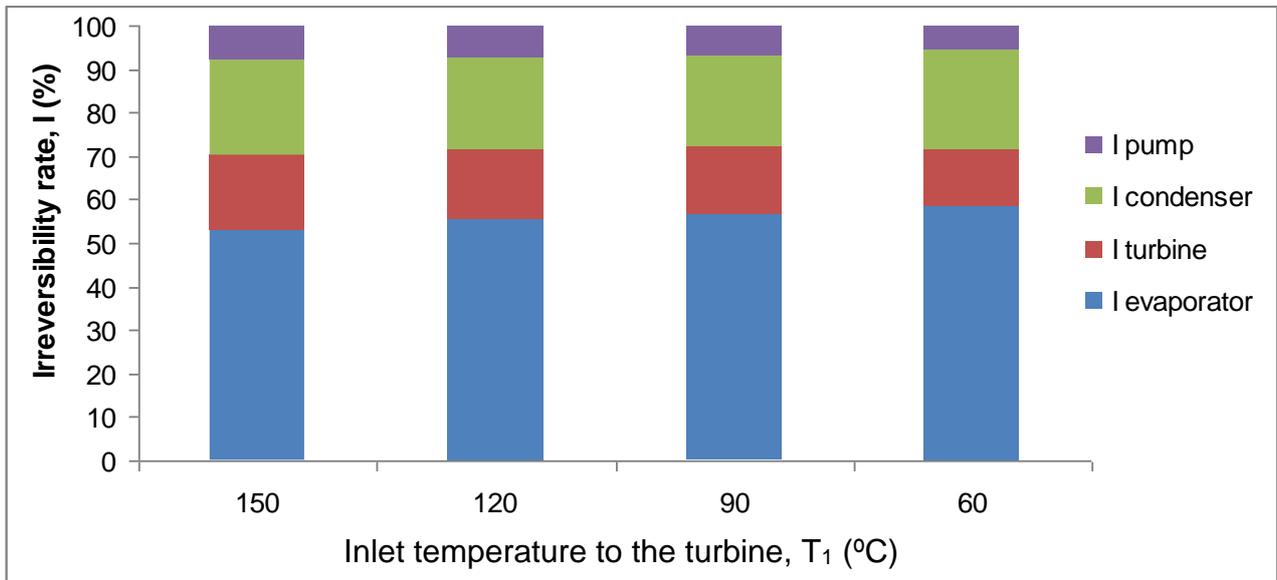
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Fig. 6. Effect of the inlet pressure to the turbine over the irreversibilities in kW (a) and percentage (b) of the process in an inlet temperature to the turbine at 150 °C.

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Fig. 7. Irreversibilities of the process in optimum conditions of design for the studied temperatures.

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