

1 **Annual and seasonal cycles of CO₂ and CH₄ in a Mediterranean Spanish**
2 **environment using different kernel functions**

3
4 **Concise title: CO₂ and CH₄ cycles in a Mediterranean environment**

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21 **Abstract**

22 This paper is based on CO₂ and CH₄ semi-hourly mole fraction measurements obtained
23 at the Low Atmosphere Research Centre (CIB) between 2010 and 2016 using a Picarro
24 G1301 analyser. The main aims of the study were to examine the temporal variation of
25 CO₂ and CH₄ by using six different kernel functions, and to study the suitability of
26 these functions to the dataset. The method used for the current study was based on
27 experimental contour plots of R² values in order to simultaneously determine the
28 bandwidths of kernel functions for the long-term and short-term. An Epanechnikov, a
29 Gaussian, a biweight, a triangular, a tricubic and a rectangular kernel function were
30 applied to extract the salient features of both the long-term (trend) and the short-term
31 (seasonality). The average linear increase growth rates found were mainly attributed to
32 the terrestrial biosphere cycle and changes in the atmospheric circulation regime. The
33 seasonal cycle exhibited a cyclical variation, revealing summer minima for both gases,
34 which may be explained by a biological minimum. Kernel analysis showed two
35 nocturnal CO₂ maxima, in spring and autumn, linked to an increase in rainfall. For CO₂
36 daytime records, only the spring peak was detected. As regards CH₄, the maximum
37 was located in winter. The best fit for the trend was obtained by the biweight kernel. In
38 contrast, the best adjustment for seasonality was achieved from the Gaussian and the
39 triangular kernel. To sum up, optimal bandwidth selection is important when kernel
40 regression functions are employed. Since no important differences were found between
41 the kernels employed, those which involve least computational effort are
42 recommended.

43 **Key words:** trend; seasonal cycle; rural; kernel functions; bandwidth; contour plot

44 **1 Introduction**

45 CO₂ and CH₄ are the two most important long-lived greenhouse gases in the atmosphere
46 that are controlled by the Kyoto Protocol. According to the IPCC (2013) report,
47 radiative forcing of 2.62 W m⁻² is caused by the sum of CO₂ and CH₄ emissions. The
48 rise in CO₂ and CH₄ mole fractions is contributing to increasing radiative forcing, a
49 measure of the change in the total radiative flux at the tropopause due to a rise in the
50 amount of greenhouse gases in the atmosphere (IPCC 2014). Estimating the distribution
51 of both gases over time is crucial vis-à-vis understanding the processes that govern their
52 cycles, forecasting future trends and, therefore, planning effective CO₂ and CH₄
53 mitigation policies and strategies (Artuso et al. 2009; Wu et al. 2012).

54 High-precision and continuous measurements of greenhouse gases in the atmosphere
55 were initiated in 1958 by Charles Keeling, who began measuring atmospheric CO₂ at
56 the Mauna Loa Observatory, Hawaii (Keeling 1960). Systematic worldwide
57 measurements of tropospheric CH₄ began in 1978 (Blake et al. 1982; Dlugokencky et al.
58 1994; Rasmussen et al. 1981). Greenhouse gas observations are currently supported on
59 a global scale by international databases such as the World Data Centre for Greenhouse
60 Gases (WDCGG) and the National Oceanic and Atmospheric Administration (NOAA),
61 among others (Pérez et al. 2016; 2017). However, observations are still lacking in some
62 areas of the world, especially in rural sites in the Mediterranean basin (Artuso et al.
63 2009). The present study is motivated by the importance of gaining better insights into
64 CO₂ and CH₄ behaviour in a Mediterranean rural area of the Iberian Peninsula.

65 From a biogeochemical point of view, three processes dominate the turnover of
66 atmospheric CO₂. These are the exchange of atmospheric CO₂ with terrestrial

67 ecosystems, the exchange of atmospheric CO₂ with the oceans and the emissions of CO₂
68 into the atmosphere from anthropogenic activities (Zhu and Yoshikawa-Inoue 2015)
69 such as fossil fuel use and industry (9.4 ± 0.5 Gt C year⁻¹ during 2007-2016) (Le Quéré
70 et al. 2018) or land use change (1.3 ± 0.7 Gt C year⁻¹ during 2007-2016) (Le Quéré et al.
71 2018). It is also important to point to photosynthesis (3.0 ± 0.86 Gt C year⁻¹ during
72 2007-2016) (Le Quéré et al. 2018) and oceans (2.4 ± 0.5 Gt C year⁻¹ during 2007-2016)
73 (Le Quéré et al. 2018) as being mainly responsible for CO₂ removal.

74 The main CH₄ sources estimated for the period 2003-2012 by the Global Methane
75 Budget (Saunois et al. 2016) were fossil fuel (121 Tg CH₄ year⁻¹), enteric fermentation
76 and manure (106 Tg CH₄ year⁻¹), landfills and waste water management (59 Tg CH₄
77 year⁻¹) as well as biomass and biofuel burning (30 Tg CH₄ year⁻¹). In contrast, the major
78 CH₄ sink is oxidation by OH radicals (454-617 Tg CH₄ year⁻¹) (Saunois et al. 2016),
79 especially in the tropical mid-troposphere, according to Nisbet et al. (2014). Minor sinks
80 include soil oxidation (9-47 Tg CH₄ year⁻¹), and reactions in the stratosphere (16-84 Tg
81 CH₄ year⁻¹) (Saunois et al. 2016).

82 Over the last few decades, the scientific community has focused its attention on
83 assessing temporal variability in an effort to quantify the magnitude and rate of
84 greenhouse gas sources and sinks. Atmospheric time variability, which comprise a long-
85 term (trend) and a short-term (seasonality) series, consist of regular observations made
86 at discrete time intervals. Decomposing series into their constituent parts involves
87 fitting mathematical functions to the data (Pickers and Manning 2015). This paper
88 focuses on applying kernel regression to decompose a CO₂ and CH₄ dataset.

89 Kernel regression is a non-parametric technique that locates and separates precise peaks
90 that are close to one other, while producing simple graphical output (Donnelly et al.

91 2011). Rather than assuming a parametric form, a smooth regression function is
92 assumed and the relationship between two variables can be summarized, thus giving a
93 more accurate estimation at the expense of substantially increased computational effort
94 (Donnelly et al. 2011).

95 Many authors have employed kernel functions to locate (e.g., Henry et al. 2002),
96 identify (e.g., Kim and Hopke 2004) and separate (e.g., Henry et al. 2011) sources of air
97 pollution by relating wind direction to measured mole fractions. Yu et al. (2004)
98 extended the approach adopted by Henry et al. (2002) to incorporate wind speed into the
99 analysis, quantifying the impact of local sources. Donnelly et al. (2011; 2012) followed
100 the analysis by Yu et al. (2004) to quantify the variation of NO₂ mole fractions at three
101 background Irish sites with wind direction and wind speed. Henry (2008) and Henry et
102 al. (2009) determined the impact of sources using short-time average air quality and
103 wind data in an extension of the methodology proposed by Henry et al. (2002) and Yu
104 et al. (2004). Kernel regressions have already been applied at the CIB station to provide
105 the CO₂ daily cycle taking into account pairs of circular variables such as wind direction
106 and time (Pérez et al. 2013). Said authors also explored the trajectories reaching the
107 northern plateau of the Iberian Peninsula employing kernel regressions (Pérez et al.
108 2015) and investigated point and linear sources of air pollution in the area (Pérez et al.
109 2016). However, most of these studies involving the application of kernel functions on
110 time series of trace gases rely on the two most common functions: the Gaussian and the
111 Epanechnikov. Hence, it is not known whether other functions may prove more suitable
112 for fitting the data and expressing the salient features of the time series. As stated by
113 Nakazawa et al. (1997), assessing a time series using one kernel function might be
114 different from that derived using the same data but a different kernel function.

115 Bearing this in mind, the current paper involves two complementary parts. The first
116 seeks to determine the suitable bandwidths given a kernel function by using a novel
117 methodology based on contour plots. The second is devoted to showing how six
118 different kernel functions, whose application has been more restricted in atmospheric
119 time series up to date, can be used to characterize the evolution of CO₂ and CH₄ in
120 terms of trend, average growth rate and seasonal cycle.

121

122 **2 Materials and methods**

123 **2.1 Experimental site**

124 The measurement campaign extended over five and a half years (15 October 2010 to 29
125 February 2016). Measurements were recorded at the Low Atmosphere Research Centre
126 (CIB) (lat: 41°48'49"N, long: 4°55'59"W, alt: 845 m). The monitoring station is located
127 at the centre of an extensive plateau in a Mediterranean rural area of Spain, near the
128 cities of Valladolid (24 km to the southeast) and Palencia (40 km to the northeast).

129 Croplands, coniferous trees and Mediterranean shrubs provide the main vegetation
130 covering the area. There are no important orographic reliefs near the site. Thus,
131 horizontal homogeneity can be assumed. A typical Mediterranean climate prevails in the
132 study site with a mean annual temperature of 12.6 °C and a mean annual rainfall of
133 around 450 mm with an evenly distributed pattern throughout the year, peaking in
134 spring and autumn (Sánchez et al. 2014).

135 **2.2 Data acquisition**

136 CO₂ and CH₄ mole fractions were routinely collected by a Cavity Ring-Down
137 Spectrometer (Picarro G1301 analyser) and averaged in half-hour intervals. This
138 analyser is based on optical technology in which direct measurement of infrared
139 absorption loss in a sample cell is used to quantify the mole fraction of a gas. Laser light
140 is directed into an optical resonator (the optical cavity) consisting of three highly
141 reflective mirrors, serving as a compact flow cell with an effective optical path length of
142 around 20 km. This long path allows for high precision measurements (Rella et al.
143 2013). The technique is described in greater detail by Crosson (2008) and Rella et al.
144 (2013).

145 The analyser was calibrated fortnightly with three NOAA standards, and mole fractions
146 were corrected slightly. Measurements were taken at three heights, 1.8, 3.7 and 8.3 m.
147 Only the highest level was used in this paper, since mole fractions changes are more
148 stable (Pérez et al. 2012).

149 The data series was divided into two periods: daytime and night-time, defined by the
150 hourly evolution (GMT hour) obtained from the National Geographic Institute of Spain.
151 The availability of a large database with scant gaps is a key point in this paper.

152 **2.3 Kernel regression method: theoretical concepts**

153 To define the temporal patterns of CO₂ and CH₄, we used kernel regression to extract
154 the trend and the seasonal component. The following subsections introduce the method.

155 **2.3.1 Kernel functions**

156 The fitting function used to calculate the average smoothed mole fractions, \bar{y} , expressed
 157 in ppm for CO₂ and ppb for CH₄, is defined by the following expression proposed by
 158 Henry et al. (2002):

$$159 \quad \bar{y}(t, h) = \frac{\sum_{i=1}^N K\left(\frac{t-t_i}{h}\right) y_i}{\sum_{i=1}^N K\left(\frac{t-t_i}{h}\right)} \quad (1)$$

160 where t is the time expressed in days, h is the bandwidth expressed in days, N is the
 161 number of observations, K is the kernel function, and y_i is the mole fraction (expressed
 162 in ppm for CO₂ and ppb for CH₄) in a time period t_i expressed in days.

163 Greater weight is given to mole fractions y_i observed at times t_i closer to time t where
 164 the average mole fraction $\bar{y}(t, h)$ is calculated, and less weight is attached to distant
 165 observations, following Eq. (1).

166 This paper seeks to analyse the six smoothing kernel functions listed in Table 1.

167 **Table 1** Kernel functions employed in the study.

Kernel function	^a K(u)	Support [u for which K(u) > 0]	Efficiency
Epanechnikov	(3/4) (1-u ²)	-1 < u < 1	1.0000
Biweight	(15/16) (1-u ²) ²	-1 < u < 1	0.9939
Gaussian	(2π) ^{-1/2} exp (- 0.5u ²)	-∞ < u < ∞	0.9512
Rectangular	1/2	-1 < u < 1	0.9295
Triangular	1 - u	-1 < u < 1	0.9859
Tricubic	(70/81) (1 - u ³) ³	-1 < u < 1	0.9870

168 ^au= [(t-t_i)/h]

170 2.3.2 Bandwidth (h)

171 The most important decision in kernel regression is choosing the bandwidth, h . The
172 different methods for determining its value aim to balance two counteracting measures,
173 the bias (increases for large h values) and the variance (increases for small h values) (de
174 Haan 1999). There are two main lines of research in the literature for determining
175 bandwidth: one focuses on mathematical procedures and the other is based on
176 experimentation, bearing in mind the characteristics of the dataset. For the first line of
177 research, there is abundant literature (e.g., Hall and Kang 2005; Härdle 1993; Harrold et
178 al. 2001; Scott 1992; Silverman 1998). The second line of research is, however, much
179 poorer in terms of the literature. Authors such as Nicolich and Jorgensen (2008) suggest
180 experimenting with the bandwidth as the best method to determine its value (Donnelly
181 et al. 2011). For exploratory analysis, a trial and error approach is also recommended
182 (Wilks 2006).

183 The current paper follows the second line of research since the mathematical procedures
184 found in the literature determine only one bandwidth while two different bandwidths are
185 needed to express the trend and seasonal evolution of the dataset. We provide a quick
186 and easy method by depicting contour plots to determine the suitable bandwidths of a
187 kernel function. This is an important strength of the proposed method given the
188 decrease in the required computational effort, and which may have applications in other
189 studies. The Epanechnikov function was used in this part of the study due to its
190 simplicity.

191 Graven et al. (2012) considered a cut-off period of 24 months to detrend the data, while
192 Pérez et al. (2017) employed a bandwidth of 1000 days to detrend the data, producing
193 graphical outputs without oscillations. Both references as well as other combinations of
194 training sets were taken into account when establishing the suitable bandwidth for CO₂
195 and CH₄.

196 Two different bandwidths were used; $h1$ to quantify the data trend and $h2$ to express the
197 seasonal component. Large $h1$ values combined with small $h2$ values and vice-versa, as
198 well as intermediate values of both bandwidths were analysed. Bandwidth values
199 ranged between 100 and 1000 days (with intervals of 100 days) for $h1$ and in the range
200 of 20 days to 160 days for $h2$, with intervals of 20 days from level to level. R² values
201 between experimental mole fractions and model measurements were obtained for each
202 bandwidth combination and depicted in contour maps, inspection of which would
203 determine the selection of specific $h1$ and $h2$ values.

204 By using R² values as the statistic to determine the bandwidths, the arbitrariness of the
205 method is substantially reduced. When the lines are close to one another, they reflect
206 major changes in R² values. In contrast, when they are further apart, the change is more
207 gradual, and R² values are more stable within this region. Hence, the $h1$ and $h2$ values
208 were chosen depending on the trend change (i.e. inflection point), defined as the region
209 in which lines change from being closer to one another to being further apart. Thus, the
210 inflection point was established in the region where the contour lines are further apart,
211 indicating stable R² values. According to this method, a region of possible bandwidth
212 combination could be suggested rather than a single unique point. Other authors, such as
213 Rodríguez-Cortés et al. (2015), also considered an interval of optimal bandwidth values
214 after testing different bandwidth combinations. Due to the narrow interval calculation

215 for $h1$ (100 days) and $h2$ (20 days), no major changes would be expected for alternative
216 surrounding $h1$ and $h2$ values. Thus, intermediate values for $h1$ and $h2$ within the region
217 where R^2 values barely change were chosen. Likewise, Grange et al. (2016) reported
218 that within a central range the final output is quite insensitive to the scaling values.
219 According to de Haan (1999), when an optimal bandwidth has been chosen for one type
220 of kernel function, the same bandwidth for other kernels will show similar smoothing
221 characteristics, and it is possible to switch between kernels without reconsidering the
222 optimal bandwidth. Thus, once the bandwidth was established, six different kernel
223 functions were applied to the dataset in order to analyse the salient features of the trend
224 and the seasonal component and to analyse the data adjustment of each kernel.

225 **2.3.3 Calculation procedure**

226 Our time series has few missing data. The procedure used was based on Pickers and
227 Manning (2015). First, the trend of the experimental data is calculated by applying the
228 kernel function with a wide bandwidth, $h1$. Second, observations were detrended by
229 subtracting the previously calculated trend from the whole time series. Third, the
230 seasonal component obtained from the second step was smoothed by a kernel function,
231 K , using a narrow bandwidth, $h2$, expressing seasonal changes. Finally, the seasonal
232 cycle was subtracted from the original observations in a deseasonalised process, and the
233 resulting series was again smoothed with the initial bandwidth, $h1$. Additionally, the
234 average growth rate was obtained, expressing the trend change over time.

235 The Gaussian kernel is computationally slower than the other kernel functions both
236 because of the exponential function calls, and because its infinite support leads to all
237 data values contributing to the smoothed estimate (Wilks 2006). For the Gaussian
238 kernel, observations in the range of $(-1,1)$ receive a weight between 0.4-0.2, while

239 observations in the range of (-3,3) decrease their statistical weight to 0.0039, and are
240 virtually 0 for the remaining data observations (Casas 2010). For this reason, the
241 interval calculation was shortened to (-3,3) and (-1,1) intervals, making the Gaussian
242 function more flexible in order to decrease the computational effort without losing
243 accuracy in data fitting. R^2 values were used as the goodness of fit indicator to compare
244 and analyse the efficacy of the kernel functions.

245 **2.4 Statistics**

246 Some of the most important statistics were determined for the data trend, since they
247 report valuable information about their evolution over the study period. The statistics
248 used here were classified into location, spread, symmetry and peakedness measures.

249 **2.4.1 Location**

250 Location statistics report information concerning the central tendency (Wilks 2006).
251 The mean (non-robust) and the median (robust) were used, since they are widely
252 employed in other environmental studies.

253 **2.4.2 Spread**

254 Spread measures indicate the dispersion or degree of variation around the central value
255 (Wilks 2006). The standard deviation, minimum and maximum value were used as non-
256 robust statistics. As a robust statistic, the interquartile range, the difference between the
257 upper ($Q_{0.75}$) and lower ($Q_{0.25}$) quartile, was calculated.

258 **2.4.3 Symmetry**

259 Symmetry measures describe data distribution around their centre (Wilks 2006). In this
260 paper, the skewness (non-robust) and the Yule-Kendall index (robust) were used to
261 describe data symmetry. The Yule-Kendall index is defined as follows (Wilks 2006):

$$262 \text{ Yule Kendall index} = (Q_{0.25} - 2Q_{0.5} + Q_{0.75})/IQ \quad (2)$$

263 where $Q_{0.25}$, $Q_{0.5}$ and $Q_{0.75}$ are the lower quartile, the median, and the upper quartile
264 respectively. IQ represents the interquartile range.

265 **2.4.4 Peakedness**

266 Peakedness expresses data concentration around the central value (Khurshid et al.
267 2007). The Kurtosis statistic has been widely employed to analyse the peakedness of a
268 univariate probability distribution (Khurshid et al. 2007). Here we use the standard
269 kurtosis (non-robust) and the robust kurtosis based on Sachs' (1978) definition, which is
270 as follows:

$$271 \text{ Robust Kurtosis} = (Q_{0.75} - Q_{0.25}) / (2(DZ_9 - DZ_1)) \quad (3)$$

272 where $Q_{0.75}$ and $Q_{0.25}$ are the upper and lower quartile respectively, while DZ_9 and DZ_1
273 refer to the 9th and the 1st decile mole fraction value (expressed in ppm for CO₂ and ppb
274 for CH₄).

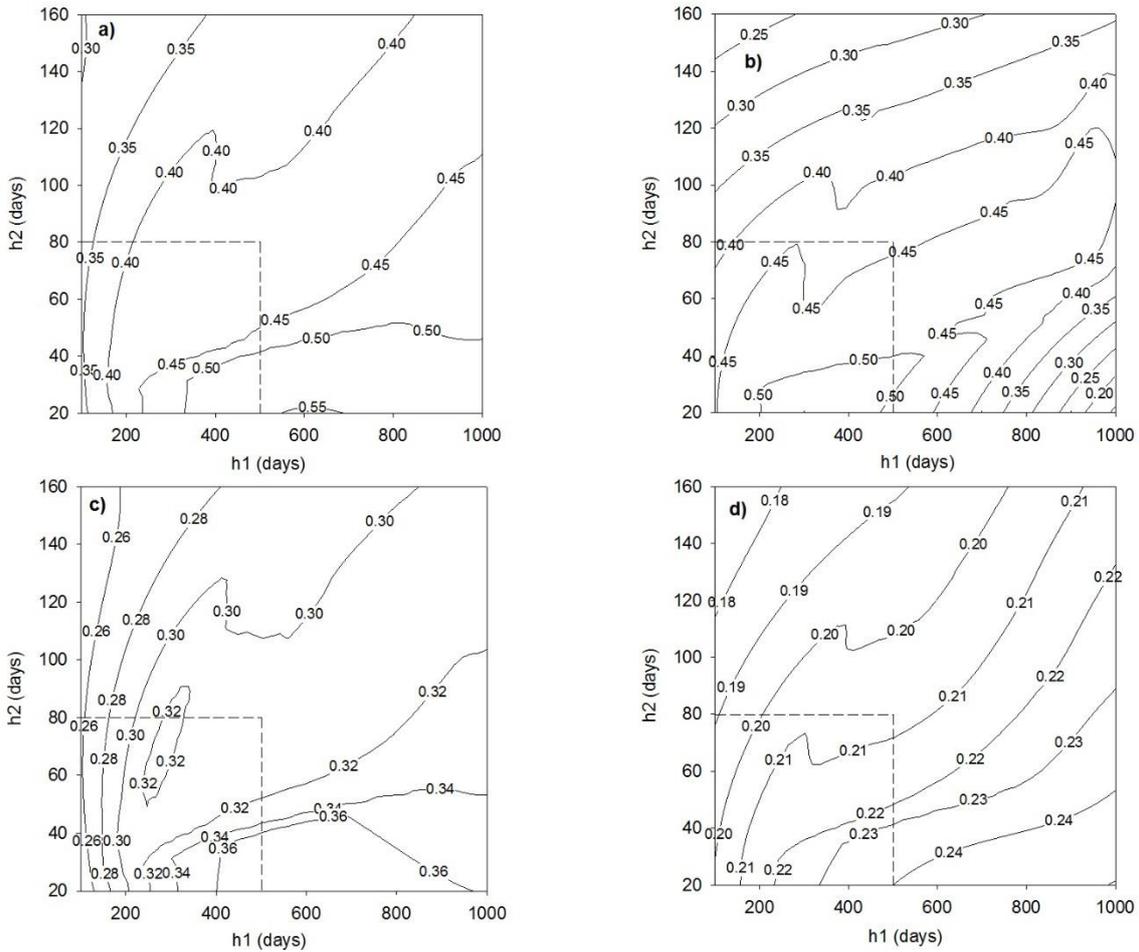
275

276 **3 Results and discussion**

277 **3.1 Bandwidth choice**

278 Figure 1 presents the contour plots following the procedure described in Section 2.3.2.
279 As a result, the inflexion point for our dataset was established by choosing a 500-day
280 bandwidth for $h1$ and 80 days for $h2$ (Fig. 1). The $h1$ and $h2$ values proposed here seem
281 to be reasonable since $h1$ is around one and a half years which, according to Barlow et
282 al. (2015), is a good indicator to express growth rate, and $h2$ (80 days) virtually
283 represents one whole season. These values agree fairly well with the results of Pérez et
284 al. (2017), who considered a bandwidth of 500 days for $h1$ and 60 days for $h2$. The

285 same bandwidth was proposed for the four scenarios so as to simplify subsequent
 286 subsections, allowing comparisons of the outcomes in similar conditions. Furthermore,
 287 large values of h result in smoother shapes suppressing details of the time series, while
 288 small values result in more irregular shapes dominated by noise or large peaks, making
 289 it difficult to locate true peaks.



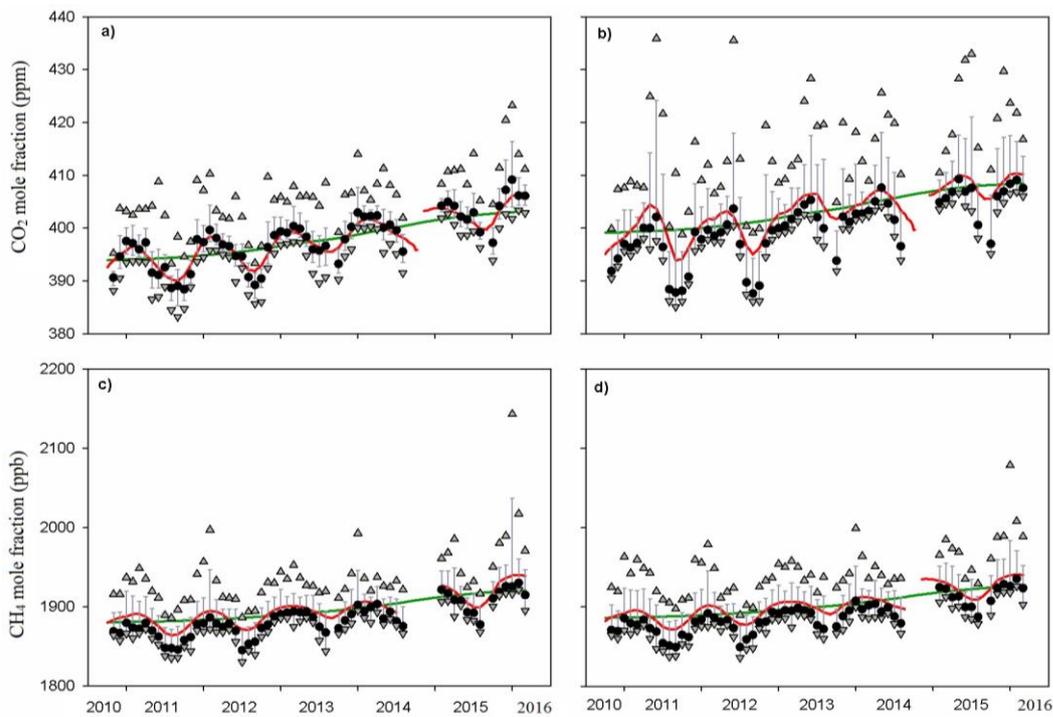
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291 **Fig. 1** Contour plots depicting the R^2 values of the average mole fractions for CO_2
 292 daytime (a), CO_2 night-time (b), CH_4 daytime (c) and CH_4 night-time data (d). The
 293 dashed line corresponds to the bandwidth chosen for each scenario.

294 3.2 Analysis of temporal variations

295 3.2.1 Trend analysis

296 Figure 2 shows the CO₂ and CH₄ trend evolution (green line) and modelled results (red
 297 line). Monthly median observations (black solid dots) were considered instead of semi-
 298 hourly data in order to reduce the noise and influence of extreme values. This allows
 299 better data interpretation over time, without much information being lost. The 10th and
 300 90th percentiles were also added in the graph in order to provide information about the
 301 monthly data range. Trend and modelled results were calculated by using the
 302 Epanechnikov Kernel due to its simplicity and widespread use (Rodríguez-Cortés et al.
 303 2015).



304

305 **Fig. 2** CO₂ and CH₄ annual trend evolution and modelled results for daytime CO₂ (a),
 306 night-time CO₂ (b), daytime CH₄ (c) and night-time CH₄ data (d). Black solid dots
 307 represent monthly median observations and grey lines indicate the interquartile range.
 308 The upper triangles correspond to the 90th percentile and the lower triangles correspond
 309 to the 10th percentile values. Finally, the green line represents the annual trend that
 310 shows an upward pattern, whereas the red line depicts data distribution modelled by
 311 applying the Epanechnikov kernel considering all the observations.

312 Table 2 presents the main statistics for annual CO₂ and CH₄ trend values in order to
313 obtain a quantitative description of their evolution over the study period.

314 **Table 2** Summary statistics for CO₂ and CH₄ trend values over the study period.

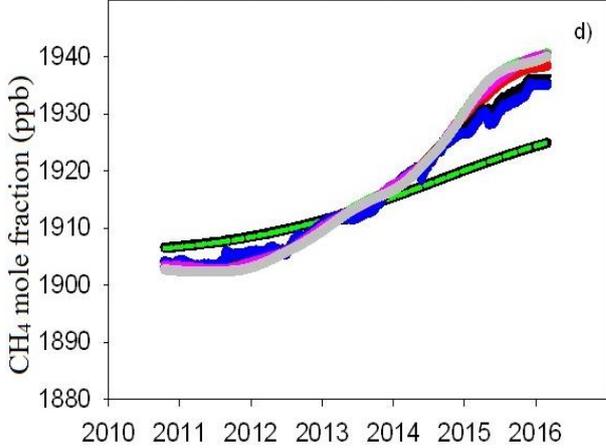
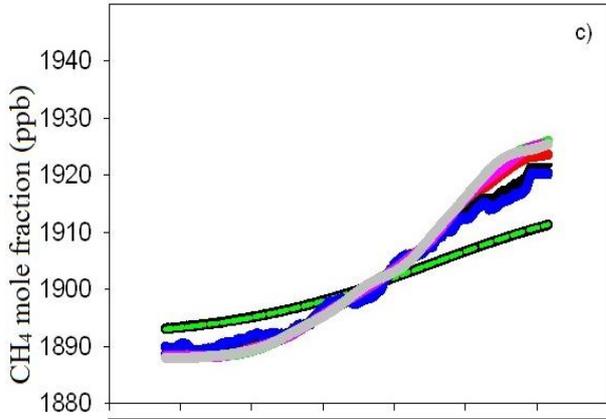
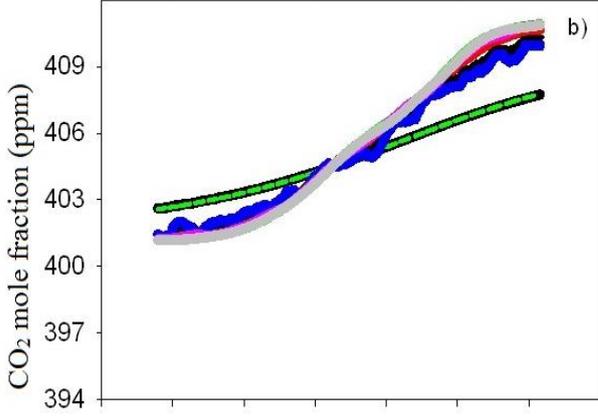
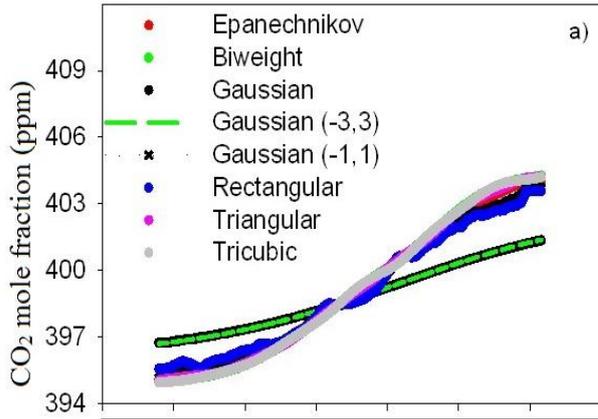
Year	2010*		2011		2012		2013		2014		2015		2016*	
CO ₂ (ppm)	Day	Night												
Mean	395.16	401.20	395.51	401.50	396.74	402.75	398.86	405.07	401.26	407.62	403.35	409.99	403.99	410.63
Median	395.16	401.20	395.47	401.44	396.69	402.68	398.87	405.12	401.23	407.61	403.38	410.11	403.98	410.63
Stand. Dev.	0.02	0.00	0.20	0.18	0.52	0.54	0.63	0.64	0.75	0.79	0.43	0.46	0.01	0.02
Interq. range	0.04	0.01	0.30	0.26	0.87	0.86	1.04	1.03	1.33	1.34	0.77	0.77	0.02	0.03
Min	395.12	401.19	395.21	401.21	395.93	401.91	397.74	403.85	399.98	406.23	402.52	409.00	403.96	410.60
Max	395.21	401.22	395.94	401.91	397.74	403.85	399.98	406.23	402.52	409.01	403.96	410.60	404.01	410.67
Skewness	2.32	3.14	22.37	30.80	12.74	18.46	-0.84	-5.30	0.71	0.42	-11.01	-26.44	2.59	2.52
Yule-Kendall	0.05	-0.10	0.28	0.52	0.12	0.14	-0.04	-0.13	0.07	0.03	-0.05	-0.26	0.04	0.06
Stand. Kurt.	-14.12	6.69	-23.55	-19.55	-30.07	-26.25	-30.28	-27.76	-33.67	-31.16	-33.18	-26.36	-13.20	-12.85
Robust Kurt.	0.30	0.25	0.28	0.26	0.30	0.29	0.30	0.29	0.32	0.30	0.32	0.30	0.32	0.30
CH ₄ (ppb)	Day	Night												
Mean	1888.40	1902.81	1889.01	1903.14	1892.40	1906.50	1899.15	1913.26	1908.93	1922.62	1919.90	1934.71	1923.45	1938.24
Median	1888.40	1902.81	1888.83	1902.91	1892.14	1906.16	1899.13	1913.30	1908.66	1922.25	1920.10	1935.29	1923.45	1938.23
Stand. Dev.	0.04	0.01	0.42	0.39	1.56	1.59	2.13	1.94	3.61	3.60	2.50	2.66	0.08	0.11
Interq. range	0.05	0.01	0.64	0.50	2.60	2.61	3.54	3.13	6.35	6.21	4.55	4.66	0.14	0.18
Min	1888.33	1902.78	1888.48	1902.82	1890.02	1904.16	1895.49	1909.77	1903.10	1916.94	1915.22	1929.26	1923.31	1938.06
Max	1888.49	1902.84	1890.03	1904.19	1895.50	1909.77	1903.11	1916.96	1915.22	1929.27	1923.32	1938.07	1923.60	1938.44
Skewness	8.23	20.70	45.97	67.80	18.64	23.87	4.18	2.10	6.54	11.25	-10.88	-23.21	2.54	2.45
Yule-Kendall	0.22	0.14	0.51	0.90	0.20	0.26	-0.01	-0.07	0.10	0.12	-0.05	-0.20	0.03	0.06
Stand. Kurt.	-7.67	19.14	-14.40	4.24	-28.71	-26.96	-30.29	-28.18	-33.38	-32.10	-34.40	-30.07	-13.04	-12.90
Robust Kurt.	0.26	0.22	0.30	0.26	0.30	0.30	0.30	0.29	0.32	0.31	0.33	0.32	0.31	0.30

*Refer to incomplete years measured. Year 2010 presents the results from 15th October to 31st December. Year 2016 presents the results from 1st January to 29th February.

315 According to the location measurements, both the mean and the median showed an
316 increased trend over time. Thus, an increase in the central data trend was inferred over
317 the study period. This upward trend can easily be explained on a global scale because of
318 the high annual increase in fossil fuel emissions in the northern temperate region (Piao
319 et al. 2017). On a smaller scale, the bulk of the Spanish economy is based on sectors
320 that emit large amounts of CO₂ to the atmosphere (Gutiérrez et al. 2008), which
321 partially explains the increasing CO₂ mean trend values presented in Table 2.
322 Furthermore, CH₄ emissions are the second main source of greenhouse gas emissions in
323 our country, as also reported Gutiérrez et al. (2008). Greater data dispersion was
324 observed from 2010 to 2014, since standard deviation and interquartile range were
325 higher during this time interval. Symmetry indicators, such as the Yule-Kendall index,
326 showed a general right-skewness distribution, which means that the distance between
327 the upper quartile and the median is greater than the distance between the median and
328 the lower quartile. Consequently, greater values than the median are predominant in the
329 dataset. As regards peakedness, almost negative standard kurtosis values were detected
330 for the data series, meaning that data distribution presents light tails and flatness when
331 compared to normal distribution (DeCarlo 1997). Robust kurtosis interpretation lies in
332 the same way. As pointed out by Sachs (1978), values above 0.263 were considered as
333 negative robust kurtosis. Negative robust kurtosis values were found (Table 2) for both
334 CO₂ and CH₄ in most years, indicating that data distribution for the study period
335 presents a wider peak (flatness) than normal distributions.

336 Analyses were performed by using the time as the independent variable, and mole
337 fractions as the dependent variable. The method depicts a smooth curve through the
338 points in a scatterplot by using Eq. (1). The kernel method produces smooth profiles
339 because the bandwidth plays the role of the smoothing parameter fitting the data (de

340 Haan 1999). The trend evolution of CO₂ and CH₄ was presented in Fig. 3. Smoother
341 curves were obtained with the Gaussian kernel, since all observations contribute to the
342 calculations. Furthermore, when it is not limited and when it is limited from (-3 to 3) the
343 Gaussian kernel presents the same graphical behaviour since the statistical weight is
344 nearly 0. Thus, both functions are virtually the same.



345

346 **Fig. 3** Trend fitting by different kernel functions. CO₂ daytime (a), CO₂ night-time (b),
 347 CH₄ daytime (c) and CH₄ night-time (d) results.

348 The long-term trend of atmospheric CO₂ and CH₄ reflected an increased pattern over
 349 time. From October 2010 to February 2016, CO₂ mean mole fractions at CIB were
 350 around 399 ppm during the daytime and 405 ppm during the night-time. These values
 351 were in consonance with global CO₂ values, which were around 395 ppm for the same
 352 period (NOAA 2017a). As regards CH₄, daytime mole fractions were approximately
 353 1.90 ppb and around 1.92 ppb during night-time. These results were in agreement with
 354 CH₄ mole fractions values for latitudes higher than 30°N, which were above 1.90 ppb in
 355 2015 (Pérez et al. 2017), and with global CH₄ mole fraction values, which were around
 356 1.8 ppb for the same study period (NOAA 2017b). These results were interpreted in
 357 terms of average growth rate (section 3.2.2. Average growth rate analysis).

358 The accuracy of each kernel was judged by how close the estimated value, obtained
 359 with kernel functions, is to the experimental data. R² values for the data trend were
 360 calculated and presented in Table 3. It should be taken into account that all the r-critical
 361 values (not presented here) were higher than the critical r-value (0.0003) for the dataset.
 362 Therefore, r-values for all the kernels studied were statistically significant with a P-
 363 value < 0.001. Thus, all the kernels are reliable and fit the data correctly, although some
 364 of them fit better for the data trend according to the results in Table 3.

365 **Table 3** R² values for CO₂ and CH₄ data trend, applying a bandwidth of 500-days.

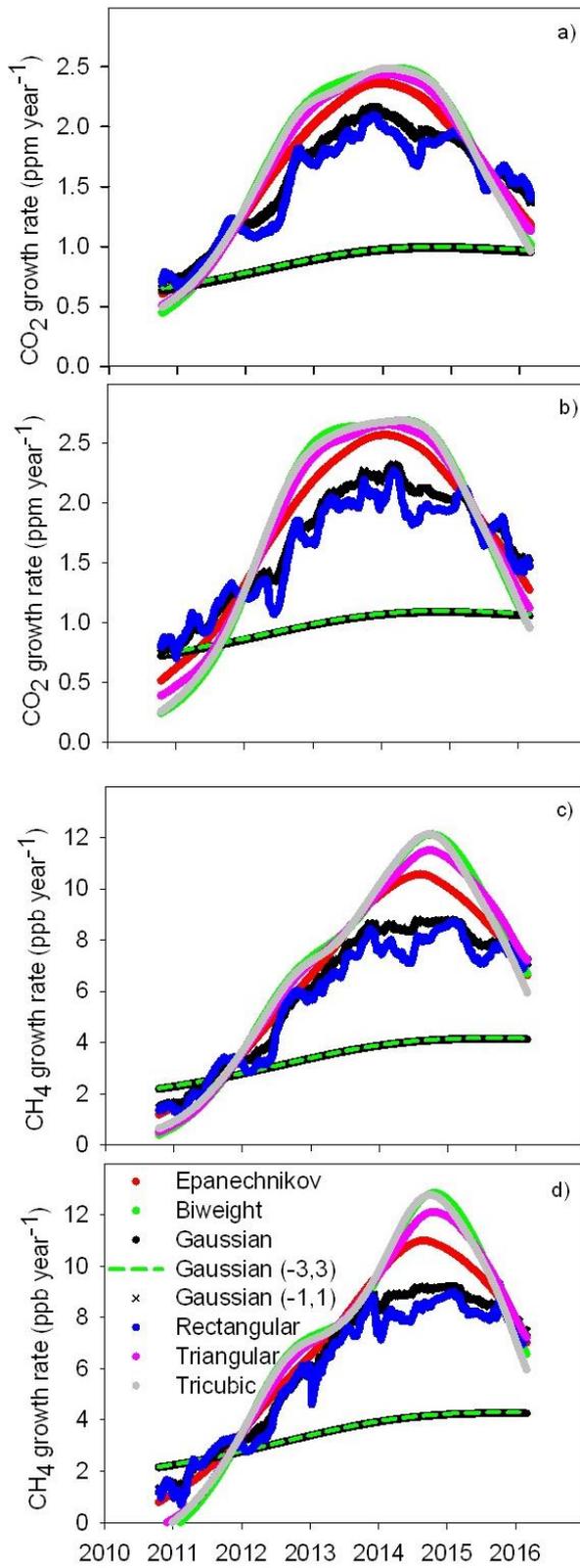
Kernel function	Daytime		Night-time	
	CO ₂	CH ₄	CO ₂	CH ₄
Epanechnikov	0.4360	0.2231	0.3708	0.1701

Biweight	0.4489	0.2329	0.3822	0.1760
Gaussian	0.3085	0.1554	0.2591	0.1180
Gaussian (-3,3)	0.3096	0.1559	0.2603	0.1185
Gaussian (-1,1)	0.4180	0.2113	0.3416	0.1628
Rectangular	0.4093	0.2059	0.3254	0.1599
Triangular	0.4461	0.2313	0.3803	0.1750
Tricubic	0.4473	0.2316	0.3812	0.1755

366 The average trend values agreed well for the six kernel functions employed (Table 3).
367 The functions overlap their distributions in the graphical output. This evidence is in line
368 with García-Portugués et al. (2014), since they consider minimal differences between
369 different kernel functions used in distribution data. However, two groups could be
370 inferred from Fig.3. A first group comprised the Gaussian and the Gaussian limited to (-
371 3,3), and a second group was made up of the other kernel functions. Slightly better
372 adjustments were obtained by applying the biweight kernel, and worse ones were
373 obtained with the Gaussian function since it employs the total real number line. Similar
374 R^2 values for the Gaussian and the Gaussian limited to (-3,3) could be inferred from
375 Table 3. In contrast, R^2 values increase around 9% for CO₂ data and 5% for CH₄ when
376 the Gaussian is limited to (-1,1) giving a better data fit, while computational time is cut
377 by half. R^2 values were higher for the daytime (around 0.40 for CO₂ and 0.21 for CH₄)
378 than during night-time (around 0.34 for CO₂ and 0.16 for CH₄). Moreover, CO₂ data fit
379 is better than CH₄ data fit, in agreement with the R^2 values. These empirical results
380 concur with those obtained by Rodríguez-Cortés et al. (2015), who advocate the
381 importance of the kernel function chosen in the data fit.

382 **3.2.2 Average growth rate analysis**

383 The long-term trend is frequently discussed in terms of variations in growth rate. As
384 stated by Zhu and Yoshikawa-Inoue (2015), research into the growth rate requires a
385 long recording period. According to Barlow et al. (2015), periods of over a year and a
386 half are good indicators. In this case, a database of five and a half years has been
387 studied. Kernel smoothing average growth rates were presented in Fig. 4, showing three
388 different groups with regard to graphical behaviour. The same two groups as for the
389 data trend were found, although a third group formed by the rectangular and the
390 Gaussian limited to $(-1,1)$ was also detected. The oscillatory behaviour of both functions
391 of this third group are partly caused by their lower efficiency (Table 1).



392

393 **Fig. 4** Average growth rate results for CO₂ daytime (a), CO₂ night-time (b), CH₄

394 daytime (c) and CH₄ night-time (d).

395 The overall CO₂ mean growth rate at CIB reached 1.72 ppm year⁻¹ (1.67 ppm year⁻¹ for
396 the daytime and 1.77 ppm year⁻¹ for night-time). This value was in agreement with that
397 found by Zhang et al. (2008) and Zhu and Yoshikawa-Inoue (2015), which were in the
398 range of 1.7 – 3.6 ppm year⁻¹.

399 As regards CH₄, the mean growth rate was 6.68 ppb year⁻¹ (6.65 ppb year⁻¹ for the
400 daytime and 6.71 ppb year⁻¹ for night-time). This result was in line with others reported
401 by Fang et al. (2016), Nisbet et al. (2014) and Vermeulen et al. (2011), which were in
402 the range of 6-10 ppb year⁻¹, in line with an in-depth analysis carried out by Pérez et al.
403 (2017).

404 Both gases presented an increasing linear rate with rapid growth from 2010 to 2014 and
405 then a decreasing linear pattern until the end. The same behaviour was depicted for
406 daytime and night-time records (Fig. 4). These increased long-term rates (trend and
407 average growth rate) were mainly attributed to the rise in anthropogenic emissions from
408 fossil fuel consumption that has increased globally from 1920 until the present (Le
409 Quéré et al. 2018). Moreover, changes in the climatology perturb growth rate behaviour
410 by shifts in the atmospheric circulation regime (Artuso et al. 2009). Climate affects
411 vegetation carbon fluxes by modifying biosphere respiration and photosynthesis
412 mechanisms (Artuso et al. 2009). Although global warming leads to a net positive
413 feedback to the carbon balance (Artuso et al. 2009) its contribution would only explain
414 a small part of the increasing trend pattern. Kim et al. (2015) also showed consistent
415 changes in the global growth rate of annual CH₄ mole fractions, with ups and downs
416 from the 1980s to 2010, although the reasons are not yet fully understood. The
417 decreasing CH₄ pattern, mainly evidenced from 2015 to 2016, agrees with global CH₄
418 growth rate values, since a decrease of around 3 ppb year⁻¹ was obtained on a global

419 scale (NOAA 2017d). CO₂ global growth rate values (NOAA 2017c) also show a
 420 decreasing pattern. However, the decreasing pattern reported on a global scale (NOAA
 421 2017c) is less pronounced (around 0.1 ppm year⁻¹) than the CIB results. Local CO₂
 422 emissions of anthropogenic activities in the surrounding area contribute to this value,
 423 although the contribution is only small compared to global background values. The
 424 main reason for this difference might stem from some border effect problems in the
 425 kernel regression functions method.

426 Night-time results were slightly higher than daytime results. During the night, soil and
 427 plant respiration together with stable stratification leads to higher values. By contrast,
 428 during the day, CO₂ uptake by vegetation through photosynthesis, as well as turbulent
 429 processes, cleans the lower atmosphere by convection.

430 Table 4 displays the average growth rate values for each kernel function used, showing
 431 differences for the Gaussian kernel function.

432 **Table 4** Average growth rate values for CO₂ and CH₄ at CIB from October 2010 to
 433 February 2016 applying a bandwidth of 500-days.

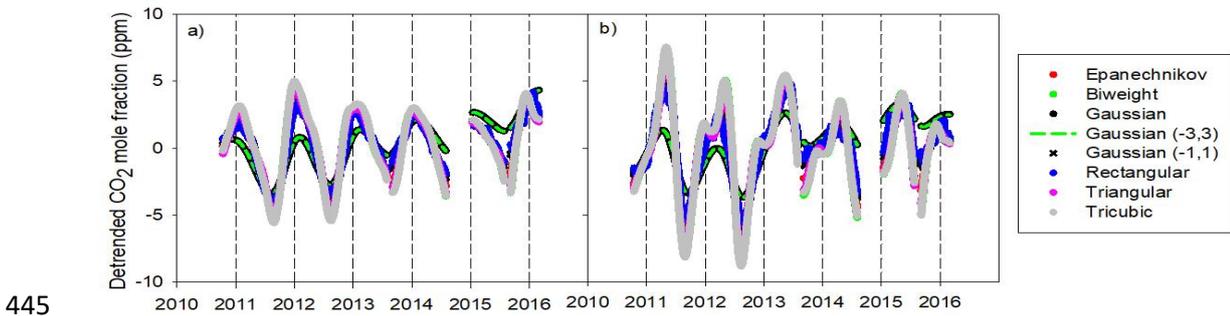
Kernel function	Daytime		Night-time	
	CO ₂	CH ₄	CO ₂	CH ₄
	(ppm year ⁻¹)	(ppb year ⁻¹)	(ppm year ⁻¹)	(ppb year ⁻¹)
Epanechnikov	1.69	6.73	1.81	6.83
Biweight	1.75	7.18	1.83	7.13
Gaussian	0.88	3.45	0.97	3.48
Gaussian (-3,3)	0.89	3.48	0.99	3.51

Gaussian (-1,1)	1.58	6.09	1.69	6.25
Rectangular	1.52	5.76	1.62	5.92
Triangular	1.73	7.05	1.83	7.03
Tricubic	1.75	7.12	1.84	7.11

434 The range of average growth rate values, considering neither the Gaussian kernel, when
435 limited to the interval calculation (-3, 3), nor when it is not limited, was narrow (Table
436 4). Both when limited to (-3,3) and when not limited, the Gaussian function showed
437 very different results compared to the other kernel functions. However, when the
438 Gaussian was limited to (-1,1), values doubled and approached those of the other
439 functions, in addition to which the data fit improved.

440 3.3.3 Analysis of the seasonal cycle

441 The kernel estimation of the cycle provides detailed information about changes in the
442 intra-annual evolution. Figures 5 and 6 present the seasonal evolution of CO₂ and CH₄,
443 respectively. In this case, a more similar graphical output was detected (Fig. 5 and 6),
444 which might be linked to smaller variability in the seasonal component.

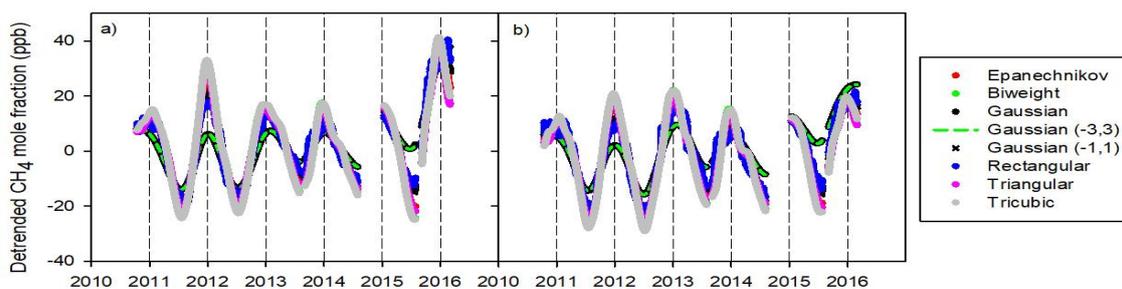


446 **Fig. 5** Smoothed detrended CO₂ seasonal cycle for the six kernel functions: CO₂
447 daytime (a) and CO₂ night-time (b) results.

448 The CO₂ seasonal cycle (Fig. 5) is mainly dominated by the physiological activity of
449 plants and soil respiration. The CO₂ daytime cycle (Fig. 5a) was characterized by a
450 decline from December to August and a subsequent rise. CO₂ mole fractions decrease
451 more rapidly from spring due to more intense photosynthetic activity, reaching the
452 minimum in August (-5.57 ppm). The site is covered by agricultural crops from autumn
453 to spring. However, coniferous trees and Mediterranean shrubs surrounding the site are
454 particularly vigorous from May to July, promoting photosynthesis as the days grow
455 longer. The peak in December (4.97 ppm) might be due to the cumulative effects of
456 CO₂ emission via root respiration as suggested Wu et al. (2012). This pattern was
457 consistent with those of many northern hemispheric locations (e.g., Wu et al. 2012;
458 Zhang et al. 2008).

459 Nocturnal CO₂ mole fractions (Fig. 5b) increased from August to April, and then
460 strongly decreased from May to August. This cycle was in line with that reported by
461 Barichivich et al. (2013). From Fig. 5b, two nocturnal maxima could be inferred. The
462 first was detected in spring (late April: 7.52 ppm) and the second in autumn (late
463 November: 1.88 ppm). Both maxima were linked to an increase in rainfall during spring
464 and autumn contributing to vegetation growth at the site, thus increasing respiration
465 rates at night-time. A cycle with two maxima was also described by Hatakka et al.
466 (2003) for CO₂ mole fractions at Pallas, Finland, from 1997 to 2003 (Pérez et al. 2017).
467 The minimum was reached in August (-8.81 ppm) linked to a biological minimum
468 attributed to slight plant and soil agricultural activities, decreasing the respiration rate.

469 Figure 6 showed a simpler cycle for CH₄ data, revealing positive values from summer to
470 winter, and negative ones from winter to summer, both during daytime and night-time
471 records.



472

473 **Fig. 6** Smoothed detrended CH₄ seasonal cycle for the six kernel functions: CH₄

474 daytime (a) and CH₄ night-time (b) results.

475 Meteorological conditions play an important role in the CH₄ cycle, since higher
 476 temperatures induce greater levels of OH radicals, which are the main CH₄ natural sink.
 477 Thus, the CH₄ maximum was reached in December (41.30 ppb for the daytime and
 478 24.20 ppb for night-time), while the CH₄ minimum was detected in July (-25.00 ppb for
 479 the daytime and -29.00 ppb for night-time). This cycle was in line with that observed at
 480 the Mauna Loa Observatory (MLO), although mole fractions at CIB were higher than
 481 those at MLO due to the greater sensitivity from emission sources at CIB. Furthermore,
 482 OH radical concentration decreases with latitude in the northern hemisphere (Kim et al.
 483 2015). MLO is located closer to the equator, such that the photochemical effect is
 484 stronger causing lower CH₄ mole fractions than at the CIB station.

485 CO₂ and CH₄ seasonal cycles reflected periodic behaviour and regular variations with
 486 small interannual variability. Differences between day and night were observed for both
 487 gases (Fig. 5 and 6), showing higher mole fractions during night-time. This was due to
 488 many superimposed causes: firstly, because of the meteorological conditions that
 489 favoured strong thermal temperature inversions at night, helping to trap CO₂ and CH₄
 490 emissions between the ground and the top of the boundary layer, and increasing their
 491 mole fraction values. Second, stable stratification at night together with the low
 492 boundary layer height at the site, 405 m, dampens vertical dispersion and transport from

493 the nearest cities, favouring the accumulation of locally-emitted pollutants. In contrast,
494 during the daytime, thermal turbulence induces convective movements, as well as the
495 expansion of the boundary layer, increasing up to 809 m at CIB, contributing to the
496 dispersion of both gases due to vertical mixing.

497 Atmospheric transport flows should also be considered when seeking to understand
498 seasonal patterns. Artuso et al. (2009) found an important influence of industrialized
499 Western Europe at the Lampedusa station from 1992 to 2007 in winter, when the
500 vegetation sink is less effective. The same origin might be attributed to our sampling
501 site, since García et al. (2016) reported that the main pollutant sources lie in Europe,
502 explaining the higher CO₂ mole fractions during this season. Furthermore, the influence
503 of fossil fuel consumption is greater during the cold months, enhancing the mole
504 fraction values. By contrast, clean air masses approaching the monitoring station from
505 the Atlantic are more frequent in summer (García et al. 2016), explaining CO₂ and CH₄
506 troughs during this season. High values of both CO₂ and CH₄ may also be related with
507 transport from the nearby cities of Valladolid (SE) and Palencia (NE) (Pérez et al.
508 2013). Additionally, atmospheric CH₄ mole fractions increase when air masses
509 originating from the southeast sector, where an urban landfill is located, reach the CIB
510 station (García et al. 2016). Finally, it should not be forgotten that the CIB station is
511 located in a region where livestock plays an important role (García et al. 2016; Sánchez
512 et al. 2014). Sánchez et al. (2014) reported almost 200 kt year⁻¹ CH₄ emissions due to
513 livestock in the region, which partly explains the higher CH₄ values at the CIB station.
514 An irregular amplitude evolution is inferred from Fig.5. This irregular pattern is
515 explained by the mathematical fitting method used in the current paper. Kernel
516 regression functions are based on local calculations, since only data within the
517 established bandwidth are considered. In fact, when harmonic equations were applied

518 to the same dataset a more regular and upward trend over time was obtained
 519 (Fernández-Duque et al. 2017). Furthermore, kernel regressions are more sensitive to
 520 gaps since they are only based on the values inside the bandwidth whereas harmonic
 521 equations consider the whole dataset for the calculations. From Fig. 5, summer minima
 522 increase over time was inferred whereas maxima mole fractions decrease over time. The
 523 CO₂ mean amplitude during the daytime was 7.81 ppm and was 11.45 ppm during
 524 night-time. These results were in agreement with those reported by Zhang et al. (2008)
 525 at the Waliguan (10.9 ppm) and Lin-an (11.5 ppm) stations. As regards CH₄ peak-to-
 526 peak amplitude (Fig. 6), a decreasing pattern over time was noticed although no major
 527 differences between daytime (41.54 ppb) and night-time (41.75 ppb) amplitude values
 528 were detected.

529 As for R² values for the seasonal component, they showed slight differences among the
 530 kernel functions employed (Table 5). As for the trend, r-values for all the kernels were
 531 statistically significant with a P-value < 0.001, such that all the kernels fit the dataset
 532 correctly. However, some differences in R² values were found among the kernels
 533 employed (Table 5).

534 **Table 5** R² values for the CO₂ and CH₄ seasonal component applying a bandwidth of
 535 80-days.

Kernel function	Daytime		Night-time	
	CO ₂	CH ₄	CO ₂	CH ₄
Epanechnikov	0.4236	0.2992	0.4473	0.2085
Biweight	0.4335	0.3053	0.4627	0.2128
Gaussian	0.4489	0.3041	0.3934	0.2195

Gaussian (-3,3)	0.4483	0.3037	0.3933	0.2192
Gaussian (-1,1)	0.4068	0.2874	0.4219	0.2002
Rectangular	0.3936	0.2789	0.3961	0.1932
Triangular	0.4328	0.3058	0.4671	0.2172
Tricubic	0.4314	0.3041	0.4558	0.2102

536 The Gaussian kernel provided the best description of the seasonal cycle for CO₂
537 daytime (0.45) and night-time CH₄ data (0.22), whereas a triangular function provided a
538 better fit for daytime CH₄ (0.31) and night-time CO₂ (0.47) results. In contrast, the
539 rectangular function provided the worst data adjustment, except in the case of the CO₂
540 nocturnal record, where the worst fit was obtained by using the Gaussian function
541 limited to (-3,3). Slight differences (3.5% for CO₂ data and 2% for CH₄) were found
542 when the Gaussian interval calculation was limited to (-1,1). This showed that limiting
543 the interval calculation did not prove as effective as for the trend with regard to the
544 seasonal component limit.

545 R² values fell to about 0.43 for CO₂ observations and to about 0.25 for CH₄ results,
546 indicating a better fit for CO₂ data than for CH₄ data, in agreement with the results
547 presented by Pérez et al. (2017).

548 No major differences were observed between daytime and night-time CO₂ results as
549 regards R² (Table 5). However, CH₄ daytime results (0.30) were slightly better than
550 night-time results (0.21).

551

552 **4 Conclusions**

553 This paper has demonstrated the usefulness of kernel regression for describing the
554 temporal variability of CO₂ and CH₄ in a Mediterranean rural area of the Spanish
555 plateau between 2010 and 2016.

556 We draw the following conclusions from our study:

- 557 (a) A novel procedure based on contour plots and its interpretation was proposed to
558 determine two optimal bandwidths at the same time. This methodology is easy,
559 quick and reproducible; thus its general use may be plausible.
- 560 (b) Temporal patterns were similar for the six kernel functions employed, obtaining
561 satisfactory R² values, since r-values for all the kernels used were higher than
562 the r-critical values for our specific dataset.
- 563 (c) As regards the data trend, the best fit was reached with the biweight kernel and
564 the worst with the Gaussian because its calculation comprises the whole real
565 line.
- 566 (d) For seasonal evolution, the triangular and the Gaussian kernel assumed the role
567 as best predictors. In contrast, the worst fits were obtained with the rectangular,
568 which could be attributed to a border effect.
- 569 (e) The differences between the kernels for the seasonal component were lower than
570 those for the trend, which could be due to slight seasonal data variability. The
571 Gaussian kernel presented a clearly different graphical behaviour because its
572 calculation comprises the whole real line.
- 573 (f) Additional run-time was needed when the Gaussian kernel was used since it is
574 involved in all observations. Shortening the interval calculation to (-3,3) did not
575 prove successful either for a decrease in calculation speed or for an increase in
576 R² values. However, when the interval calculation was limited to (-1,1), R²

577 values increased substantially for the trend, and time calculation was cut by half.
578 As regards the seasonal component, R^2 did not improve although average
579 growth rate values performed far better and approached the values obtained with
580 the other kernel functions. Thus, limiting the interval calculation to (-1,1)
581 significantly increased the flexibility of the Gaussian kernel, making the
582 calculation computationally feasible.

583 (g) Linear growth rates ($1.72 \text{ ppm year}^{-1}$ for CO_2 and $6.68 \text{ ppb year}^{-1}$ for CH_4) were
584 recorded in the research period. Anthropogenic emissions from fossil fuel
585 consumption and other industrial activities on a global scale contributed to the
586 notable increase.

587 (h) The combined effects of biological and physical processes resulted in
588 differences between day and night-time for both CO_2 and CH_4 seasonal cycles.
589 Lower mole fractions during the daytime were found due to thermal turbulence
590 and higher planetary boundary layer height. Higher values at night were linked
591 to stable stratification, lower boundary planetary height and thermal inversions.
592 Focusing on CO_2 , the influence of the terrestrial ecosystem was apparent,
593 contributing to lower values during the daytime due to photosynthesis and
594 higher values at night-time due to soil and plant respiration.

595 (i) Apart from the biological effects, during the winter, European airmasses might
596 be linked to higher CO_2 mole fraction values in winter due to large industrial
597 emissions. In summertime, the effect of masses from the Atlantic prevailed,
598 which explains the lower CO_2 and CH_4 mole fractions. An urban influence in the
599 SE direction was observed for the CH_4 results, accounting for the higher values.

600 Selecting the optimal bandwidth proves key in kernel regressions if good data
601 interpretation is to be achieved. Thus, we recommend choosing the bandwidth based on
602 the special characteristics of the time series, and not based on the typical values used in
603 the literature. Further inquiry is needed to improve the methodology described here for a
604 more precise bandwidth determination. As regards the kernel functions employed, no
605 major differences affecting temporal pattern interpretation were found between the
606 different kernels. Moreover, since R^2 values were very similar for the six kernels, we
607 recommend using those which involve least computational effort. All the kernels
608 employed have virtually the same computational effort, except the Gaussian when it is
609 not limited to $(-1,1)$. As a result, we recommend shortening the calculation interval.
610 However, it could be interesting to use more than one kernel function so as to ensure
611 results are consistent, reproducible, and free from bias. Finally, we consider it important
612 to extend the use of these functions to other areas and to other important greenhouse
613 gases. Their application may improve current knowledge of temporal patterns and help
614 gain a better insight into how gases evolve in the low atmosphere.

615

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